

CASC

1.0.5

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# Chapter 1

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by James Random Hacker.
```

```
signature of Ty Coon, 1 April 1990  
Ty Coon, President of Vice
```

That's all there is to it!



## Chapter 2

# Colored Abstract Simplicial Complex (CASC) Library

Master CI:    Development CI:

CASC is a modern and header-only C++ library which provides a data structure to represent arbitrary dimension abstract simplicial complexes with user-defined classes stored directly on the simplices at each dimension. This is achieved by taking advantage of the combinatorial nature of simplicial complexes and new C++ code features such as: variadic templates and automatic function return type deduction. Essentially CASC stores the full topology of the complex according to a [Hasse diagram](#). The representation of the topology is decoupled from interactions of user data through the use of metatemplate programming.

### 2.1 Getting Started

These instructions will get you a copy of the project up and running on your local machine for development and testing purposes.

#### 2.1.1 Prerequisites

CASC does not have any dependencies other than the C++ standard library. If you wish to use CASC, you can use the header files right away. There is no binary library to link to, and no configured header file. CASC is a pure template library defined in the headers.

We use the CMake build system (version 3+), but only to build the documentation and unit-tests, and to automate installation.

Doxygen and Graphviz is used to generate the documentation.

To use CASC in your software all you will need is a working C++ compiler with full C++14 support. This includes:

- GCC Versions 5+
- Clang Versions 3, 5+<sup>†</sup>
- XCode 8+<sup>†</sup>

<sup>†</sup> Note that there is a known issue with Clang 4.x.x versioned compilers (including XCode version 9.[0-2]), where the most specialized unique specialization is not selected leading to a compiler error. The current workaround to this problem is to either use GCC or to obtain Clang version 5+ (XCode version 9.3beta+).

### 2.1.2 Installing

CASC is header only meaning that there is nothing to compile out of the box. To use CASC, simply copy the desired headers into your project and included as necessary. If you wish to install CASC using CMake to your system, even though the library is header only, you must first create a new folder to prevent in-source "builds".

```
mkdir build
cd build
```

Subsequently run CMake specifying the installation prefix and the path to the root level `CMakeLists.txt` file.

```
cmake -DCMAKE_INSTALL_PREFIX=/usr/local/ ..
make install
```

Unit tests are also packaged along with CASC and are dependent upon [Googles C++ test framework](#). If you wish to build and run the tests, set the flag `-DBUILD_CASCTESTS=on` in your CMake command. CMake will then download and build `googletest` and link it with the CASC unit tests.

```
cmake -DBUILD_CASCTESTS=on ..
make
make tests          # Run tests through make
./bin/casctests     # Alternatively run the tests directly (more verbose)
```

Additional examples provided with CASC can be built in a similar fashion by passing the `-DBUILD_CASCEXAMPLES=on` flag to CMake.

### 2.1.3 Documentation

A current version of the documentation is available online via [github pages](#). You can also build the documentation locally if you have Doxygen and Graphviz on your system. CMake will automatically try to find a working Doxygen installation. If Doxygen is found then the documentation can be built using `make casc_doc`. Otherwise CMake will report that it could not find Doxygen.

## 2.2 Versioning & Contributing

We use [Github](#) for versioning. For the versions available, please see the [releases](#). If you find a bug or wish to request additional functionality please file an issue in the [CASC Github project](#).

## 2.3 Authors

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University of California, San Diego

See also the list of [contributors](#) who participated in this project.

## 2.4 License

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## 2.5 Acknowledgments

This project is supported by the National Institutes of Health under grant numbers P41-GM103426 ( [NBCR](#)), T32-GM008326, and R01-GM31749. It is also supported in part by the National Science Foundation under awards DMS-CM1620366 and DMS-FRG1262982.



## Chapter 3

# Building the documentation

The documentation for CASC can be generated locally using [Doxygen](#). You must have a working copy of doxygen installed on your machine in order to build the documentation.

If CMake is able to find your doxygen installation then the following sequence of commands will build the basic documentation.

```
cmake ..  
make casc_doc
```

### 3.0.1 Documentation for Developers

If you are contributing to or modifying the CASC library you may wish to document private class members or currently hidden metatemplate helper functions. Whether or not documentation for these items is generated can be controlled by modifying the default doxygen configuration: `doc/Doxyfile.in`.

To document private class functions and members toggle: `EXTRACT_PRIVATE = YES`

To enable metatemplate helper functions enable the conditional: `ENABLED_SECTIONS = detail`





## Chapter 4

# Frequently Asked Questions

### 1. Why is my simplex data not storing correctly?

If you are retrieving the data from the `SimplexID` using the dereference operator, you must retrieve the result as a reference in order to modify it. See the following example.

```
MeshType mesh = MeshType();
int key = mesh.insert({1}, 10);
auto data = *mesh.get_simplex_up({key});
data = 5;
std::cout << *mesh.get_simplex_up({key}); << std::endl // Prints 10

auto &dataRef = *mesh.get_simplex_up({key});
dataRef = 5;
std::cout << *mesh.get_simplex_up({key}) << std::endl // Prints 5
```



## Chapter 5

# Namespace Index

### 5.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

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<a href="#">index_tracker::index_tracker_detail</a>	B-tree internal data structures . . . . .	42
<a href="#">util</a>	Metatemplate programming utilities namespace . . . . .	44



## Chapter 6

# Data Structure Index

### 6.1 Data Structures

Here are the data structures with brief descriptions:

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An array based BTree . . . . .	47
<a href="#">casc::simplicial_complex&lt; traits &gt;::EdgeID&lt; k &gt;</a>	
External reference to an edge or a connection within the complex . . . . .	48
<a href="#">index_tracker::index_tracker&lt; _T, _d &gt;</a>	
Tracker of available indices implemented as a B-tree of intervals . . . . .	50
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Class representing the orientation . . . . .	54
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A range object to support range based for loops . . . . .	54
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Helper to get the kth element from a <a href="#">type_holder</a> . . . . .	95
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Specialization to recursively pop types to get the kth type . . . . .	96

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Queue based data structure to hold list of types	97
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Partial specialization to allow FIFO access of typenamees	97
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Map the types in C into V<T>	98
<a href="#">util::type_swap&lt; TUPLE, HOLDER_FULL &gt;</a>	
Move a list of types from one container to another	99
<a href="#">util::type_swap&lt; TUPLE, HOLDER&lt; Ts... &gt; &gt;</a>	
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# Chapter 7

## File Index

### 7.1 File List

Here is a list of all documented files with brief descriptions:

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## Chapter 8

# Namespace Documentation

### 8.1 casc Namespace Reference

Namespace for everything CASC.

#### Data Structures

- struct [Orientable](#)  
*Class representing the orientation.*
- struct [SimplexMap](#)  
*A multimap to represent a map of simplex indices to a set of simplices.*
- struct [SimplexSet](#)  
*A multiset to store simplices in a [simplicial\\_complex](#).*
- class [simplicial\\_complex](#)  
*The CASC data structure for representing simplicial complexes of arbitrary dimensionality with coloring.*

#### Typedefs

- template<typename KeyType, typename ... Ts>  
using [AbstractSimplicialComplex](#)
- template<typename T>  
using [NodeSet](#)  
*Helpful alias defining a `unordered_set` of simplices. See also `hashSimplexID`.*

#### Functions

- template<typename Complex>  
void [getStar](#) (Complex &F, [casc::SimplexSet](#)< Complex > &S, [casc::SimplexSet](#)< Complex > &dest)  
*Gets the star of a [SimplexSet](#).*
- template<typename Complex, typename Simplex>  
void [getStar](#) (Complex &F, Simplex &s, [casc::SimplexSet](#)< Complex > &dest)  
*Gets the star of a simplex.*
- template<typename Complex>  
void [getClosure](#) (Complex &F, [casc::SimplexSet](#)< Complex > &S, [casc::SimplexSet](#)< Complex > &dest)

- Gets the closure of a simplex set.*

  - `template<typename Complex, typename Simplex>`  
`void getClosure (Complex &F, Simplex &s, casc::SimplexSet< Complex > &dest)`

*Compute the closure of a simplex.*

  - `template<typename Complex>`  
`void getLink (Complex &F, casc::SimplexSet< Complex > &S, casc::SimplexSet< Complex > &dest)`

*Gets the link of a [SimplexSet](#).*

  - `template<typename Complex, typename Simplex>`  
`void getLink (Complex &F, Simplex &s, casc::SimplexSet< Complex > &dest)`

*Gets the link of a simplex.*

  - `template<typename Complex>`  
`void writeDOT (const std::string &filename, Complex &F)`

*Writes out the topology of an ASC into the dot format.*

  - `template<typename Visitor, typename SimplexID>`  
`void visit\_BFS\_up (Visitor &&v, typename SimplexID::complex &F, SimplexID s)`

*Traverse BFS up the complex and apply a visitor function to each simplex visited.*

  - `template<typename Visitor, typename SimplexID>`  
`void visit\_BFS\_down (Visitor &&v, typename SimplexID::complex &F, SimplexID s)`

*Traverse BFS down the complex and apply a visitor function to each simplex visited.*

  - `template<typename Visitor, typename EdgeID>`  
`void edge\_up (Visitor &&v, typename EdgeID::complex &F, EdgeID s)`

*Traverse across edges BFS.*

  - `template<class Complex, std::size_t level, class InsertIter>`  
`void neighbors (Complex &F, typename Complex::template SimplexID< level > nid, InsertIter iter)`

*Push the immediate face neighbors into the provided iterator.*

  - `template<class Complex, class SimplexID, class InsertIter>`  
`void neighbors (Complex &F, SimplexID nid, InsertIter iter)`

*This is a helper function to assist neighbors to automatically deduce the integral level.*

  - `template<class Complex, std::size_t level, class InsertIter>`  
`void neighbors\_up (Complex &F, typename Complex::template SimplexID< level > nid, InsertIter iter)`

*Push the immediate coface neighbors into the provided iterator.*

  - `template<class Complex, class SimplexID, class InsertIter>`  
`void neighbors\_up (Complex &F, SimplexID nid, InsertIter iter)`

*This is a helper function to assist neighbors to automatically deduce the integral level.*

  - `template<class Complex, std::size_t level, typename Iterator>`  
`void kneighbors\_up (Complex &F, int ring, std::set< typename Complex::template SimplexID< level > > &nbors, Iterator begin, Iterator end)`

*Code for returning a set of k-ring neighbors.*

  - `template<class Complex, class SimplexID>`  
`void kneighbors\_up (Complex &F, SimplexID nid, int ring, std::set< SimplexID > &nbors)`

*Helper function to help [kneighbors\\_up](#) to deduce the integral level of SimplexID.*

  - `template<class Complex, std::size_t level, typename Iterator>`  
`void kneighbors (Complex &F, int ring, std::set< typename Complex::template SimplexID< level > > &nbors, Iterator begin, Iterator end)`

*Code for returning a set of k-ring neighbors.*

  - `template<class Complex, class SimplexID>`  
`void kneighbors (Complex &F, SimplexID nid, int ring, std::set< SimplexID > &nbors)`

*Helper function to help [kneighbors](#) to deduce the integral level of SimplexID.*

  - `template<typename Complex>`  
`void perform\_removal (Complex &F, casc::SimplexSet< Complex > &S)`

*Remove simplex in [SimplexSet](#) S from complex F.*

  - `template<typename Complex>`  
`void perform\_insertion (Complex &F, typename decimation_detail::SimplexDataSet< Complex >::type &S)`

Insert all simplices in [SimplexSet](#)  $S$  into complex  $F$

- template<typename Complex, template< typename > class Callback>  
void [run\\_user\\_callback](#) (Complex &F, [casc::SimplexMap](#)< Complex > &S, Callback< Complex > &&clbk,  
typename decimation\_detail::SimplexDataSet< Complex >::type &rv)

Run the user specified callback function.

- template<typename Complex, typename Simplex, template< typename > class Callback>  
void [decimate](#) (Complex &F, Simplex s, Callback< Complex > &&clbk)

Decimate a simplex of any dimension while considering any meta-data stores on decimated simplices.

- template<typename Complex, typename Simplex>  
Complex::KeyType [decimateFirstHalf](#) (Complex &F, Simplex s, [SimplexMap](#)< Complex > &simplexMap)

Given a simplex to decimate generate a pre-post mapping.

- template<typename Complex>  
void [decimateBackHalf](#) (Complex &F, [SimplexMap](#)< Complex > &simplexMap, typename decimation\_detail::SimplexDataSet< Complex >::type &rv)

Given a simplexMap and mapped resulting data execute the decimation.

- template<typename Complex>  
void [init\\_orientation](#) (Complex &F)

Initialize the partial ordering of the simplex edges.

- template<typename Complex>  
void [clear\\_orientation](#) (Complex &F)

Clear the orientation of the facets.

- template<typename Complex>  
std::tuple< int, bool, bool > [compute\\_orientation](#) (Complex &F)

Initializes and calculates the orientation of a [simplicial\\_complex](#).

- template<typename Complex>  
std::tuple< int, bool, bool > [check\\_orientation](#) (Complex &F)

Checks for self consistent orientation and fill in missing orientations.

- template<std::size\_t k, typename Complex>  
static auto & [get](#) ([SimplexMap](#)< Complex > &S)

Get the map for a simplex dimension.

- template<std::size\_t k, typename Complex>  
static auto & [get](#) (const [SimplexMap](#)< Complex > &S)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

- template<std::size\_t k, typename Complex>  
static auto & [get](#) ([SimplexSet](#)< Complex > &S)

Get the [NodeSet](#) for a simplex dimension from a [SimplexSet](#).

- template<std::size\_t k, typename Complex>  
static auto & [get](#) (const [SimplexSet](#)< Complex > &S)

- template<typename Complex>  
bool [operator==](#) (const [SimplexSet](#)< Complex > &lhs, const [SimplexSet](#)< Complex > &rhs)

Compare if the sets are equivalent.

- template<typename Complex>  
bool [operator!=](#) (const [SimplexSet](#)< Complex > &lhs, const [SimplexSet](#)< Complex > &rhs)

Compare if the sets are not equivalent.

- template<typename Complex>  
static void [set\\_union](#) (const [SimplexSet](#)< Complex > &A, const [SimplexSet](#)< Complex > &B, [SimplexSet](#)< Complex > &dest)

Compute the set union.

- template<typename Complex>  
static void [set\\_intersection](#) (const [SimplexSet](#)< Complex > &A, const [SimplexSet](#)< Complex > &B, [SimplexSet](#)< Complex > &dest)

Compute the set intersection.

- `template<typename Complex>`  
`static void set_difference (const SimplexSet< Complex > &A, const SimplexSet< Complex > &B,`  
`SimplexSet< Complex > &dest)`  
*Compute the set difference.*
- `template<typename T, std::size_t k>`  
`std::string to_string (const std::array< T, k > &A)`  
*Returns a string representation of the vertex subsimplicies of a given simplex.*

## 8.1.1 Typedef Documentation

### 8.1.1.1 AbstractSimplicialComplex

```
template<typename KeyType, typename ... Ts>
using casc::AbstractSimplicialComplex
```

**Initial value:**

```
simplicial_complex<
    detail::simplicial_complex_traits_default<KeyType, Ts...> >
```

Alias to generate a CASC from a list of traits. See also `simplicial_complex_traits_default`. Example – To create a tetrahedral mesh with integer data on all simplices:

```
auto mesh = AbstractSimplicialComplex<
    int, // KEYTYPE
    int, // Root data
    int, // Vertex data
    int, // Edge data
    int, // Face data
    int  // Volume data
>();
```

### 8.1.1.2 NodeSet

```
template<typename T>
using casc::NodeSet
```

**Initial value:**

```
std::unordered_set<T, simplex_set_detail::hashSimplexID<T> >
```

## 8.1.2 Function Documentation

### 8.1.2.1 check\_orientation()

```
template<typename Complex>
std::tuple< int, bool, bool > casc::check_orientation (
    Complex & F)
```

**Parameters**

<i>F</i>	Simplicial_complex
----------	--------------------

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
----------------	--

## Returns

A tuple of the number of connected components, where the complex is orientable, and if it is psuedo manifold.

## 8.1.2.2 clear\_orientation()

```
template<typename Complex>
void casc::clear_orientation (
    Complex & F)
```

## Parameters

<i>F</i>	Simplicial complex of interest
----------	--------------------------------

## Template Parameters

<i>Complex</i>	Typename of the simplicial complex
----------------	------------------------------------

## 8.1.2.3 compute\_orientation()

```
template<typename Complex>
std::tuple< int, bool, bool > casc::compute_orientation (
    Complex & F)
```

## Parameters

<i>F</i>	Simplicial_complex
----------	--------------------

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
----------------	--

## Returns

A tuple of the number of connected components, where the complex is orientable, and if it is psuedo manifold.

## 8.1.2.4 decimate()

```
template<typename Complex, typename Simplex, template< typename > class Callback>
void casc::decimate (
    Complex & F,
    Simplex s,
    Callback< Complex > && clbk)
```

## Parameters

in	<i>F</i>	<a href="#">simplicial_complex</a> to operate on.
in	<i>s</i>	Simplex to decimate.
in	<i>clbk</i>	Callback function to map meta-data

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a>
<i>Simplex</i>	Typename of the simplex
<i>Callback</i>	Typename of the template template callback functor

Alias for [SimplexSet](#)

Alias for [SimplexMap](#)

8.1.2.5 `decimateBackHalf()`

```
template<typename Complex>
void casc::decimateBackHalf (
    Complex & F,
    SimplexMap< Complex > & simplexMap,
    typename decimation_detail::SimplexDataSet< Complex >::type & rv)
```

## Parameters

<i>F</i>	Simplicial complex to operate on
<i>simplexMap</i>	<a href="#">SimplexMap</a> mapping simplices before and after decimation
<i>rv</i>	Resulting data for each simplex

## Template Parameters

<i>Complex</i>	Typename of the complex of interest
----------------	-------------------------------------

8.1.2.6 `decimateFirstHalf()`

```
template<typename Complex, typename Simplex>
Complex::KeyType casc::decimateFirstHalf (
    Complex & F,
    Simplex s,
    SimplexMap< Complex > & simplexMap)
```

## Parameters

in	<i>F</i>	<a href="#">simplicial_complex</a> to operate on.
in	<i>s</i>	Simplex to decimate.
	<i>simplexMap</i>	The simplex map to populate

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a>
<i>Simplex</i>	Typename of the simplex

Alias for [SimplexSet](#)

## 8.1.2.7 edge\_up()

```
template<typename Visitor, typename EdgeID>
void casc::edge_up (
    Visitor && v,
    typename EdgeID::complex & F,
    EdgeID s)
```

## Parameters

in	<i>v</i>	Visitor functor to apply.
	<i>F</i>	The <a href="#">simplicial_complex</a> to traverse.
in	<i>s</i>	The edge to start at.

## Template Parameters

<i>Visitor</i>	Typename of the functor.
<i>EdgeID</i>	Typename of the edge.

## 8.1.2.8 get() [1/3]

```
template<std::size_t k, typename Complex>
static auto & casc::get (
    const SimplexSet< Complex > & S) [inline], [static]
```

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

## 8.1.2.9 get() [2/3]

```
template<std::size_t k, typename Complex>
static auto & casc::get (
    SimplexMap< Complex > & S) [inline], [static]
```

## Parameters

<i>S</i>	<a href="#">SimplexMap</a> to retrieve from.
----------	--

## Template Parameters

<i>k</i>	Simplex dimension.
<i>Complex</i>	Typename of the complex.

## Returns

Returns a map of `std::Array<KeyType, k>` to [SimplexSet](#).

8.1.2.10 `get()` [3/3]

```
template<std::size_t k, typename Complex>
static auto & casc::get (
    SimplexSet< Complex > & S) [inline], [static]
```

## Parameters

<i>S</i>	<a href="#">SimplexSet</a> of interest.
----------	---

## Template Parameters

<i>k</i>	Simplex dimension desired.
<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .

## Returns

A [NodeSet](#) which holds simplices of dimension 'k' and a member of [SimplexSet](#) 'S'.

8.1.2.11 `getClosure()` [1/2]

```
template<typename Complex>
void casc::getClosure (
    Complex & F,
    casc::SimplexSet< Complex > & S,
    casc::SimplexSet< Complex > & dest)
```

## Parameters

in	<i>F</i>	Complex of interest.
in	<i>S</i>	<a href="#">SimplexSet</a> to compute the closure of.
out	<i>dest</i>	Destination <a href="#">SimplexSet</a>

## Template Parameters

<i>Complex</i>	Typename of the complex.
----------------	--------------------------

8.1.2.12 `getClosure()` [2/2]

```
template<typename Complex, typename Simplex>
void casc::getClosure (
    Complex & F,
    Simplex & s,
    casc::SimplexSet< Complex > & dest)
```



## Parameters

in	<i>F</i>	Complex of interest.
in	<i>s</i>	Simplex of interest.
out	<i>dest</i>	Destination <a href="#">SimplexSet</a> .

## Template Parameters

<i>Complex</i>	Typename of the complex.
<i>Simplex</i>	Typename of the simplex.

8.1.2.13 `getLink()` [1/2]

```
template<typename Complex>
void casc::getLink (
    Complex & F,
    casc::SimplexSet< Complex > & S,
    casc::SimplexSet< Complex > & dest)
```

## Parameters

in	<i>F</i>	Complex of interest.
in	<i>S</i>	<a href="#">SimplexSet</a> to get the link of.
out	<i>dest</i>	Destination <a href="#">SimplexSet</a> .

## Template Parameters

<i>Complex</i>	Typename of the complex.
----------------	--------------------------

8.1.2.14 `getLink()` [2/2]

```
template<typename Complex, typename Simplex>
void casc::getLink (
    Complex & F,
    Simplex & s,
    casc::SimplexSet< Complex > & dest)
```

## Parameters

<i>F</i>	Complex of interest.
<i>s</i>	Simplex of interest.
<i>dest</i>	Destination <a href="#">SimplexSet</a> .

## Template Parameters

<i>Complex</i>	Typename of the complex.
<i>Simplex</i>	Typename of the simplex.

**8.1.2.15 getStar() [1/2]**

```
template<typename Complex>
void casc::getStar (
    Complex & F,
    casc::SimplexSet< Complex > & S,
    casc::SimplexSet< Complex > & dest)
```

**Parameters**

in	<i>F</i>	Complex of interest.
in	<i>S</i>	<a href="#">SimplexSet</a> to compute the star of.
out	<i>dest</i>	Destination <a href="#">SimplexSet</a> .

**Template Parameters**

<i>Complex</i>	Typename of the complex.
----------------	--------------------------

**8.1.2.16 getStar() [2/2]**

```
template<typename Complex, typename Simplex>
void casc::getStar (
    Complex & F,
    Simplex & s,
    casc::SimplexSet< Complex > & dest)
```

**Parameters**

in	<i>F</i>	Complex of interest.
	<i>s</i>	Simplex to get the star of.
out	<i>dest</i>	Destination <a href="#">SimplexSet</a> .

**Template Parameters**

<i>Complex</i>	Typename of the complex.
<i>Simplex</i>	Typename of the simplex.

**8.1.2.17 init\_orientation()**

```
template<typename Complex>
void casc::init_orientation (
    Complex & F)
```

**Parameters**

<i>F</i>	Simplicial complex of interest
----------	--------------------------------

## Template Parameters

<i>Complex</i>	Typename of the simplicial complex
----------------	------------------------------------

## 8.1.2.18 kneighbors() [1/2]

```
template<class Complex, std::size_t level, typename Iterator>
void casc::kneighbors (
    Complex & F,
    int ring,
    std::set< typename Complex::template SimplexID< level > > & nbors,
    Iterator begin,
    Iterator end)
```

## Parameters

in	<i>F</i>	The <a href="#">simplicial_complex</a> to traverse.
in	<i>ring</i>	The number of rings of neighbors to collect.
out	<i>nbors</i>	Set of previously seen simplices.
in	<i>begin</i>	The begin
in	<i>end</i>	The end

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
<i>level</i>	Simplex dimension of the simplex and neighbors.
<i>Iterator</i>	{ description }

## 8.1.2.19 kneighbors() [2/2]

```
template<class Complex, class SimplexID>
void casc::kneighbors (
    Complex & F,
    SimplexID nid,
    int ring,
    std::set< SimplexID > & nbors)
```

## Parameters

in	<i>F</i>	The simplicial complex
in	<i>nid</i>	Simplex of interest to get the neighbors of.
in	<i>ring</i>	The number of rings to include as a neighbor.
out	<i>nbors</i>	Set of neighbors to populate.

## Template Parameters

<i>Complex</i>	Typename of the complex.
<i>SimplexID</i>	Typename of the SimplexID.

**8.1.2.20 neighbors\_up()** [1/2]

```
template<class Complex, std::size_t level, typename Iterator>
void casc::neighbors_up (
    Complex & F,
    int ring,
    std::set< typename Complex::template SimplexID< level > > & nbors,
    Iterator begin,
    Iterator end)
```

**Parameters**

in	<i>F</i>	The <a href="#">simplicial_complex</a> to traverse.
in	<i>ring</i>	The number of rings of neighbors to collect.
out	<i>nbors</i>	Set of previously seen simplices.
in	<i>begin</i>	The begin
in	<i>end</i>	The end

**Template Parameters**

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
<i>level</i>	Simplex dimension of the simplex and neighbors.
<i>Iterator</i>	{ description }

**8.1.2.21 neighbors\_up()** [2/2]

```
template<class Complex, class SimplexID>
void casc::neighbors_up (
    Complex & F,
    SimplexID nid,
    int ring,
    std::set< SimplexID > & nbors)
```

**Parameters**

in	<i>F</i>	The simplicial complex
in	<i>nid</i>	Simplex of interest to get the neighbors of.
in	<i>ring</i>	The number of rings to include as a neighbor.
out	<i>nbors</i>	Set of neighbors to populate.

**Template Parameters**

<i>Complex</i>	Typename of the complex.
<i>SimplexID</i>	Typename of the SimplexID.

**8.1.2.22 neighbors()** [1/2]

```
template<class Complex, class SimplexID, class InsertIter>
void casc::neighbors (
    Complex & F,
    SimplexID nid,
    InsertIter iter)
```

## Parameters

	<i>F</i>	The simplicial complex.
in	<i>nid</i>	Simplex to get neighbors of.
in	<i>iter</i>	The iterator to push members into.

## Template Parameters

<i>Complex</i>	Type of the simplicial complex
<i>level</i>	The integral level of the node
<i>InsertIter</i>	Typename of the iterator.

## 8.1.2.23 neighbors() [2/2]

```
template<class Complex, std::size_t level, class InsertIter>
void casc::neighbors (
    Complex & F,
    typename Complex::template SimplexID< level > nid,
    InsertIter iter)
```

This function gets the set of neighbors which share a common face. We compute this by traversing to all faces of the simplex of interest. Then we get all cofaces of this set. Depending on the type of iterator passed, duplicate simplices will be included or excluded. Note that this is the traditional definition of neighbor. For example, faces which share an edge are neighbors.

## Parameters

	<i>F</i>	The simplicial complex
in	<i>nid</i>	Simplex to get neighbors of.
in	<i>iter</i>	The iterator to push members into.

## Template Parameters

<i>Complex</i>	Type of the simplicial complex
<i>level</i>	The integral level of the node
<i>InsertIter</i>	Typename of the iterator.

## 8.1.2.24 neighbors\_up() [1/2]

```
template<class Complex, class SimplexID, class InsertIter>
void casc::neighbors_up (
    Complex & F,
    SimplexID nid,
    InsertIter iter)
```

## Parameters

	<i>F</i>	The simplicial complex.
in	<i>nid</i>	Simplex to get neighbors of.
in	<i>iter</i>	The iterator to push members into.

## Template Parameters

<i>Complex</i>	Type of the simplicial complex
<i>level</i>	The integral level of the node
<i>InsertIter</i>	Typename of the iterator.

## 8.1.2.25 neighbors\_up() [2/2]

```
template<class Complex, std::size_t level, class InsertIter>
void casc::neighbors_up (
    Complex & F,
    typename Complex::template SimplexID< level > nid,
    InsertIter iter)
```

## Parameters

	<i>F</i>	The simplicial complex.
in	<i>nid</i>	Simplex to get neighbors of.
in	<i>iter</i>	The iterator to push members into.

## Template Parameters

<i>Complex</i>	Type of the simplicial complex
<i>level</i>	The integral level of the node
<i>InsertIter</i>	Typename of the iterator.

## 8.1.2.26 operator!=(())

```
template<typename Complex>
bool casc::operator!=(
    const SimplexSet< Complex > & lhs,
    const SimplexSet< Complex > & rhs)
```

## Parameters

in	<i>lhs</i>	The left hand side
in	<i>rhs</i>	The right hand side

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
----------------	--

## Returns

True if the sets are inequal, false otherwise.

## 8.1.2.27 operator==(())

```
template<typename Complex>
bool casc::operator==(
    const SimplexSet< Complex > & lhs,
    const SimplexSet< Complex > & rhs)
```

## Parameters

in	<i>lhs</i>	The left hand side
in	<i>rhs</i>	The right hand side

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a>
----------------	--

## Returns

True if the sets are equal, false otherwise.

## 8.1.2.28 perform\_insertion()

```
template<typename Complex>
void casc::perform_insertion (
    Complex & F,
    typename decimation_detail::SimplexDataSet< Complex >::type & S)
```

## Parameters

<i>F</i>	The <a href="#">simplicial_complex</a> to insert into.
<i>S</i>	<a href="#">SimplexSet</a> of simplices to insert.

## Template Parameters

<i>Complex</i>	Typename of complex
----------------	---------------------

## 8.1.2.29 perform\_removal()

```
template<typename Complex>
void casc::perform_removal (
    Complex & F,
    casc::SimplexSet< Complex > & S)
```

## Parameters

<i>F</i>	The <a href="#">simplicial_complex</a> to remove from.
<i>S</i>	<a href="#">SimplexSet</a> of simplices to remove.

## Template Parameters

<i>Complex</i>	Typename of complex
----------------	---------------------

### 8.1.2.30 run\_user\_callback()

```
template<typename Complex, template< typename > class Callback>
void casc::run_user_callback (
    Complex & F,
    casc::SimplexMap< Complex > & S,
    Callback< Complex > && clbk,
    typename decimation_detail::SimplexDataSet< Complex >::type & rv)
```



## Parameters

in	<i>F</i>	The <a href="#">simplicial_complex</a>
in	<i>S</i>	<a href="#">SimplexMap</a> of
in	<i>clbk</i>	User specified callback functor
out	<i>rv</i>	Multi-vector to place results.

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a>
<i>Callback</i>	Typename of the template template callback functor

## 8.1.2.31 set\_difference()

```
template<typename Complex>
static void casc::set_difference (
    const SimplexSet< Complex > & A,
    const SimplexSet< Complex > & B,
    SimplexSet< Complex > & dest) [static]
```

## Parameters

in	<i>A</i>	A <a href="#">SimplexSet</a>
in	<i>B</i>	Another <a href="#">SimplexSet</a>
out	<i>dest</i>	The destination <a href="#">SimplexSet</a> .

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
----------------	--

## 8.1.2.32 set\_intersection()

```
template<typename Complex>
static void casc::set_intersection (
    const SimplexSet< Complex > & A,
    const SimplexSet< Complex > & B,
    SimplexSet< Complex > & dest) [static]
```

## Parameters

in	<i>A</i>	A <a href="#">SimplexSet</a>
in	<i>B</i>	Another <a href="#">SimplexSet</a>
out	<i>dest</i>	The destination <a href="#">SimplexSet</a> .

## Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
----------------	--

### 8.1.2.33 set\_union()

```
template<typename Complex>
static void casc::set_union (
    const SimplexSet< Complex > & A,
    const SimplexSet< Complex > & B,
    SimplexSet< Complex > & dest) [static]
```

#### Parameters

in	<i>A</i>	A <a href="#">SimplexSet</a>
in	<i>B</i>	Another <a href="#">SimplexSet</a>
out	<i>dest</i>	The destination <a href="#">SimplexSet</a> .

#### Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
----------------	--

### 8.1.2.34 to\_string()

```
template<typename T, std::size_t k>
std::string casc::to_string (
    const std::array< T, k > & A)
```

#### Parameters

in	<i>A</i>	Array containing name of a simplex.
----	----------	-------------------------------------

#### Template Parameters

<i>T</i>	Typename KeyType.
<i>k</i>	Dimension of the simplex.

#### Returns

String representation of the object.

### 8.1.2.35 visit\_BFS\_down()

```
template<typename Visitor, typename SimplexID>
void casc::visit_BFS_down (
    Visitor && v,
    typename SimplexID::complex & F,
    SimplexID s)
```

#### Parameters

in	<i>v</i>	Visitor functor to apply.
	<i>F</i>	The <a href="#">simplicial_complex</a> to traverse.
in	<i>s</i>	The simplex to start at.

## Template Parameters

<i>Visitor</i>	Typename of the functor.
<i>SimplexID</i>	Typename of the simplex.

## 8.1.2.36 visit\_BFS\_up()

```
template<typename Visitor, typename SimplexID>
void casc::visit_BFS_up (
    Visitor && v,
    typename SimplexID::complex & F,
    SimplexID s)
```

## Parameters

in	<i>v</i>	Visitor functor to apply.
	<i>F</i>	The <a href="#">simplicial_complex</a> to traverse.
in	<i>s</i>	The simplex to start at.

## Template Parameters

<i>Visitor</i>	Typename of the functor.
<i>SimplexID</i>	Typename of the simplex.

## 8.1.2.37 writeDOT()

```
template<typename Complex>
void casc::writeDOT (
    const std::string & filename,
    Complex & F)
```

The resulting dot file can be rendered into an image using tools such as GraphViz.

```
dot -Tpng input.dot > output.png
```

## Parameters

in	<i>filename</i>	Filename to write out to.
in	<i>F</i>	Simplicial complex to generate the DOT of.

## Template Parameters

<i>Complex</i>	Typename of the simplicial complex.
----------------	-------------------------------------

## 8.2 index\_tracker Namespace Reference

Index tracker namespace.

## Namespaces

- namespace [index\\_tracker\\_detail](#)  
*B-tree internal data structures.*

## Data Structures

- class [index\\_tracker](#)  
*Tracker of available indices implemented as a B-tree of intervals.*

## Functions

- `template<typename T, std::size_t d>`  
`std::ostream & operator<< (std::ostream &out, const index\_tracker\_detail::BTreeNode< T, d > *head)`

## 8.3 [index\\_tracker::index\\_tracker\\_detail](#) Namespace Reference

B-tree internal data structures.

## Data Structures

- struct [BTreeNode](#)  
*An array based BTree.*
- struct [Interval](#)  
*[Interval](#) object represents a range.*

## Typedefs

- `template<typename Node>`  
`using Pointer = typename Node::Pointer`
- `template<typename Node>`  
`using Data = typename Node::Data`
- `template<typename Node>`  
`using Scalar = typename Node::Scalar`

## Functions

- template<typename T>  
bool **operator**< (const Interval< T > &x, const Interval< T > &y)
- template<typename T>  
bool **operator**> (const Interval< T > &x, const Interval< T > &y)
- template<typename T>  
bool **operator**< (T x, const Interval< T > &y)
- template<typename T>  
bool **operator**> (const Interval< T > &x, T y)
- template<typename T>  
bool **operator**< (const Interval< T > &x, T y)
- template<typename T>  
bool **operator**> (T x, const Interval< T > &y)
- template<typename T>  
bool **operator**== (const Interval< T > &x, const Interval< T > &y)
- template<typename T>  
std::ostream & **operator**<< (std::ostream &out, const Interval< T > &x)
- template<typename T>  
int **merge** (Interval< T > &A, T x)
- template<typename Node>  
void **rebalance** (Pointer< Node > head, std::size\_t i)
- template<typename Node>  
void **insert\_H** (Pointer< Node > head, const Data< Node > &data)
- template<typename Node>  
Pointer< Node > **insert** (Pointer< Node > head, Data< Node > data)
- template<typename Node>  
bool **get** (Pointer< Node > head, Data< Node > data)
- template<typename Node>  
void **get\_replacement** (Pointer< Node > head, Data< Node > &key)
- template<typename Node>  
void **remove\_H** (Pointer< Node > head, Data< Node > data)
- template<typename Node>  
Pointer< Node > **remove** (Pointer< Node > head, Data< Node > data)
- template<typename Node>  
void **fill\_left** (Pointer< Node > head, Data< Node > &x)
- template<typename Node>  
void **fill\_right** (Pointer< Node > head, Data< Node > &x)
- template<typename Node>  
void **insert\_scalar\_H** (Pointer< Node > head, Scalar< Node > data)
- template<typename Node>  
Pointer< Node > **insert\_scalar** (Pointer< Node > head, Scalar< Node > data)
- template<typename Node>  
void **insert\_left** (Pointer< Node > head, const Data< Node > &x)
- template<typename Node>  
bool **remove\_scalar\_H** (Pointer< Node > head, Scalar< Node > x)
- template<typename Node>  
bool **remove\_scalar** (Pointer< Node > &head, Scalar< Node > data)
- template<typename Node>  
Scalar< Node > **pop\_scalar** (Pointer< Node > &head)
- template<typename Node>  
void **destruct** (Pointer< Node > head)
- template<typename Node>  
Data< Node > **check\_order** (Pointer< Node > head, Data< Node > curr)

## 8.4 util Namespace Reference

Metatemplate programming utilities namespace.

### Data Structures

- struct [int\\_type\\_map](#)  
*Maps an integer sequence and typename,  $F$ , into outholder.*
- struct [range](#)  
*A range object to support range based for loops.*
- struct [remove\\_first\\_val](#)  
*General template for removing the first value from a type holder.*
- struct [remove\\_first\\_val](#)< [Integer](#), [InHolder](#)< [Integer](#),  $I$ ,  $Is...$  > >  
*Specialization for removing first integer from a sequence of compile time integers.*
- struct [reverse\\_sequence](#)  
*Reverse an Integer Sequence.*
- struct [type\\_get](#)  
*Helper to get the  $k$ th element from a [type\\_holder](#).*
- struct [type\\_get](#)< 0, [type\\_holder](#)<  $Ts...$  > >  
*Specialization for terminal case.*
- struct [type\\_get](#)<  $k$ , [type\\_holder](#)<  $Ts...$  > >  
*Specialization to recursively pop types to get the  $k$ th type.*
- struct [type\\_holder](#)  
*Queue based data structure to hold list of types.*
- struct [type\\_holder](#)<  $T$ ,  $Ts...$  >  
*Partial specialization to allow FIFO access of typenames.*
- struct [type\\_map](#)  
*Map the types in  $C$  into  $V<T>$ .*
- struct [type\\_swap](#)  
*Move a list of types from one container to another.*
- struct [type\\_swap](#)< [TUPLE](#), [HOLDER](#)<  $Ts...$  > >  
*Move a list of types from one container to another.*

### Functions

- `template<typename T>  
range< T > make\_range (T b, T e)`  
*Make a range object.*
- `template<typename T>  
range< T > make\_range (std::pair< T, T > p)`  
*Makes a range object.*
- `template<class Integer, typename IntegerSequence, typename Fn, typename ... Args>  
void int\_for\_each (Fn &&f, Args &&... args)`  
*Calls a function  $f$ . `apply< $k$ >()` for a sequence of integer  $k$ 's.*

### 8.4.1 Function Documentation

#### 8.4.1.1 int\_for\_each()

```
template<class Integer, typename IntegerSequence, typename Fn, typename ... Args>
void util::int_for_each (
    Fn && f,
    Args &&... args)
```

## Parameters

in	<i>args</i>	Arguments to f
in	<i>f</i>	Functor with <code>apply&lt;k&gt;()</code> method

## Template Parameters

<i>Integer</i>	Integer type
<i>IntegerSequence</i>	Sequence of integers to iterate
<i>Fn</i>	Typename of functor f
<i>Args</i>	Typenames of the arguments

8.4.1.2 `make_range()` [1/2]

```
template<typename T>
range< T > util::make_range (
    std::pair< T, T > p)
```

## Parameters

in	<i>p</i>	A pair containing begin and end iterators.
----	----------	--

## Template Parameters

<i>T</i>	Typename of the iterator.
----------	---------------------------

## Returns

Returns a range of the iterators.

8.4.1.3 `make_range()` [2/2]

```
template<typename T>
range< T > util::make_range (
    T b,
    T e)
```

## Parameters

in	<i>b</i>	Iterator to the beginning.
in	<i>e</i>	Iterator to the end.

## Template Parameters

<i>T</i>	Typename of the iterator.
----------	---------------------------

## Returns

Returns a range of the iterators.





## Chapter 9

# Data Structure Documentation

### 9.1 index\_tracker::index\_tracker\_detail::BTreeNode< \_T, \_d > Struct Template Reference

An array based BTree.

```
#include <index_tracker.h>
```

#### Public Types

- using **Scalar** = `_T`
- using **Data** = `Interval<Scalar>`
- using **Pointer** = `BTreeNode*`

#### Public Member Functions

- **BTreeNode** (const `Data` &t)
- template<typename Iter>  
**BTreeNode** (Iter begin, Iter end)

#### Data Fields

- `std::size_t k`
- `std::array< Data, N > data`
- `std::array< Pointer, N+1 > next`

#### Static Public Attributes

- static constexpr `std::size_t d` = `_d`
- static constexpr `std::size_t N` = `2*d+1`

#### 9.1.1 Detailed Description

```
template<typename _T, std::size_t _d>  
struct index_tracker::index_tracker_detail::BTreeNode< _T, _d >
```

## Template Parameters

$\leftrightarrow$	{ description }
$\overleftarrow{\leftrightarrow}$	
$T$	
$\leftrightarrow$	{ description }
$\overleftarrow{\leftrightarrow}$	
$d$	

The documentation for this struct was generated from the following file:

- include/casc/[index\\_tracker.h](#)

## 9.2 `casc::simplicial_complex< traits >::EdgeID< k >` Struct Template Reference

External reference to an edge or a connection within the complex.

```
#include <SimplicialComplex.h>
```

### Public Types

- using **complex** = [simplicial\\_complex](#)<traits>  
*Typename of the complex.*

### Public Member Functions

- **EdgeID** ()  
*Default constructor wraps a nullptr and dummy edge.*
- **EdgeID** (NodePtr< k > p, [KeyType](#) e)  
*Constructor to wrap an Edge.*
- **EdgeID** (const [EdgeID](#) &rhs)  
*Copy constructor.*
- **EdgeID** & **operator=** (const [EdgeID](#) &rhs)  
*Assignment operator.*
- auto const & **operator\*** () const  
*Dereferencing an [EdgeID](#) gets the data on the edge.*
- auto & **operator\*** ()  
*Dereferencing an [EdgeID](#) gets the data on the edge.*
- [KeyType](#) **key** () const  
*Get the key of the edge.*
- auto const & **data** () const  
*Return the data stored on the edge.*
- auto & **data** ()  
*Return the data stored on the edge.*
- [SimplexID](#)< k > **up** () const  
*Get the coboundary simplex.*
- [SimplexID](#)< k-1 > **down** () const  
*Get the simplex below.*

## Data Fields

- friend `simplicial_complex< traits >`  
*EdgeID is a friend of the complex.*

## Static Public Attributes

- static constexpr `std::size_t level` = `k`  
*The dimension of the simplex which the edge points to.*

## Friends

- bool `operator==` (`EdgeID` lhs, `EdgeID` rhs)  
*Equality of wrapped pointers and edges.*
- bool `operator!=` (`EdgeID` lhs, `EdgeID` rhs)  
*Compare wrapped pointers and edges.*
- bool `operator<=` (`EdgeID` lhs, `EdgeID` rhs)  
*Compare wrapped pointers and edges.*
- bool `operator>=` (`EdgeID` lhs, `EdgeID` rhs)  
*Compare wrapped pointers and edges.*
- bool `operator<` (`EdgeID` lhs, `EdgeID` rhs)  
*Less than defines an ordering of key types on the edges.*
- bool `operator>` (`EdgeID` lhs, `EdgeID` rhs)  
*Greater than comparison.*

## 9.2.1 Detailed Description

```
template<typename traits>
template<std::size_t k>
struct casc::simplicial_complex< traits >::EdgeID< k >
```

### Template Parameters

<code>k</code>	The edge connects a simplex of size k-1 to a simplex of size k.
----------------	---

## 9.2.2 Constructor & Destructor Documentation

### 9.2.2.1 `EdgeID()` [1/2]

```
template<typename traits>
template<std::size_t k>
casc::simplicial_complex< traits >::EdgeID< k >::EdgeID (
    NodePtr< k > p,
    KeyType e) [inline]
```

### Parameters

in	<code>p</code>	Pointer to the next Node.
in	<code>e</code>	Key of the edge

### 9.2.2.2 EdgelID() [2/2]

```
template<typename traits>
template<std::size_t k>
casc::simplicial_complex< traits >::EdgeID< k >::EdgeID (
    const EdgeID< k > & rhs) [inline]
```

#### Parameters

in	rhs	The right hand side
----	-----	---------------------

## 9.2.3 Member Function Documentation

### 9.2.3.1 down()

```
template<typename traits>
template<std::size_t k>
SimplexID< k-1 > casc::simplicial_complex< traits >::EdgeID< k >::down () const [inline]
```

#### Returns

SimplexID of the simplex below the edge.

### 9.2.3.2 up()

```
template<typename traits>
template<std::size_t k>
SimplexID< k > casc::simplicial_complex< traits >::EdgeID< k >::up () const [inline]
```

#### Returns

SimplexID of the simplex above the edge.

The documentation for this struct was generated from the following file:

- include/casc/SimplicialComplex.h

## 9.3 index\_tracker::index\_tracker< \_T, \_d > Class Template Reference

Tracker of available indices implemented as a B-tree of intervals.

```
#include <index_tracker.h>
```

#### Public Types

- using **Node** = [index\\_tracker\\_detail::BTreeNode](#)<\_T, \_d>  
*Typedef of BTree Node.*
- using **T** = \_T

## Public Member Functions

- `index_tracker()`  
*Number of bins.*
- `void insert (T x)`
- `index_tracker_detail::Scalar< Node > pop ()`
- `void remove (index_tracker_detail::Scalar< Node > x)`
- `bool empty () const`

## Static Public Attributes

- `static constexpr std::size_t d = _d`  
*Typename of the type to store.*

## Friends

- `std::ostream & operator<< (std::ostream &out, const index_tracker &x)`

### 9.3.1 Detailed Description

```
template<typename _T, std::size_t _d = 16>
class index_tracker::index_tracker<_T, _d>
```

#### Template Parameters

$\leftarrow$ $\_T$	Typename of the indices
$\leftarrow$ $\_d$	Max number of interval bins = 2*value+1

### 9.3.2 Constructor & Destructor Documentation

#### 9.3.2.1 `index_tracker()`

```
template<typename _T, std::size_t _d = 16>
index_tracker::index_tracker<_T, _d>::index_tracker () [inline]
```

Initialize with interval [0~max)

The documentation for this class was generated from the following file:

- `include/casc/index_tracker.h`

## 9.4 util::int\_type\_map< IntegerType, OutHolder, IntegerSequence, F > Struct Template Reference

Maps an integer sequence and typename, F, into outholder.

```
#include <util.h>
```

### Public Types

- using **type** = typename detail::int\_type\_map\_helper<IntegerType, OutHolder, IntegerSequence, F>::type  
*Tuple of Out<F<0>, F<1>, F<2>, ...>.*

### 9.4.1 Detailed Description

**template<class IntegerType, template< class ... > class OutHolder, class IntegerSequence, template< IntegerType > class F>**

**struct util::int\_type\_map< IntegerType, OutHolder, IntegerSequence, F >**

Given an Integer Sequence  $I<0, 1, 2, 3, \dots>$  and template template type  $F<I>$ , this function produces  $Out<F<0>, F<1>, F<2>, \dots>$ .

#### Template Parameters

<i>IntegerType</i>	Typename of an integer type
<i>OutHolder</i>	Typename of a holder for types
<i>IntegerSequence</i>	Integral sequence of types
<i>F</i>	Typename of class to be broadcast with integer

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.5 index\_tracker::index\_tracker\_detail::Interval< T > Struct Template Reference

[Interval](#) object represents a range.

```
#include <index_tracker.h>
```

## Public Member Functions

- **Interval** ()  
*Default constructor.*
- **Interval** (T a)  
*Construct an interval from a to a+1.*
- **Interval** (T a, T b)  
*Construct an interval from a to b.*
- **Interval** (const [Interval](#)< T > &rhs)  
*Copy constructor.*
- [Interval](#) & **operator=** (const [Interval](#) &rhs)  
*Assignment operator overload.*
- bool **has** (T x)  
*Is x in the bounds of the interval.*
- T **lower** () const  
*Get the lower inclusive bound of the interval.*
- T **upper** () const  
*Get the upper exclusive bound of the interval.*
- T & **lower** ()  
*Get the lower inclusive bound of the interval.*
- T & **upper** ()  
*Get the upper exclusive bound of the interval.*
- std::size\_t **size** ()  
*Get the size of the interval.*

## 9.5.1 Detailed Description

```
template<typename T>
struct index_tracker::index_tracker_detail::Interval< T >
```

### Template Parameters

<code>T</code>	Typename of the interval data
----------------	-------------------------------

## 9.5.2 Member Function Documentation

### 9.5.2.1 `operator=()`

```
template<typename T>
Interval & index\_tracker::index\_tracker\_detail::Interval< T >::operator= (
    const Interval< T > & rhs) [inline]
```

### Parameters

<code>in</code>	<code>rhs</code>	The right hand side
-----------------	------------------	---------------------

### Returns

Reference to this

The documentation for this struct was generated from the following file:

- `include/casc/index_tracker.h`

## 9.6 `casc::Orientable` Struct Reference

Class representing the orientation.

```
#include <Orientable.h>
```

### Data Fields

- `int orientation`  
*Integer representing +/- 1 orientation.*

The documentation for this struct was generated from the following file:

- `include/casc/Orientable.h`

## 9.7 `util::range< T >` Struct Template Reference

A range object to support range based for loops.

```
#include <util.h>
```

### Public Member Functions

- `template<class C>`  
`range` (C &&c)  
*Construct a range for a container class.*
- `range` (T b, T e)  
*Construct a range from an iterator.*
- `T begin` ()  
*Get the beginning iterator.*
- `T end` ()  
*Get the end iterator.*

### 9.7.1 Detailed Description

```
template<typename T>
struct util::range< T >
```

This is a basic data structure which implements a `begin()` and `end()` functions for range based for looping added in C++11. See also `range-for`.

#### Template Parameters

<code>T</code>	Typename of the iterator
----------------	--------------------------

### 9.7.2 Constructor & Destructor Documentation

#### 9.7.2.1 `range()` [1/2]

```
template<typename T>
template<class C>
util::range< T >::range (
    C && c) [inline]
```



## Parameters

in	<i>c</i>	Container class which implements <a href="#">begin()</a> and <a href="#">end()</a> .
----	----------	--

## Template Parameters

<i>C</i>	Typename of the container.
----------	----------------------------

## 9.7.2.2 range() [2/2]

```
template<typename T>
util::range< T >::range (
    T b,
    T e) [inline]
```

## Parameters

in	<i>b</i>	Beginning iterator
in	<i>e</i>	End iterator.

## 9.7.3 Member Function Documentation

## 9.7.3.1 begin()

```
template<typename T>
T util::range< T >::begin () [inline]
```

## Returns

Returns an iterator to the beginning.

## 9.7.3.2 end()

```
template<typename T>
T util::range< T >::end () [inline]
```

## Returns

Returns an iterator to the end.

The documentation for this struct was generated from the following file:

- [include/casc/util.h](#)

## 9.8 util::remove\_first\_val< Integer, IntegerSequence > Struct Template Reference

General template for removing the first value from a type holder.

```
#include <util.h>
```

### 9.8.1 Detailed Description

```
template<class Integer, class IntegerSequence>
struct util::remove_first_val< Integer, IntegerSequence >
```

Template Parameters

<i>Integer</i>	Typename of integer.
<i>IntegerSequence</i>	Sequence of compile time integers.

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.9 util::remove\_first\_val< Integer, InHolder< Integer, I, Is... > > Struct Template Reference

Specialization for removing first integer from a sequence of compile time integers.

```
#include <util.h>
```

Public Types

- using **type** = InHolder<Integer, Is...>  
*Type holder with first value removed.*

### 9.9.1 Detailed Description

```
template<class Integer, template< class, Integer... > class InHolder, Integer I, Integer... Is>
struct util::remove_first_val< Integer, InHolder< Integer, I, Is... > >
```

Template Parameters

<i>Integer</i>	Typename of integer type.
<i>InHolder</i>	Type holder of integer sequence.
<i>I</i>	The first integer
<i>Is</i>	Remaining integers

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.10 util::reverse\_sequence< Integer, IntegerSequence > Struct Template Reference

Reverse an Integer Sequence.

```
#include <util.h>
```

### Public Types

- using **type** = typename detail::reverse\_sequence\_helper<Integer, IntegerSequence>::type  
*Reversed sequence of types.*

### 9.10.1 Detailed Description

```
template<class Integer, class IntegerSequence>
struct util::reverse_sequence< Integer, IntegerSequence >
```

#### Template Parameters

<i>Integer</i>	Typename of an integer class.
<i>IntegerSequence</i>	Sequence of compile-time integers.

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.11 casc::simplicial\_complex< traits >::SimplexID< k > Struct Template Reference

A handle for a simplex object in the complex.

```
#include <SimplicialComplex.h>
```

### Public Types

- using **complex** = [simplicial\\_complex](#)<traits>  
*Typename of the complex.*

## Public Member Functions

- **SimplexID** ()  
*Default constructor wraps a nullptr.*
- **SimplexID** (NodePtr< k > p)  
*Constructor to wrap a NodePtr<k>.*
- **SimplexID** (const SimplexID &rhs)  
*Copy constructor.*
- **SimplexID** & **operator=** (const SimplexID &rhs)  
*Assignment operator.*
- **operator std::uintptr\_t** () const  
*Support casting to uintptr\_t for hashing.*
- **complex::NodeData**< k > const & **operator\*** () const  
*Dereferencing a SimplexID returns the data stored.*
- **complex::NodeData**< k > & **operator\*** ()  
*Dereferencing a SimplexID returns the data stored.*
- **complex::NodeData**< k > const & **data** () const  
*Get a handle to the stored data.*
- **complex::NodeData**< k > & **data** ()  
*Get a handle to the stored data.*
- **std::array**< KeyType, k > **indices** () const  
*Gets the name of a simplex as an std::Array.*
- **template**<class Inserter>  
void **cover\_insert** (Inserter pos) const  
*Insert the coboundary keys of a simple into an inserter.*
- **std::vector**< KeyType > **cover** () const  
*Get the coboundary keys of a simplex.*
- **template**<std::size\_t j>  
**SimplexID**< k+j > **get\_simplex\_up** (const KeyType(&s)[j]) const  
*Get a coboundary simplex.*
- **template**<std::size\_t j>  
**SimplexID**< k+j > **get\_simplex\_up** (const std::array< KeyType, j > &arr) const  
*Get a coboundary simplex.*
- **SimplexID**< k+1 > **get\_simplex\_up** (const KeyType s) const  
*Convenience version of get\_simplex\_up when the name 's' consists of a single character.*
- **template**<std::size\_t j>  
**SimplexID**< k-j > **get\_simplex\_down** (const KeyType(&s)[j]) const  
*Gets the simplex down.*
- **template**<std::size\_t j>  
**SimplexID**< k-j > **get\_simplex\_down** (const std::array< KeyType, j > &arr) const  
*Gets the simplex down.*
- **SimplexID**< k-1 > **get\_simplex\_down** (const KeyType s) const  
*Gets the simplex down.*

## Data Fields

- friend **simplicial\_complex**< traits >  
*SimplexID is a friend of the complex.*

### Static Public Attributes

- static constexpr `std::size_t level` = `k`  
*The dimension of the simplex.*

### Friends

- bool `operator==` (`SimplexID` lhs, `SimplexID` rhs)  
*Equality of wrapped pointers.*
- bool `operator!=` (`SimplexID` lhs, `SimplexID` rhs)  
*Inequality of wrapped pointers.*
- bool `operator<=` (`SimplexID` lhs, `SimplexID` rhs)  
*Compare wrapped pointers.*
- bool `operator>=` (`SimplexID` lhs, `SimplexID` rhs)  
*Compare wrapped pointers.*
- bool `operator<` (`SimplexID` lhs, `SimplexID` rhs)  
*Compare wrapped pointers.*
- bool `operator>` (`SimplexID` lhs, `SimplexID` rhs)  
*Compare wrapped pointers.*
- `std::ostream & operator<<` (`std::ostream &out`, const `SimplexID &nid`)  
*Print the simplex as its name.*

## 9.11.1 Detailed Description

`template<typename traits>`

`template<std::size_t k>`

`struct casc::simplicial_complex< traits >::SimplexID< k >`

`SimplexID` wraps a `Node*` for external handling. This way the end users are never exposed to a raw pointer. For all general purposes algorithms should use and pass `SimplexIDs` over raw pointers.

#### Template Parameters

<code>k</code>	The Simplex dimension.
----------------	------------------------

## 9.11.2 Constructor & Destructor Documentation

### 9.11.2.1 `SimplexID()` [1/2]

```
template<typename traits>
template<std::size_t k>
casc::simplicial_complex< traits >::SimplexID< k >::SimplexID (
    NodePtr< k > p) [inline]
```

#### Parameters

<code>in</code>	<code>p</code>	The NodePtr to wrap
-----------------	----------------	---------------------

### 9.11.2.2 `SimplexID()` [2/2]

```
template<typename traits>
template<std::size_t k>
casc::simplicial_complex< traits >::SimplexID< k >::SimplexID (
    const SimplexID< k > & rhs) [inline]
```

## Parameters

in	<i>rhs</i>	Another <a href="#">SimplexID</a> to copy.
----	------------	--

## 9.11.3 Member Function Documentation

### 9.11.3.1 `cover()`

```
template<typename traits>
template<std::size_t k>
std::vector< KeyType > casc::simplicial\_complex< traits >::SimplexID< k >::cover () const
[inline]
```

## Returns

A vector of coboundary indices.

### 9.11.3.2 `cover_insert()`

```
template<typename traits>
template<std::size_t k>
template<class Inserter>
void casc::simplicial\_complex< traits >::SimplexID< k >::cover_insert (
    Inserter pos) const [inline]
```

## Parameters

in	<i>pos</i>	Iterator inserter
----	------------	-------------------

## Template Parameters

<i>Inserter</i>	Typename of the inserter.
-----------------	---------------------------

### 9.11.3.3 `get_simplex_up()` [1/3]

```
template<typename traits>
template<std::size_t k>
SimplexID< k+1 > casc::simplicial\_complex< traits >::SimplexID< k >::get_simplex_up (
    const KeyType s) const [inline]
```

## Parameters

in	<i>id</i>	The identifier of a simplex.
in	<i>s</i>	The relative single character name of the desired simplex.

## Template Parameters

<i>i</i>	The size of simplex 'id'.
----------	---------------------------

## Returns

`SimplexID` of node corresponding to  $id \cup s$ .

9.11.3.4 `get_simplex_up()` [2/3]

```
template<typename traits>
template<std::size_t k>
template<std::size_t j>
SimplexID< k+j > casc::simplicial_complex< traits >::SimplexID< k >::get_simplex_up (
    const KeyType(&) s[j]) const [inline]
```

## Parameters

in	<i>s</i>	Array of keys to follow
----	----------	-------------------------

## Template Parameters

<i>j</i>	Number of keys
----------	----------------

## Returns

The simplex up

9.11.3.5 `get_simplex_up()` [3/3]

```
template<typename traits>
template<std::size_t k>
template<std::size_t j>
SimplexID< k+j > casc::simplicial_complex< traits >::SimplexID< k >::get_simplex_up (
    const std::array< KeyType, j > & arr) const [inline]
```

## Parameters

in	<i>arr</i>	Array of keys to follow
----	------------	-------------------------

## Template Parameters

<i>j</i>	Number of keys
----------	----------------

## Returns

The simplex up

9.11.3.6 `indices()`

```
template<typename traits>
template<std::size_t k>
std::array< KeyType, k > casc::simplicial_complex< traits >::SimplexID< k >::indices ()
const [inline]
```

**Parameters**

in	<i>id</i>	<a href="#">SimplexID</a> of the simplex of interest.
----	-----------	---

**Returns**

Array containing the name of 'id'.

**9.11.4 Friends And Related Symbol Documentation****9.11.4.1 operator<<**

```
template<typename traits>
template<std::size_t k>
std::ostream & operator<< (
    std::ostream & out,
    const SimplexID< k > & nid) [friend]
```

**Parameters**

	<i>out</i>	Handle to the stream
in	<i>nid</i>	<a href="#">SimplexID</a> of interest

**Returns**

Handle to the stream

**Example**

```
(.c)
    mesh.insert<3>({0,1,2});
    std::cout << s << std::endl;
    s{0,1,2}"
```

The documentation for this struct was generated from the following file:

- include/casc/[SimplicialComplex.h](#)

**9.12 casc::SimplexMap< Complex > Struct Template Reference**

A multimap to represent a map of simplex indices to a set of simplices.

```
#include <SimplexMap.h>
```



## Public Types

- `template<std::size_t j>`  
using **SimplexID** = `typename Complex::template SimplexID<j>`  
*Alias for `SimplexID`.*
- using **LevelIndex** = `typename Complex::LevelIndex`  
*Index sequence of types from the `simplicial_complex`.*
- using **cLevelIndex**  
*Index sequence starting at 1.*
- using **RevIndex**  
*Reversed Index sequence.*
- using **cRevIndex**  
*Reversed index sequence stops at 1.*
- using **type\_this** = `SimplexMap<Complex>`  
*Typename of this object.*

## Public Member Functions

- **SimplexMap** ()  
*Default constructor.*
- `template<std::size_t k>`  
`auto & get ()`  
*Get the map for a particular simplex dimension.*
- `template<std::size_t k>`  
`auto & get () const`

## Friends

- `std::ostream & operator<< (std::ostream &output, const SimplexMap< Complex > &S)`  
*Print the `SimplexMap`.*

### 9.12.1 Detailed Description

```
template<typename Complex>
struct casc::SimplexMap< Complex >
```

#### Template Parameters

<i>Complex</i>	Typename of the <code>simplicial_complex</code> .
----------------	---

### 9.12.2 Member Typedef Documentation

#### 9.12.2.1 `cLevelIndex`

```
template<typename Complex>
using casc::SimplexMap< Complex >::cLevelIndex
```

#### Initial value:

```
typename util::remove_first_val<std::size_t,
                                LevelIndex>::type
```

### 9.12.2.2 cRevIndex

```
template<typename Complex>
using casc::SimplexMap< Complex >::cRevIndex
```

#### Initial value:

```
typename util::reverse_sequence<std::size_t,
                                cLevelIndex>::type
```

### 9.12.2.3 RevIndex

```
template<typename Complex>
using casc::SimplexMap< Complex >::RevIndex
```

#### Initial value:

```
typename util::reverse_sequence<std::size_t,
                                LevelIndex>::type
```

## 9.12.3 Member Function Documentation

### 9.12.3.1 get() [1/2]

```
template<typename Complex>
template<std::size_t k>
auto & casc::SimplexMap< Complex >::get () [inline]
```

#### Template Parameters

<i>k</i>	Simplex dimension to retrieve.
----------	--------------------------------

#### Returns

A map of [SimplexID<k>](#) to [SimplexSet](#).

### 9.12.3.2 get() [2/2]

```
template<typename Complex>
template<std::size_t k>
auto & casc::SimplexMap< Complex >::get () const [inline]
```

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

## 9.12.4 Friends And Related Symbol Documentation

### 9.12.4.1 operator<<

```
template<typename Complex>
std::ostream & operator<< (
    std::ostream & output,
    const SimplexMap< Complex > & S) [friend]
```

## Parameters

	<i>output</i>	Handle to the stream to print to.
<i>in</i>	<i>S</i>	<a href="#">SimplexMap</a> to print.

## Returns

Handle to the stream.

The documentation for this struct was generated from the following file:

- `include/casc/SimplexMap.h`

## 9.13 `casc::SimplexSet< Complex >` Struct Template Reference

A multiset to store simplices in a [simplicial\\_complex](#).

```
#include <SimplexSet.h>
```

## Public Types

- `template<std::size_t j>`  
using **SimplexID** = typename `Complex::template SimplexID<j>`  
*Alias for [SimplexID](#).*
- using **LevelIndex** = typename `Complex::LevelIndex`  
*Index sequence of types from the [simplicial\\_complex](#).*
- using **cLevelIndex**  
*Index sequence starting at 1.*
- using **RevIndex**  
*Reversed index sequence.*
- using **cRevIndex**  
*Reversed index sequence stops at 1.*
- using **type\_this** = `SimplexSet<Complex>`  
*Typename of this.*
- using **SimplexIDLevel**  
*Tuple of SimplexIDs wrt an integral level.*

## Public Member Functions

- **SimplexSet** ()  
*Default constructor.*
- **~SimplexSet** ()  
*Default destructor.*
- template<std::size\_t k>  
auto **empty** () const noexcept  
*Checks if a level has no elements.*
- template<std::size\_t k>  
auto **size** () const noexcept  
*Return the number of elements in a level.*
- void **clear** ()  
*Clear the contents.*
- template<std::size\_t k>  
void **insert** (SimplexID< k > s)  
*Insert a simplex into the set.*
- void **insert** (const SimplexSet< Complex > &s)  
*Insert a SimplexSet into this.*
- template<std::size\_t k>  
void **erase** (SimplexID< k > s)  
*Remove a simplex from the set.*
- void **erase** (const SimplexSet< Complex > &s)  
*Remove a set of simplices.*
- template<std::size\_t k>  
auto **find** (const SimplexID< k > s)  
*Get the simplex of interest.*
- template<std::size\_t k>  
auto **find** (const SimplexID< k > s) const  
*Get the simplex of interest.*
- template<std::size\_t k>  
auto **end** ()  
*Get the past-the-end iterator.*
- template<std::size\_t k>  
auto **cend** () const  
*Get the past-the-end iterator.*
- template<std::size\_t k>  
auto **begin** ()  
*Get an iterator to the first element of the container.*
- template<std::size\_t k>  
auto **cbegin** () const  
*Get an iterator to the first element of the container.*
- template<std::size\_t k>  
auto & **get** ()  
*Get the NodeSet for a particular simplex dimension.*
- template<std::size\_t k>  
auto & **get** () const  
*Get the NodeSet for a particular simplex dimension.*

## Data Fields

- **util::type\_map**< SimplexIDLevel, NodeSet >::type **tupleSet**  
*Tuple of NodeSets per level.*

## Friends

- `std::ostream & operator<< (std::ostream &output, const SimplexSet< Complex > &S)`  
Print the [SimplexSet](#).

### 9.13.1 Detailed Description

```
template<typename Complex>
struct casc::SimplexSet< Complex >
```

This is really a tuple of sets where each set corresponds to a simplex dimension. Many convenience functions are wrapped so this behaves much like a `std::set`.

#### Template Parameters

<i>Complex</i>	Typename of the <a href="#">simplicial_complex</a> .
----------------	--

### 9.13.2 Member Typedef Documentation

#### 9.13.2.1 `cLevelIndex`

```
template<typename Complex>
using casc::SimplexSet< Complex >::cLevelIndex
```

##### Initial value:

```
typename util::remove_first_val<std::size_t,
                                LevelIndex>::type
```

#### 9.13.2.2 `cRevIndex`

```
template<typename Complex>
using casc::SimplexSet< Complex >::cRevIndex
```

##### Initial value:

```
typename util::reverse_sequence<std::size_t,
                                cLevelIndex>::type
```

#### 9.13.2.3 `RevIndex`

```
template<typename Complex>
using casc::SimplexSet< Complex >::RevIndex
```

##### Initial value:

```
typename util::reverse_sequence<std::size_t,
                                LevelIndex>::type
```

#### 9.13.2.4 SimplexIDLevel

```
template<typename Complex>
using casc::SimplexSet< Complex >::SimplexIDLevel
```

##### Initial value:

```
typename util::int_type_map<std::size_t,
                                std::tuple, LevelIndex, SimplexID>::type
```

### 9.13.3 Member Function Documentation

#### 9.13.3.1 begin()

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::begin () [inline]
```

##### Template Parameters

<code>k</code>	The simplex dimension to get iterator of.
----------------	---

##### Returns

Returns an iterator to the first element.

#### 9.13.3.2 cbegin()

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::cbegin () const [inline]
```

##### Template Parameters

<code>k</code>	The simplex dimension to get iterator of.
----------------	---

##### Returns

Returns an iterator to the first element.

#### 9.13.3.3 cend()

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::cend () const [inline]
```

## Template Parameters

<code>k</code>	The simplex dimension to get iterator of.
----------------	---

## Returns

Returns an iterator to the element following the last element of the set for the specified simplex dimension.

9.13.3.4 `empty()`

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::empty () const [inline], [noexcept]
```

## Template Parameters

<code>k</code>	Level to check.
----------------	-----------------

## Returns

True if the container is empty, false otherwise.

9.13.3.5 `end()`

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::end () [inline]
```

## Template Parameters

<code>k</code>	The simplex dimension to get iterator of.
----------------	---

## Returns

Returns an iterator to the element following the last element of the set for the specified simplex dimension.

9.13.3.6 `erase()` [1/2]

```
template<typename Complex>
void casc::SimplexSet< Complex >::erase (
    const SimplexSet< Complex > & s) [inline]
```

## Parameters

<code>in</code>	<code>s</code>	<code>SimplexSet</code> to remove.
-----------------	----------------	------------------------------------

9.13.3.7 `erase()` [2/2]

```
template<typename Complex>
template<std::size_t k>
void casc::SimplexSet< Complex >::erase (
    SimplexID< k > s) [inline]
```

**Parameters**

in	s	Simplex to remove.
----	---	--------------------

**Template Parameters**

k	Simplex dimension of 's'.
---	---------------------------

**9.13.3.8 find() [1/2]**

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::find (
    const SimplexID< k > s) [inline]
```

**Parameters**

in	s	The simplex to search for.
----	---	----------------------------

**Template Parameters**

k	Simplex dimension of 's'.
---	---------------------------

**Returns**

Iterator to an element with key equivalent to s. If no such element is found, past-the-end iterator (see [end\(\)](#)) is returned.

**9.13.3.9 find() [2/2]**

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::find (
    const SimplexID< k > s) const [inline]
```

**Parameters**

in	s	The simplex to search for.
----	---	----------------------------

**Template Parameters**

k	Simplex dimension of 's'.
---	---------------------------

**Returns**

Iterator to an element with key equivalent to s. If no such element is found, past-the-end iterator (see [end\(\)](#)) is returned.

**9.13.3.10 get() [1/2]**

```
template<typename Complex>
template<std::size_t k>
auto & casc::SimplexSet< Complex >::get () [inline]
```



## Template Parameters

<i>k</i>	Simplex dimension to get.
----------	---------------------------

## Returns

Returns the [NodeSet](#) corresponding to the requested dimension.

9.13.3.11 `get()` [2/2]

```
template<typename Complex>
template<std::size_t k>
auto & casc::SimplexSet< Complex >::get () const [inline]
```

## Template Parameters

<i>k</i>	Simplex dimension to get.
----------	---------------------------

## Returns

Returns the [NodeSet](#) corresponding to the requested dimension.

9.13.3.12 `insert()` [1/2]

```
template<typename Complex>
void casc::SimplexSet< Complex >::insert (
    const SimplexSet< Complex > & s) [inline]
```

## Parameters

in	<i>s</i>	The <a href="#">SimplexSet</a> to insert.
----	----------	---

9.13.3.13 `insert()` [2/2]

```
template<typename Complex>
template<std::size_t k>
void casc::SimplexSet< Complex >::insert (
    SimplexID< k > s) [inline]
```

## Parameters

in	<i>s</i>	Simplex to insert.
----	----------	--------------------

## Template Parameters

<i>k</i>	Simplex dimension of 's'.
----------	---------------------------

9.13.3.14 `size()`

```
template<typename Complex>
template<std::size_t k>
auto casc::SimplexSet< Complex >::size () const [inline], [noexcept]
```

### Template Parameters

<i>k</i>	Simplex dimension to query
----------	----------------------------

### Returns

Returns the number of simplices of dimension *k* are in the set.

## 9.13.4 Friends And Related Symbol Documentation

### 9.13.4.1 operator<<

```
template<typename Complex>
std::ostream & operator<< (
    std::ostream & output,
    const SimplexSet< Complex > & S) [friend]
```

See also `casc::simplicial_complex::SimplexID::operator<<`.

### Parameters

	<i>output</i>	Handle to the stream to print to.
<i>in</i>	<i>S</i>	<a href="#">SimplexSet</a> to print.

### Returns

Handle to the stream.

The documentation for this struct was generated from the following file:

- `include/casc/SimplexSet.h`

## 9.14 `casc::simplicial_complex< traits >` Class Template Reference

The CASC data structure for representing simplicial complexes of arbitrary dimensionality with coloring.

```
#include <SimplicialComplex.h>
```

### Data Structures

- struct [EdgeID](#)  
*External reference to an edge or a connection within the complex.*
- struct [SimplexID](#)  
*A handle for a simplex object in the complex.*

## Public Types

- using **KeyType** = typename traits::KeyType  
*Typename of simplex keys.*
- using **NodeDataTypes** = typename traits::NodeTypes  
*Typenames of the data stored on simplices.*
- using **EdgeDataTypes** = typename traits::EdgeTypes  
*Typenames of the data stored on edges.*
- using **type\_this** = simplicial\_complex<traits>  
*Type of this.*
- using **LevelIndex** = typename std::make\_index\_sequence<numLevels>  
*Index of all simplex dimensions in the complex.*
- template<std::size\_t k>  
using **NodeData** = typename util::type\_get<k, NodeDataTypes>::type
- template<std::size\_t k>  
using **EdgeData** = typename util::type\_get<k, EdgeDataTypes>::type

## Public Member Functions

- **simplicial\_complex** ()  
*Default constructor.*
- **~simplicial\_complex** ()  
*Destruct the simplicial complex.*
- template<std::size\_t n>  
**SimplexID**< n > **insert** (const KeyType(&s)[n])  
*Insert a simplex and all sub-simplices into the complex.*
- template<std::size\_t n>  
**SimplexID**< n > **insert** (const KeyType(&s)[n], const NodeData< n > &data)  
*Insert a simplex and all sub-simplices into the complex along with data.*
- template<std::size\_t n>  
**SimplexID**< n > **insert** (const std::array< KeyType, n > &s)  
*Insert a simplex named and all sub-simplices into the complex.*
- template<std::size\_t n>  
**SimplexID**< n > **insert** (const std::array< KeyType, n > &s, const NodeData< n > &data)  
*Insert a simplex and all sub-simplices into the complex along with data.*
- **KeyType add\_vertex** ()  
*Add a new vertex to the complex.*
- **KeyType add\_vertex** (const NodeData< 1 > &data)  
*Add a new vertex to the complex with data.*
- template<std::size\_t n, typename Lambda>  
void **get\_name** (SimplexID< n > id, Lambda fn) const  
*Apply a lambda function the name of a simplex.*
- template<std::size\_t n>  
std::array< KeyType, n > **get\_name** (SimplexID< n > id) const  
*Gets the name of a simplex as an std::Array.*
- std::array< KeyType, 0 > **get\_name** (SimplexID< 0 >) const  
*Gets the name of a simplex.*
- template<std::size\_t n>  
**SimplexID**< n > **get\_simplex\_up** (const KeyType(&s)[n]) const  
*Gets the simplex with name 's'.*
- template<std::size\_t n>  
**SimplexID**< n > **get\_simplex\_up** (const std::array< KeyType, n > &arr) const

- `template<std::size_t i, std::size_t j>`  
`SimplexID< i+j > get_simplex_up (const SimplexID< i > id, const KeyType(&s)[j]) const`  
*Get the simplex identifier which has the name 's' relative to the simplex 'id'.*
- `template<std::size_t i, std::size_t j>`  
`SimplexID< i+j > get_simplex_up (const SimplexID< i > id, const std::array< KeyType, j > &arr) const`
- `template<std::size_t i>`  
`SimplexID< i+1 > get_simplex_up (const SimplexID< i > id, const KeyType s) const`  
*Convenience version of get\_simplex\_up when the name 's' consists of a single character.*
- `SimplexID< 0 > get_simplex_up () const`  
*Get the root simplex.*
- `template<std::size_t i, std::size_t j>`  
`SimplexID< i-j > get_simplex_down (const SimplexID< i > id, const KeyType(&s)[j]) const`  
*Get the sub-simplex of the simplex 'id' which does not have 's' in the name.*
- `template<std::size_t i, std::size_t j>`  
`SimplexID< i-j > get_simplex_down (const SimplexID< i > id, const std::array< KeyType, j > &arr) const`
- `template<std::size_t i>`  
`SimplexID< i-1 > get_simplex_down (const SimplexID< i > id, const KeyType s) const`  
*Convenience version of get\_simplex\_down when the name 's' consists of a single character.*
- `SimplexID< 0 > get_simplex_down () const`  
*Get the root simplex.*
- `template<std::size_t k, class Inserter>`  
`void get_cover_insert (const SimplexID< k > id, Inserter pos) const`  
*Insert the coboundary keys of a simple into an inserter.*
- `template<std::size_t k, class Lambda>`  
`void get_cover (const SimplexID< k > id, Lambda fn) const`  
*Apply a lambda function to the coboundary keys.*
- `template<std::size_t k>`  
`std::vector< KeyType > get_cover (const SimplexID< k > id) const`  
*Get the coboundary keys of a simplex.*
- `template<std::size_t k>`  
`std::set< SimplexID< k+1 > > up (const std::set< SimplexID< k > > &&simplices) const`  
*Get the coboundary of a set of simplices.*
- `template<std::size_t k>`  
`std::set< SimplexID< k+1 > > up (const std::set< SimplexID< k > > &simplices) const`  
*Get the coboundary of a set of simplices.*
- `template<std::size_t k>`  
`std::set< SimplexID< k+1 > > up (const SimplexID< k > nid) const`  
*Get the coboundary of a simplex.*
- `template<std::size_t k, class InsertIter>`  
`void up (const std::set< SimplexID< k > > &&simplices, InsertIter iter) const`
- `template<std::size_t k, class InsertIter>`  
`void up (const std::set< SimplexID< k > > &simplices, InsertIter iter) const`
- `template<std::size_t k, class InsertIter>`  
`void up (const SimplexID< k > simplex, InsertIter iter) const`
- `template<std::size_t k>`  
`std::set< SimplexID< k-1 > > down (const std::set< SimplexID< k > > &&simplices) const`  
*Get the boundary of a set of simplices.*
- `template<std::size_t k>`  
`std::set< SimplexID< k-1 > > down (const std::set< SimplexID< k > > &simplices) const`  
*Get the boundary of a set of simplices.*
- `template<std::size_t k>`  
`std::set< SimplexID< k-1 > > down (const SimplexID< k > simplex) const`  
*Get the boundary of a simplex.*

- `template<std::size_t k, class InsertIter>`  
`void down (const std::set< SimplexID< k > > &&simplices, InsertIter iter) const`
- `template<std::size_t k, class InsertIter>`  
`void down (const std::set< SimplexID< k > > &simplices, InsertIter iter) const`
- `template<std::size_t k, class InsertIter>`  
`void down (const SimplexID< k > simplex, InsertIter iter) const`
- `template<std::size_t k>`  
`EdgeID< k+1 > get_edge_up (SimplexID< k > simplex, KeyType a)`  
*Gets the edge up from a simplex.*
- `template<std::size_t k>`  
`EdgeID< k > get_edge_down (SimplexID< k > simplex, KeyType a)`  
*Gets the edge down from a simplex.*
- `template<std::size_t k>`  
`EdgeID< k+1 > get_edge_up (SimplexID< k > simplex, KeyType a) const`  
*Gets the edge up from a simplex.*
- `template<std::size_t k>`  
`EdgeID< k > get_edge_down (SimplexID< k > simplex, KeyType a) const`  
*Gets the edge down from a simplex.*
- `template<std::size_t k>`  
`bool exists (const KeyType(&s)[k]) const`  
*Check whether a simplex with some name exists.*
- `template<std::size_t k>`  
`std::size_t size () const`  
*Get the number of simplices of dimension 'k'.*
- `template<std::size_t k>`  
`auto get_level_id ()`  
*Create an iterator to traverse the SimplexIDs of a dimension.*
- `template<std::size_t k>`  
`auto get_level_id () const`  
*Create an iterator to traverse the SimplexIDs of a dimension.*
- `template<std::size_t k>`  
`auto get_level ()`  
*Create an iterator to traverse the simplex data of a dimension.*
- `template<std::size_t k>`  
`auto get_level () const`  
*Create an iterator to traverse the simplex data of a dimension.*
- `template<std::size_t k>`  
`std::size_t remove (const KeyType(&s)[k])`  
*Remove a simplex and all dependent simplices by name.*
- `template<std::size_t k>`  
`std::size_t remove (const std::array< KeyType, k > &s)`  
*Remove a simplex and all dependent simplices by name.*
- `template<std::size_t k>`  
`std::size_t remove (SimplexID< k > s)`  
*Remove a simplex and all dependent simplices by SimplexID.*
- `template<std::size_t k>`  
`bool onBoundary (const SimplexID< k > s) const`  
*Checks whether a simplex is on a boundary.*
- `template<std::size_t level>`  
`bool nearBoundary (const SimplexID< level > s) const`  
*Checks whether a simplex is near a boundary.*
- `template<std::size_t L, std::size_t R>`  
`bool leq (SimplexID< L > lhs, SimplexID< R > rhs) const`

*Checks whether a simplex is on a boundary.*

- `template<std::size_t L, std::size_t R>`  
`bool eq (SimplexID< L >, SimplexID< R >) const`

*Equality comparison of two simplices.*

- `template<std::size_t k>`  
`bool eq (SimplexID< k > lhs, SimplexID< k > rhs) const`

*Equality comparison of two simplices.*

- `template<std::size_t L, std::size_t R>`  
`bool lt (SimplexID< L > lhs, SimplexID< R > rhs) const`

*Less than comparison of simplices.*

### Static Public Attributes

- `static constexpr std::size_t numLevels = NodeDataTypes::size`

*Total number of levels in the complex.*

- `static constexpr std::size_t topLevel = numLevels-1`

*Dimension of the simplicial complex.*

- `static constexpr std::size_t bdryLevel = numLevels-2`

*Dimension of boundaries.*

### Friends

- struct [SimplexID](#)
- struct [EdgeID](#)

## 9.14.1 Detailed Description

```
template<typename traits>
class casc::simplicial_complex< traits >
```

You can create a CASC object by defining a struct containing the traits of the complex. For example:

```
struct complex_traits{
    using KeyType = int;
    using NodeType = util::type_holder<int,int,int,int>;
    using EdgeTypes = util::type_holder<int,int,int>;
};

using SurfaceMesh = simplicial_complex<complex_traits>;
```

This is the preferred method for creating a new CASC type. Alternatively you can use the [AbstractSimplicialComplex](#) alias to build a struct for you.

### Template Parameters

<i>traits</i>	A struct defining the dimension of the complex and data to be stored on each node and edge.
---------------	---

## 9.14.2 Member Typedef Documentation

### 9.14.2.1 EdgeData

```
template<typename traits>
template<std::size_t k>
using casc::simplicial_complex< traits >::EdgeData = typename util::type_get<k, EdgeDataTypes>↵
::type
```

Convenience alias for the user specified `EdgeData<k>` typename

### 9.14.2.2 NodeData

```
template<typename traits>
template<std::size_t k>
using casc::simplicial_complex< traits >::NodeData = typename util::type_get<k, NodeDataTypes>↵
::type
```

Convenience alias for the user specified `NodeData<k>` typename

## 9.14.3 Constructor & Destructor Documentation

### 9.14.3.1 `~simplicial_complex()`

```
template<typename traits>
casc::simplicial_complex< traits >::~~simplicial_complex () [inline]
```

Recursively go over the simplices and remove them prior to destructing the CASC object itself.

## 9.14.4 Member Function Documentation

### 9.14.4.1 `add_vertex()` [1/2]

```
template<typename traits>
KeyType casc::simplicial_complex< traits >::add_vertex () [inline]
```

A list of currently unused indices are tracked using a B-tree. This function retrieves a currently unused index and creates a new vertex while returning the new key.

#### Returns

The key of the new vertex.

### 9.14.4.2 `add_vertex()` [2/2]

```
template<typename traits>
KeyType casc::simplicial_complex< traits >::add_vertex (
    const NodeData< 1 > & data) [inline]
```

#### Returns

The key of the new vertex.

### 9.14.4.3 `down()` [1/3]

```
template<typename traits>
template<std::size_t k>
std::set< SimplexID< k-1 > > casc::simplicial_complex< traits >::down (
    const SimplexID< k > simplex) const [inline]
```

**Parameters**

<i>simplex</i>	The simplex of interest.
----------------	--------------------------

**Template Parameters**

<i>k</i>	The dimension of the simplex.
----------	-------------------------------

**Returns**

Set of (k-1)-simplices of which 'simplex' is a coface of.

**9.14.4.4 down() [2/3]**

```
template<typename traits>
template<std::size_t k>
std::set< SimplexID< k-1 > > casc::simplicial_complex< traits >::down (
    const std::set< SimplexID< k > > && simplices) const [inline]
```

**Parameters**

<i>simplices</i>	The set of simplicies.
------------------	------------------------

**Template Parameters**

<i>k</i>	The dimension of the simplicies.
----------	----------------------------------

**Returns**

The set of boundary simplicies.

**9.14.4.5 down() [3/3]**

```
template<typename traits>
template<std::size_t k>
std::set< SimplexID< k-1 > > casc::simplicial_complex< traits >::down (
    const std::set< SimplexID< k > > & simplices) const [inline]
```

**Parameters**

<i>simplices</i>	The set of simplicies.
------------------	------------------------

**Template Parameters**

<i>k</i>	The dimension of the simplicies.
----------	----------------------------------

**Returns**

The set of boundary simplicies.



**9.14.4.6 `eq()`** [1/2]

```
template<typename traits>
template<std::size_t k>
bool casc::simplicial_complex< traits >::eq (
    SimplexID< k > lhs,
    SimplexID< k > rhs) const [inline]
```

**Parameters**

in	<i>lhs</i>	The left hand side
in	<i>rhs</i>	The right hand side

**Template Parameters**

<i>k</i>	Dimension of the simplices.
----------	-----------------------------

**Returns**

True if the names are the same.

**9.14.4.7 `eq()`** [2/2]

```
template<typename traits>
template<std::size_t L, std::size_t R>
bool casc::simplicial_complex< traits >::eq (
    SimplexID< L > ,
    SimplexID< R > ) const [inline]
```

**Parameters**

in	<i>lhs</i>	The left hand side
in	<i>rhs</i>	The right hand side

**Template Parameters**

<i>L</i>	Dimension of lhs simplex.
<i>R</i>	Dimension of rhs simplex.

**Returns**

Always false as  $L \neq R$ . The  $L=R$  case is overloaded by partial specialization.

**9.14.4.8 `exists()`**

```
template<typename traits>
template<std::size_t k>
bool casc::simplicial_complex< traits >::exists (
    const KeyType (&) s[k]) const [inline]
```

**Parameters**

in	<i>s</i>	C-style array of the name
----	----------	---------------------------

**Template Parameters**

<i>k</i>	The dimension of the simplex.
----------	-------------------------------

**Returns**

True if the simplex is in the complex.

**9.14.4.9 `get_cover()` [1/2]**

```
template<typename traits>
template<std::size_t k>
std::vector< KeyType > casc::simplicial_complex< traits >::get_cover (
    const SimplexID< k > id) const [inline]
```

**Parameters**

in	<i>id</i>	The identifier of a simplex.
----	-----------	------------------------------

**Template Parameters**

<i>k</i>	The dimension of the simplex.
----------	-------------------------------

**Returns**

A vector of coboundary indices.

**9.14.4.10 `get_cover()` [2/2]**

```
template<typename traits>
template<std::size_t k, class Lambda>
void casc::simplicial_complex< traits >::get_cover (
    const SimplexID< k > id,
    Lambda fn) const [inline]
```

**Parameters**

in	<i>id</i>	The identifier
in	<i>fn</i>	The function

**Template Parameters**

<i>k</i>	The dimension of the simplex.
<i>Lambda</i>	Typename of a functor which supports operator(KeyType).

**9.14.4.11 `get_cover_insert()`**

```
template<typename traits>
template<std::size_t k, class Inserter>
void casc::simplicial_complex< traits >::get_cover_insert (
    const SimplexID< k > id,
    Inserter pos) const [inline]
```

**Parameters**

in	<i>id</i>	The identifier of a simplex.
in	<i>pos</i>	Iterator inserter

**Template Parameters**

<i>k</i>	The dimension of the simplex.
<i>Inserter</i>	Typename of the inserter.

**9.14.4.12 `get_edge_down()` [1/2]**

```
template<typename traits>
template<std::size_t k>
EdgeID< k > casc::simplicial_complex< traits >::get_edge_down (
    SimplexID< k > simplex,
    KeyType a) [inline]
```

**Parameters**

in	<i>simplex</i>	The simplex of interest.
in	<i>a</i>	Key of the edge to get.

**Template Parameters**

<i>k</i>	The level of the simplex of interest
----------	--------------------------------------

**Returns**

The edge down.

**9.14.4.13 `get_edge_down()` [2/2]**

```
template<typename traits>
template<std::size_t k>
EdgeID< k > casc::simplicial_complex< traits >::get_edge_down (
    SimplexID< k > simplex,
    KeyType a) const [inline]
```

**Parameters**

in	<i>simplex</i>	The simplex of interest.
in	<i>a</i>	Key of the edge to get.

**Template Parameters**

<i>k</i>	The level of the simplex of interest
----------	--------------------------------------

**Returns**

The edge down.

**9.14.4.14 `get_edge_up()` [1/2]**

```
template<typename traits>
template<std::size_t k>
EdgeID< k+1 > casc::simplicial_complex< traits >::get_edge_up (
    SimplexID< k > simplex,
    KeyType a) [inline]
```

**Parameters**

in	<i>simplex</i>	The simplex of interest.
in	<i>a</i>	Key of the edge to get.

**Template Parameters**

<i>k</i>	The level of the simplex of interest
----------	--------------------------------------

**Returns**

The edge up.

**9.14.4.15 `get_edge_up()` [2/2]**

```
template<typename traits>
template<std::size_t k>
EdgeID< k+1 > casc::simplicial_complex< traits >::get_edge_up (
    SimplexID< k > simplex,
    KeyType a) const [inline]
```

**Parameters**

in	<i>simplex</i>	The simplex of interest.
in	<i>a</i>	Key of the edge to get.

## Template Parameters

<code>k</code>	The level of the simplex of interest
----------------	--------------------------------------

## Returns

The edge up.

9.14.4.16 `get_level()` [1/2]

```
template<typename traits>
template<std::size_t k>
auto casc::simplicial_complex< traits >::get_level () [inline]
```

## Template Parameters

<code>k</code>	The simplex dimension to traverse.
----------------	------------------------------------

## Returns

An iterator across the data of all k-simplices in the complex.

9.14.4.17 `get_level()` [2/2]

```
template<typename traits>
template<std::size_t k>
auto casc::simplicial_complex< traits >::get_level () const [inline]
```

## Template Parameters

<code>k</code>	The simplex dimension to traverse.
----------------	------------------------------------

## Returns

An iterator across the data of all k-simplices in the complex.

9.14.4.18 `get_level_id()` [1/2]

```
template<typename traits>
template<std::size_t k>
auto casc::simplicial_complex< traits >::get_level_id () [inline]
```

## Template Parameters

<code>k</code>	The simplex dimension to traverse.
----------------	------------------------------------

## Returns

An iterator across all k-simplices of the complex.

9.14.4.19 `get_level_id()` [2/2]

```
template<typename traits>
template<std::size_t k>
auto casc::simplicial_complex< traits >::get_level_id () const [inline]
```

### Template Parameters

<i>k</i>	The simplex dimension to traverse.
----------	------------------------------------

### Returns

An iterator across all k-simplices of the complex.

#### 9.14.4.20 `get_name()` [1/3]

```
template<typename traits>
std::array< KeyType, 0 > casc::simplicial_complex< traits >::get_name (
    SimplexID< 0 > ) const [inline]
```

This is the explicit specialization which handles the empty set simplex.

### Parameters

in	<i>id</i>	<a href="#">SimplexID</a> of the simplex of interest.
----	-----------	---

### Returns

Array containing the name of 'id'.

#### 9.14.4.21 `get_name()` [2/3]

```
template<typename traits>
template<std::size_t n>
std::array< KeyType, n > casc::simplicial_complex< traits >::get_name (
    SimplexID< n > id) const [inline]
```

### Parameters

in	<i>id</i>	<a href="#">SimplexID</a> of the simplex of interest.
----	-----------	---

### Template Parameters

<i>n</i>	Size of the simplex referenced by 'id'.
----------	---

### Returns

Array containing the name of 'id'.

#### 9.14.4.22 `get_name()` [3/3]

```
template<typename traits>
template<std::size_t n, typename Lambda>
void casc::simplicial_complex< traits >::get_name (
    SimplexID< n > id,
    Lambda fn) const [inline]
```

## Parameters

in	<i>id</i>	<a href="#">SimplexID</a> of the simplex of interest.
in	<i>fn</i>	Lambda function to apply to the name of 'id'.

## Template Parameters

<i>n</i>	Dimension of simplex 'id'.
<i>Lambda</i>	Functor which supports operator(KeyType).

9.14.4.23 `get_simplex_down()` [1/3]

```
template<typename traits>
SimplexID< 0 > casc::simplicial_complex< traits >::get_simplex_down () const [inline]
```

## Returns

The root simplex.

9.14.4.24 `get_simplex_down()` [2/3]

```
template<typename traits>
template<std::size_t i>
SimplexID< i-1 > casc::simplicial_complex< traits >::get_simplex_down (
    const SimplexID< i > id,
    const KeyType s) const [inline]
```

## Parameters

in	<i>id</i>	The identifier of a simplex.
in	<i>s</i>	The relative single character name of the desired simplex.

## Template Parameters

<i>i</i>	The size of simplex 'id'.
----------	---------------------------

## Returns

The node down.

9.14.4.25 `get_simplex_down()` [3/3]

```
template<typename traits>
template<std::size_t i, std::size_t j>
SimplexID< i-j > casc::simplicial_complex< traits >::get_simplex_down (
    const SimplexID< i > id,
    const KeyType (&) s[j]) const [inline]
```

**Parameters**

in	<i>id</i>	The identifier of a simplex.
in	<i>s</i>	The relative name of the desired simplex.

**Template Parameters**

<i>i</i>	The size of simplex 'id'.
<i>j</i>	The length of the name 's'.

**Returns**

The node down.

**9.14.4.26 get\_simplex\_up() [1/4]**

```
template<typename traits>
SimplexID< 0 > casc::simplicial_complex< traits >::get_simplex_up () const [inline]
```

**Returns**

The root simplex.

**9.14.4.27 get\_simplex\_up() [2/4]**

```
template<typename traits>
template<std::size_t n>
SimplexID< n > casc::simplicial_complex< traits >::get_simplex_up (
    const KeyType(&) s[n]) const [inline]
```

**Parameters**

in	<i>s</i>	Name of the simplex to find.
----	----------	------------------------------

**Template Parameters**

<i>n</i>	Dimension of simplex s.
----------	-------------------------

**Returns**

[SimplexID](#) of node corresponding to 's'.

**9.14.4.28 get\_simplex\_up() [3/4]**

```
template<typename traits>
template<std::size_t i>
SimplexID< i+1 > casc::simplicial_complex< traits >::get_simplex_up (
    const SimplexID< i > id,
    const KeyType s) const [inline]
```



## Parameters

in	<i>id</i>	The identifier of a simplex.
in	<i>s</i>	The relative single character name of the desired simplex.

## Template Parameters

<i>i</i>	The size of simplex 'id'.
----------	---------------------------

## Returns

[SimplexID](#) of node corresponding to  $id \cup s$ .

9.14.4.29 `get_simplex_up()` [4/4]

```
template<typename traits>
template<std::size_t i, std::size_t j>
SimplexID< i+j > casc::simplicial_complex< traits >::get_simplex_up (
    const SimplexID< i > id,
    const KeyType(&) s[j]) const [inline]
```

## Parameters

in	<i>id</i>	The identifier of a simplex.
in	<i>s</i>	The relative name of the desired simplex.

## Template Parameters

<i>i</i>	The size of simplex 'id'.
<i>j</i>	The length of the name 's'.

## Returns

[SimplexID](#) of node corresponding to  $id \cup s$ .

9.14.4.30 `insert()` [1/4]

```
template<typename traits>
template<std::size_t n>
SimplexID< n > casc::simplicial_complex< traits >::insert (
    const KeyType(&) s[n]) [inline]
```

Example – insert the simplex {1,2,3}:

```
mesh.insert<3>({1,2,3});
```

**Parameters**

in	<i>s</i>	A C style array of vertices of simplex 's'.
----	----------	---

**Template Parameters**

<i>n</i>	Dimension of simplex 's'.
----------	---------------------------

**9.14.4.31 insert() [2/4]**

```
template<typename traits>
template<std::size_t n>
SimplexID< n > casc::simplicial_complex< traits >::insert (
    const KeyType (&) s[n],
    const NodeData< n > & data) [inline]
```

Example – insert the simplex {1,2,3} with data:

```
mesh.insert<3>({1,2,3}, 5);
```

**Parameters**

in	<i>s</i>	A C style array of vertices of simplex 's'.
in	<i>data</i>	The data to be stored at the simplex 's'.

**Template Parameters**

<i>n</i>	Dimension of simplex 's'.
----------	---------------------------

**9.14.4.32 insert() [3/4]**

```
template<typename traits>
template<std::size_t n>
SimplexID< n > casc::simplicial_complex< traits >::insert (
    const std::array< KeyType, n > & s) [inline]
```

**Parameters**

in	<i>s</i>	Array of vertices comprising 's'.
----	----------	-----------------------------------

**Template Parameters**

<i>n</i>	Dimension of simplex 's'.
----------	---------------------------

**9.14.4.33 insert() [4/4]**

```
template<typename traits>
template<std::size_t n>
SimplexID< n > casc::simplicial_complex< traits >::insert (
    const std::array< KeyType, n > & s,
    const NodeData< n > & data) [inline]
```

## Parameters

<code>in</code>	<code>s</code>	Array of vertices comprising 's'.
<code>in</code>	<code>data</code>	The data to be stored at the simplex 's'.

## Template Parameters

<code>n</code>	Dimension of simplex 's'.
----------------	---------------------------

9.14.4.34 `leq()`

```
template<typename traits>
template<std::size_t L, std::size_t R>
bool casc::simplicial_complex< traits >::leq (
    SimplexID< L > lhs,
    SimplexID< R > rhs) const [inline]
```

## Parameters

<code>in</code>	<code>s</code>	<code>SimplexID</code> of interest
-----------------	----------------	------------------------------------

## Template Parameters

<code>k</code>	Dimension of the simplex
----------------	--------------------------

## Returns

True if the simplex interacts with a `topLevel-1` simplex which is on a boundary.

Specialization of the facets

## Parameters

<code>in</code>	<code>s</code>	<code>SimplexID</code> of interest
-----------------	----------------	------------------------------------

## Template Parameters

<code>k</code>	Dimension of the simplex
----------------	--------------------------

## Returns

True if `s` is on a boundary

Specialization of the `topLevel-1` simplices

**Parameters**

in	<i>s</i>	SimplexID of interest
----	----------	-----------------------

**Template Parameters**

<i>k</i>	Dimension of the simplex
----------	--------------------------

**Returns**

True if *s* is on a boundary

Less than or equal to comparison operator of two SimplexIDs.

**Parameters**

in	<i>lhs</i>	The left hand side
in	<i>rhs</i>	The right hand side

**Template Parameters**

<i>L</i>	Dimension of lhs simplex.
<i>R</i>	Dimension of rhs simplex.

**Returns**

True if lhs is rhs or a proper face of rhs.

**9.14.4.35 lt()**

```
template<typename traits>
template<std::size_t L, std::size_t R>
bool casc::simplicial_complex< traits >::lt (
    SimplexID< L > lhs,
    SimplexID< R > rhs) const [inline]
```

**Parameters**

in	<i>lhs</i>	The left hand side
in	<i>rhs</i>	The right hand side

**Template Parameters**

<i>L</i>	Dimension of lhs simplex.
<i>R</i>	Dimension of rhs simplex.

**Returns**

True if lhs is a proper subface of rhs.

**9.14.4.36 `nearBoundary()`**

```
template<typename traits>
template<std::size_t level>
bool casc::simplicial_complex< traits >::nearBoundary (
    const SimplexID< level > s) const [inline]
```

**Parameters**

<code>in</code>	<code>s</code>	<code>SimplexID</code> of interest
-----------------	----------------	------------------------------------

**Template Parameters**

<code>level</code>	Dimension of the simplex
--------------------	--------------------------

**Returns**

True if the simplex or any subsimplices are onBoundary.

**9.14.4.37 `onBoundary()`**

```
template<typename traits>
template<std::size_t k>
bool casc::simplicial_complex< traits >::onBoundary (
    const SimplexID< k > s) const [inline]
```

**Parameters**

<code>in</code>	<code>s</code>	<code>SimplexID</code> of interest
-----------------	----------------	------------------------------------

**Template Parameters**

<code>k</code>	Dimension of the simplex
----------------	--------------------------

**Returns**

True if the simplex is a member of a topLevel-1 simplex on the boundary or if the simplex is on a boundary or if the simplex is a coboundary of a boundary topLevel-1 simplex.

**9.14.4.38 `remove()` [1/3]**

```
template<typename traits>
template<std::size_t k>
std::size_t casc::simplicial_complex< traits >::remove (
    const KeyType(&) s[k]) [inline]
```

**Parameters**

in	s	C-style array with the name of the simplex to remove.
----	---	---

**Template Parameters**

k	The dimension of the simplex.
---	-------------------------------

**Returns**

Integer corresponding to the number of simplices removed.

**9.14.4.39 remove() [2/3]**

```
template<typename traits>
template<std::size_t k>
std::size_t casc::simplicial_complex< traits >::remove (
    const std::array< KeyType, k > & s) [inline]
```

**Parameters**

in	s	std::array with the name of the simplex to remove.
----	---	--

**Template Parameters**

k	The dimension of the simplex.
---	-------------------------------

**Returns**

Integer corresponding to the number of simplices removed.

**9.14.4.40 remove() [3/3]**

```
template<typename traits>
template<std::size_t k>
std::size_t casc::simplicial_complex< traits >::remove (
    SimplexID< k > s) [inline]
```

**Parameters**

in	s	SimplexID of the simplex to remove.
----	---	-------------------------------------

**Template Parameters**

k	The dimension of the simplex.
---	-------------------------------

**Returns**

Integer corresponding to the number of simplices removed.

#### 9.14.4.41 `size()`

```
template<typename traits>
template<std::size_t k>
std::size_t casc::simplicial_complex< traits >::size () const [inline]
```

## Template Parameters

<i>k</i>	The dimension of interest.
----------	----------------------------

## Returns

Integer number of k-simplices in the complex.

**9.14.4.42 up()** [1/3]

```
template<typename traits>
template<std::size_t k>
std::set< SimplexID< k+1 > > casc::simplicial_complex< traits >::up (
    const SimplexID< k > nid) const [inline]
```

## Parameters

<i>nid</i>	The simplex of interest
------------	-------------------------

## Template Parameters

<i>k</i>	The dimension of the simplex.
----------	-------------------------------

## Returns

Set of (k+1)-simplices of which 'nid' is a face of.

**9.14.4.43 up()** [2/3]

```
template<typename traits>
template<std::size_t k>
std::set< SimplexID< k+1 > > casc::simplicial_complex< traits >::up (
    const std::set< SimplexID< k > > && simplices) const [inline]
```

## Parameters

<i>simplices</i>	The set of simplices
------------------	----------------------

## Template Parameters

<i>k</i>	The dimension of the simplices.
----------	---------------------------------

## Returns

The set of coboundary simplices.

**9.14.4.44 up()** [3/3]

```
template<typename traits>
template<std::size_t k>
std::set< SimplexID< k+1 > > casc::simplicial_complex< traits >::up (
    const std::set< SimplexID< k > > & simplices) const [inline]
```



## Parameters

<i>simplices</i>	The set of simplices
------------------	----------------------

## Template Parameters

<i>k</i>	The dimension of the simplices.
----------	---------------------------------

## Returns

The set of coboundary simplices.

## 9.14.5 Friends And Related Symbol Documentation

### 9.14.5.1 EdgeID

```
template<typename traits>
friend struct EdgeID [friend]
```

[EdgeID](#) is a friend to [simplicial\\_complex](#)

### 9.14.5.2 SimplexID

```
template<typename traits>
friend struct SimplexID [friend]
```

[SimplexID](#) is a friend of [simplicial\\_complex](#)

The documentation for this class was generated from the following file:

- [include/casc/SimplicialComplex.h](#)

## 9.15 util::type\_get< k, T > Struct Template Reference

Helper to get the kth element from a [type\\_holder](#).

```
#include <util.h>
```

### 9.15.1 Detailed Description

```
template<std::size_t k, typename T>
struct util::type_get< k, T >
```

This is the empty general template which will be later specialized.

## Template Parameters

<i>k</i>	Integer index of the type to retrieve
<i>T</i>	A <a href="#">type_holder</a> queue of typenames

The documentation for this struct was generated from the following file:

- [include/casc/util.h](#)

## 9.16 `util::type_get< 0, type_holder< Ts... > >` Struct Template Reference

Specialization for terminal case.

```
#include <util.h>
```

## Public Types

- using **type** = typename [type\\_holder](#)<Ts...>::head  
*The first type of the [type\\_holder](#).*

### 9.16.1 Detailed Description

```
template<typename ... Ts>
struct util::type_get< 0, type_holder< Ts... > >
```

## Template Parameters

<i>Ts</i>	Following typenames
-----------	---------------------

The documentation for this struct was generated from the following file:

- [include/casc/util.h](#)

## 9.17 `util::type_get< k, type_holder< Ts... > >` Struct Template Reference

Specialization to recursively pop types to get the kth type.

```
#include <util.h>
```

## Public Types

- using **type** = typename [type\\_get](#)<k-1, typename [type\\_holder](#)<Ts...>::tail>::type  
*Recurse after popping the first type off.*

### 9.17.1 Detailed Description

```
template<std::size_t k, typename ... Ts>
struct util::type_get< k, type_holder< Ts... > >
```

## Template Parameters

<i>k</i>	Integral constant of the type to get
<i>Ts</i>	List of typenames

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.18 util::type\_holder< Ts > Struct Template Reference

Queue based data structure to hold list of types.

```
#include <util.h>
```

## Static Public Attributes

- static const std::size\_t **size** = sizeof ... (Ts)  
*Length of the list of types.*

### 9.18.1 Detailed Description

```
template<typename ... Ts>
struct util::type_holder< Ts >
```

Types in the [type\\_holder](#) can be accessed by accessing the `head` type. Subsequent types are in the `tail`. See also [type\\_get](#).

## Template Parameters

<i>Ts</i>	List of typenames
-----------	-------------------

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.19 util::type\_holder< T, Ts... > Struct Template Reference

Partial specialization to allow FIFO access of typenames.

```
#include <util.h>
```

## Public Types

- using **head** = T  
*The first type.*
- using **tail** = [type\\_holder](#)<Ts...>  
*The following types.*

## Static Public Attributes

- static const std::size\_t **size** = 1 + [type\\_holder](#)<Ts...>::size  
*Length of the list of types.*
- static const std::size\_t **size**  
*Length of the list of types.*

### 9.19.1 Detailed Description

```
template<typename T, typename ... Ts>
struct util::type_holder< T, Ts... >
```

#### Template Parameters

<i>T</i>	The first typename
<i>Ts</i>	The following typenames

The documentation for this struct was generated from the following file:

- [include/casc/util.h](#)

## 9.20 util::type\_map< C, V > Struct Template Reference

Map the types in C into V<T>.

```
#include <util.h>
```

## Public Types

- using **type** = typename detail::type\_map\_helper<C, V>::type  
*Tuple of C<V<T1>, V<T2>, V<T3>, ...>*

### 9.20.1 Detailed Description

```
template<class C, template< typename > class V>
struct util::type_map< C, V >
```

Given a container of types C<T1, T2, T3, ...> and template type V<T>, this function will apply the types in C to V<T>. This produces C<V<T1>, V<T2>, V<T3>, ...>.

## Template Parameters

<i>C</i>	Container of compile time types.
<i>V</i>	Template template class $\mathbb{V}<\mathbb{T}>$ to map into.

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.21 util::type\_swap< TUPLE, HOLDER\_FULL > Struct Template Reference

Move a list of types from one container to another.

```
#include <util.h>
```

### 9.21.1 Detailed Description

```
template<template< class ... > class TUPLE, typename HOLDER_FULL>
struct util::type_swap< TUPLE, HOLDER_FULL >
```

## Template Parameters

<i>TUPLE</i>	Empty container
<i>HOLDER_FULL</i>	Full container

The documentation for this struct was generated from the following file:

- include/casc/[util.h](#)

## 9.22 util::type\_swap< TUPLE, HOLDER< Ts... > > Struct Template Reference

Move a list of types from one container to another.

```
#include <util.h>
```

## Public Types

- using **type** = TUPLE<Ts...>  
*Empty container filled with typenames from full container.*

### 9.22.1 Detailed Description

```
template<template< class ... > class TUPLE, template< class ... > class HOLDER, typename ... Ts>
struct util::type_swap< TUPLE, HOLDER< Ts... > >
```

## Template Parameters

<i>TUPLE</i>	Empty container
<i>HOLDER</i>	Full container
<i>Ts</i>	Typenames in full container

The documentation for this struct was generated from the following file:

- `include/casc/util.h`

# Chapter 10

## File Documentation

### 10.1 include/casc/CASCFunctions.h File Reference

Contains various functions that operate on simplicial complexes.

```
#include <iostream>
#include <fstream>
#include "SimplicialComplex.h"
#include "CASCTraversals.h"
#include "SimplexSet.h"
#include "stringutil.h"
```

#### Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

#### Functions

- template<typename Complex>  
void `casc::getStar` (Complex &F, `casc::SimplexSet`< Complex > &S, `casc::SimplexSet`< Complex > &dest)  
*Gets the star of a `SimplexSet`.*
- template<typename Complex, typename Simplex>  
void `casc::getStar` (Complex &F, Simplex &s, `casc::SimplexSet`< Complex > &dest)  
*Gets the star of a simplex.*
- template<typename Complex>  
void `casc::getClosure` (Complex &F, `casc::SimplexSet`< Complex > &S, `casc::SimplexSet`< Complex > &dest)  
*Gets the closure of a simplex set.*
- template<typename Complex, typename Simplex>  
void `casc::getClosure` (Complex &F, Simplex &s, `casc::SimplexSet`< Complex > &dest)  
*Compute the closure of a simplex.*
- template<typename Complex>  
void `casc::getLink` (Complex &F, `casc::SimplexSet`< Complex > &S, `casc::SimplexSet`< Complex > &dest)  
*Gets the link of a `SimplexSet`.*
- template<typename Complex, typename Simplex>  
void `casc::getLink` (Complex &F, Simplex &s, `casc::SimplexSet`< Complex > &dest)  
*Gets the link of a simplex.*
- template<typename Complex>  
void `casc::writeDOT` (const std::string &filename, Complex &F)  
*Writes out the topology of an ASC into the dot format.*

## 10.2 CASCFunctions.h

[Go to the documentation of this file.](#)

```

00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
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00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00029
00030 #pragma once
00031
00032 #include <iostream>
00033 #include <fstream>
00034 #include "SimplicialComplex.h"
00035 #include "CASCTraversals.h"
00036 #include "SimplexSet.h"
00037 #include "stringutil.h"
00038
00039 namespace casc
00040 {
00043 namespace func_detail
00044 {
00045
00052 template <typename Complex>
00053 struct SimplexAggregator
00054 {
00056     using SimplexSet = typename casc::SimplexSet<Complex>;
00057
00063     SimplexAggregator(SimplexSet* p) : pLevels(p) {}
00064
00076     template <std::size_t k>
00077     bool visit(Complex &, typename Complex::template SimplexID<k> s)
00078     {
00079         // If the simplex isn't there, insert it.
00080         if (pLevels->find(s) == pLevels->template end<k>())
00081         {
00082             pLevels->insert(s);
00083             return true;
00084         }
00085         else
00086         {
00087             // Everything after has been found already
00088             return false;
00089         }
00090     }
00091     private:
00092         SimplexSet* pLevels;
00093 };
00094
00100 template <typename Complex>
00101 struct StarHelper
00102 {
00112     template <std::size_t k>
00113     static void apply(Complex &F,
00114                     casc::SimplexSet<Complex> &S,
00115                     casc::SimplexSet<Complex> &dest)
00116     {
00117         auto s = casc::get<k>(S);
00118         for (auto simplex : s)
00119         {
00120             visit_BFS_up(SimplexAggregator<Complex>(&dest), F, simplex);
00121         }
00122     }
00123 };
00124
00130 template <typename Complex>

```



```

00131 struct ClosureHelper
00132 {
00142     template <std::size_t k>
00143     static void apply(Complex &F,
00144                       casc::SimplexSet<Complex> &S,
00145                       casc::SimplexSet<Complex> &dest)
00146     {
00147         auto s = casc::get<k>(S);
00148         for (auto simplex : s)
00149         {
00150             visit_BFS_down(SimplexAggregator<Complex>(&dest), F, simplex);
00151         }
00152     }
00153 };
00154
00160 template <typename Complex>
00161 struct GraphVisitor
00162 {
00164     std::ostream &fout;
00165
00171     GraphVisitor(std::ostream &os) : fout(os) {}
00172
00183     template <std::size_t level>
00184     bool visit(const Complex &F, typename Complex::template SimplexID<level> s)
00185     {
00186         auto name = to_string(F.get_name(s));
00187
00188         auto covers = F.get_cover(s);
00189         for (auto cover : covers)
00190         {
00191             auto edge = F.get_edge_up(s, cover);
00192             auto nextName = to_string(F.get_name(edge.up()));
00193             if ((*edge).orientation == 1)
00194             {
00195                 fout << "  \"\" < name < \"\" -> \"\"
00196                     << nextName < \"\" < std::endl;
00197             }
00198             else
00199             {
00200                 fout << "  \"\" < nextName < \"\" -> \"\"
00201                     << name < \"\" < std::endl;
00202             }
00203         }
00204         return true;
00205     }
00206
00216     bool visit(const Complex &F, typename Complex::template SimplexID<Complex::topLevel-1> s)
00217     {
00218
00219         auto name = to_string(F.get_name(s));
00220         auto covers = F.get_cover(s);
00221         for (auto cover : covers)
00222         {
00223             auto edge = F.get_edge_up(s, cover);
00224             auto nextName = to_string(F.get_name(edge.up()));
00225             auto orient = (*edge.up()).orientation;
00226             if (orient == 1)
00227             {
00228                 nextName = "+" + nextName;
00229             }
00230             else
00231             {
00232                 nextName = "-" + nextName;
00233             }
00234             if ((*edge).orientation == 1)
00235             {
00236                 fout << "  \"\" < name < \"\" -> \"\"
00237                     << nextName < \"\" < std::endl;
00238             }
00239             else
00240             {
00241                 fout << "  \"\" < nextName < \"\" -> \"\"
00242                     << name < \"\" < std::endl;
00243             }
00244         }
00245         return true;
00246     }
00247
00255     void visit(const Complex &, typename Complex::template SimplexID<Complex::topLevel>){}
00256 };
00257
00264 template <typename Complex, typename K>
00265 struct DotHelper {};
00266
00273 template <typename Complex, std::size_t k>
00274 struct DotHelper<Complex, std::integral_constant<std::size_t, k> >
00275 {

```

```

00282     static void printlevel(std::ofstream &fout, const Complex &F)
00283     {
00284         auto nodes = F.template get_level_id<k>();
00285         fout << "subgraph cluster_" << k << " {\n"
00286             << "label=\"Level " << k << "\"\n";
00287         for (auto node : nodes)
00288         {
00289             fout << "\"" << to_string(F.get_name(node)) << "\"";
00290         }
00291         fout << "\n}\n";
00292         DotHelper<Complex, std::integral_constant<std::size_t, k+1> >::printlevel(fout, F);
00293     }
00294 };
00295
00301 template <typename Complex>
00302 struct DotHelper<Complex, std::integral_constant<std::size_t, Complex::topLevel> >
00303 {
00310     static void printlevel(std::ofstream &fout, const Complex &F)
00311     {
00312         auto nodes = F.template get_level_id<Complex::topLevel>();
00313         fout << "subgraph cluster_" << Complex::topLevel << " {\n"
00314             << "label=\"Level " << Complex::topLevel << "\"\n";
00315         for (auto node : nodes)
00316         {
00317             auto orient = (*node).orientation;
00318             if (orient == 1)
00319             {
00320                 fout << "\"+ ";
00321             }
00322             else
00323             {
00324                 fout << "\"- ";
00325             }
00326             fout << to_string(F.get_name(node)) << "\"";
00327         }
00328         fout << "\n}\n";
00329     }
00330 };
00331 } // end namespace func_detail
00332
00343 template <typename Complex>
00344 void getStar(Complex &F, casc::SimplexSet<Complex> &S,
00345             casc::SimplexSet<Complex> &dest)
00346 {
00347     using SimplexSet = typename casc::SimplexSet<Complex>;
00348     using RevIndex   = typename SimplexSet::cRevIndex;
00349
00350     // Start at the top and work up. We can assume that if we've seen it then
00351     // everything after has been added.
00352     util::int_for_each<std::size_t, RevIndex>(
00353         func_detail::StarHelper<Complex>(), F, S, dest);
00354 }
00355
00366 template <typename Complex, typename Simplex>
00367 void getStar(Complex &F, Simplex &s, casc::SimplexSet<Complex> &dest)
00368 {
00369     visit_BFS_up(func_detail::SimplexAggregator<Complex>(&dest), F, s);
00370 }
00371
00381 template <typename Complex>
00382 void getClosure(Complex &F, casc::SimplexSet<Complex> &S,
00383               casc::SimplexSet<Complex> &dest)
00384 {
00385     using SimplexSet = typename casc::SimplexSet<Complex>;
00386     using LevelIndex = typename SimplexSet::cLevelIndex;
00387     // Start at the bottom and work down.
00388     // We can assume that everything below has been looked at.
00389     util::int_for_each<std::size_t, LevelIndex>(
00390         func_detail::ClosureHelper<Complex>(), F, S, dest);
00391 }
00392
00403 template <typename Complex, typename Simplex>
00404 void getClosure(Complex &F, Simplex &s, casc::SimplexSet<Complex> &dest)
00405 {
00406     visit_BFS_down(func_detail::SimplexAggregator<Complex>(&dest), F, s);
00407 }
00408
00418 template <typename Complex>
00419 void getLink(Complex &F, casc::SimplexSet<Complex> &S,
00420            casc::SimplexSet<Complex> &dest)
00421 {
00422     using SimplexSet = typename casc::SimplexSet<Complex>;
00423
00424     SimplexSet star;
00425     SimplexSet closure;
00426     SimplexSet closeStar;
00427     SimplexSet starClose;

```

```

00428     getStar(F, S, star);
00429     getClosure(F, star, closeStar);
00430
00431     getClosure(F, S, closure);
00432     getStar(F, closure, starClose);
00433     casc::set_difference(closeStar, starClose, dest);
00434 }
00435
00446 template <typename Complex, typename Simplex>
00447 void getLink(Complex &F, Simplex &s, casc::SimplexSet<Complex> &dest)
00448 {
00449     using SimplexSet = typename casc::SimplexSet<Complex>;
00450     SimplexSet star;
00451     SimplexSet closure;
00452     SimplexSet closeStar;
00453     SimplexSet starClose;
00454     getStar(F, s, star);
00455     getClosure(F, star, closeStar);
00456
00457     getClosure(F, s, closure);
00458     getStar(F, closure, starClose);
00459     casc::set_difference(closeStar, starClose, dest);
00460 }
00461
00476 template <typename Complex>
00477 void writeDOT(const std::string &filename, Complex &F)
00478 {
00479     // TODO: Put back the const F (0)
00480     std::ofstream fout(filename);
00481     if (!fout.is_open())
00482     {
00483         std::cerr << "File '" << filename
00484                 << "' could not be written to." << std::endl;
00485         fout.close();
00486         exit(1);
00487     }
00488
00489     fout << "digraph {\n"
00490         << "node [shape = record,height = .1]"
00491         << "splines=line;\n"
00492         << "dpi=300;\n";
00493     auto v = func_detail::GraphVisitor<Complex>(fout);
00494     visit_BFS_up(v, F, F.get_simplex_up());
00495
00496     // List the simplices
00497     func_detail::DotHelper<Complex,
00498                         std::integral_constant<std::size_t, 0>>::printlevel(fout, F);
00499     fout << "}\n";
00500     fout.close();
00501 }
00502 } // end namespace casc

```

## 10.3 include/casc/CASCTraversals.h File Reference

Implementations of various advanced traversals such as by neighborhood and breadth first search.

```

#include <set>
#include <vector>
#include <iostream>
#include <string>
#include <type_traits>
#include <utility>
#include <casc/casc>

```

### Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

## Functions

- `template<typename Visitor, typename SimplexID>`  
`void casc::visit\_BFS\_up (Visitor &&v, typename SimplexID::complex &F, SimplexID s)`  
*Traverse BFS up the complex and apply a visitor function to each simplex visited.*
- `template<typename Visitor, typename SimplexID>`  
`void casc::visit\_BFS\_down (Visitor &&v, typename SimplexID::complex &F, SimplexID s)`  
*Traverse BFS down the complex and apply a visitor function to each simplex visited.*
- `template<typename Visitor, typename EdgeID>`  
`void casc::edge\_up (Visitor &&v, typename EdgeID::complex &F, EdgeID s)`  
*Traverse across edges BFS.*
- `template<class Complex, std::size_t level, class InsertIter>`  
`void casc::neighbors (Complex &F, typename Complex::template SimplexID< level > nid, InsertIter iter)`  
*Push the immediate face neighbors into the provided iterator.*
- `template<class Complex, class SimplexID, class InsertIter>`  
`void casc::neighbors (Complex &F, SimplexID nid, InsertIter iter)`  
*This is a helper function to assist neighbors to automatically deduce the integral level.*
- `template<class Complex, std::size_t level, class InsertIter>`  
`void casc::neighbors\_up (Complex &F, typename Complex::template SimplexID< level > nid, InsertIter iter)`  
*Push the immediate coface neighbors into the provided iterator.*
- `template<class Complex, class SimplexID, class InsertIter>`  
`void casc::neighbors\_up (Complex &F, SimplexID nid, InsertIter iter)`  
*This is a helper function to assist neighbors to automatically deduce the integral level.*
- `template<class Complex, std::size_t level, typename Iterator>`  
`void casc::kneighbors\_up (Complex &F, int ring, std::set< typename Complex::template SimplexID< level >  
> &nbors, Iterator begin, Iterator end)`  
*Code for returning a set of k-ring neighbors.*
- `template<class Complex, class SimplexID>`  
`void casc::kneighbors\_up (Complex &F, SimplexID nid, int ring, std::set< SimplexID > &nbors)`  
*Helper function to help [kneighbors\\_up](#) to deduce the integral level of SimplexID.*
- `template<class Complex, std::size_t level, typename Iterator>`  
`void casc::kneighbors (Complex &F, int ring, std::set< typename Complex::template SimplexID< level > >  
&nbors, Iterator begin, Iterator end)`  
*Code for returning a set of k-ring neighbors.*
- `template<class Complex, class SimplexID>`  
`void casc::kneighbors (Complex &F, SimplexID nid, int ring, std::set< SimplexID > &nbors)`  
*Helper function to help [kneighbors](#) to deduce the integral level of SimplexID.*

## 10.4 CASCTraversals.h

[Go to the documentation of this file.](#)

```

00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
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00012  *
00013  * This library is distributed in the hope that it will be useful,
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00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *

```

```

00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00030
00031 #pragma once
00032
00033 #include <set>
00034 #include <vector>
00035 #include <iostream>
00036 #include <string>
00037 #include <type_traits>
00038 #include <utility>
00039 #include <casc/casc>
00040
00041 namespace casc
00042 {
00043     namespace visitor_detail
00044     {
00045         template <typename Visitor, typename Traits, typename Complex, typename K>
00046         struct BFS_Up_Node {};
00047
00048         template <typename Visitor, typename Traits, typename Complex, std::size_t k>
00049         struct BFS_Up_Node<Visitor, Traits, Complex, std::integral_constant<std::size_t, k> >
00050         {
00051             static constexpr auto level = k;
00052             using CurrSimplexID = typename Complex::template SimplexID<level>;
00053             using NextSimplexID = typename Complex::template SimplexID<level+1>;
00054             template <typename T> using Container = typename Traits::template Container<T>;
00055
00056             using BFS_Up_Node_Next = BFS_Up_Node<Visitor, Traits, Complex, std::integral_constant<std::size_t,
00057             level+1> >;
00058
00059             template <typename Iterator>
00060             static void apply(Visitor &&v, Complex &F, Iterator begin, Iterator end)
00061             {
00062                 Container<NextSimplexID> next;
00063
00064                 for (auto curr = begin; curr != end; ++curr)
00065                 {
00066                     if (v.visit(F, *curr))
00067                     {
00068                         F.get_cover(*curr, [&](typename Complex::KeyType a)
00069                         {
00070                             auto id = F.get_simplex_up(*curr, a);
00071                             next.insert(id);
00072                         });
00073                     }
00074                 }
00075
00076                 BFS_Up_Node_Next::apply(std::forward<Visitor>(v), F, next.begin(), next.end());
00077             }
00078         };
00079
00080         template <typename Visitor, typename Traits, typename Complex>
00081         struct BFS_Up_Node<Visitor, Traits, Complex, std::integral_constant<std::size_t, Complex::topLevel> >
00082         {
00083             static constexpr auto level = Complex::topLevel;
00084             using CurrSimplexID = typename Complex::template SimplexID<level>;
00085
00086             template <typename Iterator>
00087             static void apply(Visitor &&v, Complex &F, Iterator begin, Iterator end)
00088             {
00089                 for (auto curr = begin; curr != end; ++curr)
00090                 {
00091                     v.visit(F, *curr);
00092                 }
00093             }
00094         };
00095
00096         template <typename Visitor, typename Traits, typename Complex, typename K>
00097         struct BFS_Down_Node {};
00098
00099         template <typename Visitor, typename Traits, typename Complex, std::size_t k>
00100         struct BFS_Down_Node<Visitor, Traits, Complex, std::integral_constant<std::size_t, k> >
00101         {
00102             static constexpr auto level = k;
00103             using CurrSimplexID = typename Complex::template SimplexID<level>;
00104             using NextSimplexID = typename Complex::template SimplexID<level-1>;
00105             template <typename T> using Container = typename Traits::template Container<T>;
00106
00107             using BFS_Down_Node_Next = BFS_Down_Node<Visitor, Traits, Complex,

```

```

std::integral_constant<std::size_t, level-1> >;
00184
00195     template <typename Iterator>
00196     static void apply(Visitor &&v, Complex &F, Iterator begin, Iterator end)
00197     {
00198         Container<NextSimplexID> next;
00199
00200         for (auto curr = begin; curr != end; ++curr)
00201         {
00202             if (v.visit(F, *curr))
00203             {
00204                 F.get_name(*curr, [&](typename Complex::KeyType a)
00205                 {
00206                     auto id = F.get_simplex_down(*curr, a);
00207                     next.insert(id);
00208                 });
00209             }
00210         }
00211
00212         BFS_Down_Node_Next::apply(std::forward<Visitor>(v), F, next.begin(), next.end());
00213     }
00214 };
00215
00223 template <typename Visitor, typename Traits, typename Complex>
00224 struct BFS_Down_Node<Visitor, Traits, Complex, std::integral_constant<std::size_t, 1> >
00225 {
00236     template <typename Iterator>
00237     static void apply(Visitor &&v, Complex &F, Iterator begin, Iterator end)
00238     {
00239         for (auto curr = begin; curr != end; ++curr)
00240         {
00241             v.visit(F, *curr);
00242         }
00243     }
00244 };
00245
00254 // template <typename Visitor, typename Traits, typename Complex>
00255 // struct BFS_Down_Node<Visitor, Traits, Complex,
00256 // std::integral_constant<std::size_t, 0>
00257 // {
00258 //     template <typename Iterator>
00259 //     static void apply(Visitor&& v, Complex& F, Iterator begin, Iterator end)
00260 //     {}
00261 // };
00262
00263
00272 template <typename Visitor, typename Traits, typename Complex, typename K>
00273 struct BFS_Edge {};
00274
00275
00284 template <typename Visitor, typename Traits, typename Complex, std::size_t k>
00285 struct BFS_Edge<Visitor, Traits, Complex, std::integral_constant<std::size_t, k> >
00286 {
00287     static constexpr auto level = k;
00288     using CurrEdgeID = typename Complex::template EdgeID<level>;
00289     using NextEdgeID = typename Complex::template EdgeID<level+1>;
00290     using CurrSimplexID = typename Complex::template SimplexID<level>;
00291     template <typename T> using Container = typename Traits::template Container<T>;
00292     using BFS_Edge_Next = BFS_Edge<Visitor, Traits, Complex, std::integral_constant<std::size_t,
00293 level+1> >;
00294
00295     template <typename Iterator>
00296     static void apply(Visitor &&v, Complex &F, Iterator begin, Iterator end)
00297     {
00298         Container<NextEdgeID> next;
00299         std::vector<typename Complex::KeyType> cover;
00300
00301         for (auto curr = begin; curr != end; ++curr)
00302         {
00303             v.visit(F, *curr);
00304
00305             CurrSimplexID n = curr->up();
00306             F.get_cover(n, std::back_inserter(cover));
00307             for (auto a : cover)
00308             {
00309                 NextEdgeID id = F.get_edge_up(n, a);
00310                 next.insert(next.end(), id);
00311             }
00312             cover.clear();
00313         }
00314
00315         BFS_Edge_Next::apply(std::forward<Visitor>(v), F, next.begin(), next.end());
00316     }
00317 };
00318
00319
00332 };
00333
00334
00342 template <typename Visitor, typename Traits, typename Complex>

```

```

00343 struct BFS_Edge<Visitor, Traits, Complex, std::integral_constant<std::size_t, Complex::topLevel> >
00344 {
00345     static constexpr auto level = Complex::topLevel;
00346     using CurrEdgeID = typename Complex::template EdgeID<level>;
00347
00348     template <typename Iterator>
00349     static void apply(Visitor &&v, Complex &F, Iterator begin, Iterator end)
00350     {
00351         for (auto curr = begin; curr != end; ++curr)
00352         {
00353             v.visit(F, *curr);
00354         }
00355     }
00356 };
00357
00358 struct BFS_Repeat_Node_traits
00359 {
00360     template <typename T> using Container = std::vector<T>;
00361 };
00362
00363 struct BFS_NoRepeat_Node_Traits
00364 {
00365     template <typename T> using Container = NodeSet<T>;
00366 };
00367
00368 struct BFS_NoRepeat_Edge_Traits
00369 {
00370     template <typename T> using Container = NodeSet<T>;
00371     // template <typename Complex, typename SimplexID> auto node_next(Complex F,
00372     // SimplexID s);
00373 };
00374 // End namespace visitor_detail
00375
00376 template <typename Visitor, typename SimplexID>
00377 void visit_BFS_up(Visitor &&v, typename SimplexID::complex &F, SimplexID s)
00378 {
00379     namespace cvd = visitor_detail;
00380     cvd::BFS_Up_Node<Visitor, cvd::BFS_NoRepeat_Node_Traits, typename SimplexID::complex,
00381         std::integral_constant<std::size_t, SimplexID::level> >::apply(
00382         std::forward<Visitor>(v), F, &s, &s+1);
00383 }
00384
00385 template <typename Visitor, typename SimplexID>
00386 void visit_BFS_down(Visitor &&v, typename SimplexID::complex &F, SimplexID s)
00387 {
00388     namespace cvd = visitor_detail;
00389     cvd::BFS_Down_Node<Visitor, cvd::BFS_NoRepeat_Node_Traits, typename SimplexID::complex,
00390         std::integral_constant<std::size_t, SimplexID::level> >::apply(
00391         std::forward<Visitor>(v), F, &s, &s+1);
00392 }
00393
00394 template <typename Visitor, typename EdgeID>
00395 void edge_up(Visitor &&v, typename EdgeID::complex &F, EdgeID s)
00396 {
00397     namespace cvd = visitor_detail;
00398     cvd::BFS_Edge<Visitor, cvd::BFS_NoRepeat_Edge_Traits, typename EdgeID::complex,
00399         std::integral_constant<std::size_t, EdgeID::level> >::apply(
00400         std::forward<Visitor>(v), F, &s, &s+1);
00401 }
00402
00403 template <class Complex, std::size_t level, class InsertIter>
00404 void neighbors(Complex &F, typename Complex::template SimplexID<level> nid, InsertIter iter)
00405 {
00406     for (auto a : F.get_name(nid))
00407     {
00408         auto id = F.get_simplex_down(nid, a);
00409         for (auto b : F.get_cover(id))
00410         {
00411             auto nbor = F.get_simplex_up(id, b);
00412             if (nbor != nid)
00413             {
00414                 *iter++ = nbor;
00415             }
00416         }
00417     }
00418 }
00419
00420 template <class Complex, class SimplexID, class InsertIter>
00421 void neighbors(Complex &F, SimplexID nid, InsertIter iter)
00422 {
00423     neighbors<Complex, SimplexID::level, InsertIter>(F, nid, iter);
00424 }
00425
00426 template <class Complex, std::size_t level, class InsertIter>
00427 void neighbors_up(Complex &F, typename Complex::template SimplexID<level> nid, InsertIter iter)
00428 {

```

```

00523     for (auto a : F.get_cover(nid))
00524     {
00525         auto id = F.get_simplex_up(nid, a);
00526         for (auto b : F.get_name(id))
00527         {
00528             auto nbor = F.get_simplex_down(id, b);
00529             if (nbor != nid)
00530             {
00531                 *iter++ = nbor;
00532             }
00533         }
00534     }
00535 }
00536
00549 template <class Complex, class SimplexID, class InsertIter>
00550 void neighbors_up(Complex &F, SimplexID nid, InsertIter iter)
00551 {
00552     neighbors_up<Complex, SimplexID::level, InsertIter>(F, nid, iter);
00553 }
00554
00555
00556
00570 template <class Complex, std::size_t level, typename Iterator>
00571 void kneighbors_up(Complex &F, int ring, std::set<typename Complex::template SimplexID<level> > &nbors,
00572                  Iterator begin, Iterator end)
00573 {
00574     if (ring == 0)
00575     {
00576         return;
00577     }
00578     std::set<typename Complex::template SimplexID<level> > next;
00579     for (auto nid = begin; nid != end; ++nid)
00580     {
00581         for (auto a : F.get_cover(*nid))
00582         {
00583             auto id = F.get_simplex_up(*nid, a);
00584             for (auto b : F.get_name(id))
00585             {
00586                 auto nbor = F.get_simplex_down(id, b);
00587                 if (nbors.insert(nbor).second)
00588                 {
00589                     next.insert(nbor);
00590                 }
00591             }
00592         }
00593     }
00594     return kneighbors_up<Complex, level>(F, ring-1, nbors, next.begin(), next.end());
00595 }
00596
00597
00612 template <class Complex, class SimplexID>
00613 void kneighbors_up(Complex &F, SimplexID nid, int ring, std::set<SimplexID> &nbors)
00614 {
00615     nbors.insert(nid);
00616     std::set<SimplexID> next {
00617         nid
00618     };
00619     kneighbors_up<Complex, SimplexID::level>(F, ring, nbors, next.begin(), next.end());
00620     nbors.erase(nid);
00621 }
00622
00623
00637 template <class Complex, std::size_t level, typename Iterator>
00638 void kneighbors(Complex &F, int ring, std::set<typename Complex::template SimplexID<level> > &nbors,
00639               Iterator begin, Iterator end)
00640 {
00641     if (ring == 0)
00642     {
00643         return;
00644     }
00645     std::set<typename Complex::template SimplexID<level> > next;
00646     for (auto nid = begin; nid != end; ++nid)
00647     {
00648         for (auto a : F.get_name(*nid))
00649         {
00650             auto id = F.get_simplex_down(*nid, a);
00651             for (auto b : F.get_cover(id))
00652             {
00653                 auto nbor = F.get_simplex_up(id, b);
00654                 if (nbors.insert(nbor).second)
00655                 {
00656                     next.insert(nbor);
00657                 }
00658             }
00659         }
00660     }

```



```

00660     }
00661     }
00662 }
00663 }
00664 return neighbors_up<Complex, level>(F, ring-1, nbors, next.begin(), next.end());
00665 }
00666
00679 template <class Complex, class SimplexID>
00680 void neighbors(Complex &F, SimplexID nid, int ring, std::set<SimplexID> &nbors)
00681 {
00682     nbors.insert(nid);
00683     std::set<SimplexID> next {
00684         nid
00685     };
00686     neighbors<Complex, SimplexID::level>(F, ring, nbors, next.begin(), next.end());
00687     nbors.erase(nid);
00688 }
00689
00690 } // End namespace casc
00691
00692
00693 // namespace visitor_detail
00694 // {
00695 // template <typename Visitor, typename Complex, std::size_t k, std::size_t
00696 // ring>
00697 // struct Neighbors_Up_Node
00698 // {
00699 //     static constexpr auto level = k;
00700 //     using SimplexID = typename Complex::template SimplexID<level>;
00701 //
00702 //     using Neighbors_Up_Node_Next =
00703 //     Neighbors_Up_Node<Visitor, Complex, level, ring-1>;
00704 //
00705 //     template <typename Iterator>
00706 //     static void apply(Visitor&& v, Complex& F, NodeSet<SimplexID>& nodes,
00707 // Iterator begin, Iterator end)
00708 //     {
00709 //         NodeSet<SimplexID> next;
00710 //
00711 //         for(auto curr = begin; curr != end; ++curr)
00712 //         {
00713 //             if(v.visit(F, *curr))
00714 //             {
00715 //                 for(auto a : F.get_cover(*curr))
00716 //                 {
00717 //                     auto id = F.get_simplex_up(*curr,a);
00718 //                     for(auto b : F.get_name(id))
00719 //                     {
00720 //                         auto nbor = F.get_simplex_down(id,b);
00721 //                         if(nodes.insert(nbor).second)
00722 //                         {
00723 //                             next.insert(nbor);
00724 //                         }
00725 //                     }
00726 //                 }
00727 //             }
00728 //         }
00729 //
00730 //         Neighbors_Up_Node_Next::apply(std::forward<Visitor>(v), F, nodes,
00731 // next.begin(), next.end());
00732 //     }
00733 // };
00734
00735 // template <typename Visitor, typename Complex, std::size_t k>
00736 // struct Neighbors_Up_Node<Visitor, Complex, k, 0>
00737 // {
00738 //     static constexpr auto level = k;
00739 //     using SimplexID = typename Complex::template SimplexID<level>;
00740 //
00741 //     template <typename Iterator>
00742 //     static void apply(Visitor&& v, Complex& F, NodeSet<SimplexID>& nodes,
00743 // Iterator begin, Iterator end)
00744 //     {
00745 //         for(auto curr = begin; curr != end; ++curr)
00746 //         {
00747 //             v.visit(F, *curr);
00748 //         }
00749 //     }
00750 // };
00751
00752 // template <typename Visitor, typename Complex, std::size_t k, std::size_t
00753 // ring>
00754 // struct Neighbors_Down_Node
00755 // {
00756 //     static constexpr auto level = k;
00757 //     using SimplexID = typename Complex::template SimplexID<level>;
00758

```

```

00759 //      using Neighbors_Down_Node_Next = Neighbors_Down_Node<Visitor,Complex,
00760 //          level,ring-1>;
00761
00762 //      template <typename Iterator>
00763 //      static void apply(Visitor&& v, Complex& F, NodeSet<SimplexID>& nodes,
00764 // Iterator begin, Iterator end)
00765 //      {
00766 //          NodeSet<SimplexID> next;
00767
00768 //          for(auto curr = begin; curr != end; ++curr)
00769 //          {
00770 //              if(v.visit(F, *curr))
00771 //              {
00772 //                  for(auto a : F.get_name(*curr))
00773 //                  {
00774 //                      auto id = F.get_simplex_down(*curr,a);
00775 //                      for(auto b : F.get_cover(id))
00776 //                      {
00777 //                          auto nbor = F.get_simplex_up(id,b);
00778 //                          if(nodes.insert(nbor).second)
00779 //                          {
00780 //                              next.insert(nbor);
00781 //                          }
00782 //                      }
00783 //                  }
00784 //              }
00785 //          }
00786
00787 //          Neighbors_Down_Node_Next::apply(std::forward<Visitor>(v), F, nodes,
00788 // next.begin(), next.end());
00789 //      }
00790 // };
00791
00792 // template <typename Visitor, typename Complex, std::size_t k>
00793 // struct Neighbors_Down_Node<Visitor, Complex, k, 0>
00794 // {
00795 //     static constexpr auto level = k;
00796 //     using SimplexID = typename Complex::template SimplexID<level>;
00797
00798 //     template <typename Iterator>
00799 //     static void apply(Visitor&& v, Complex& F, NodeSet<SimplexID>& nodes,
00800 // Iterator begin, Iterator end)
00801 //     {
00802 //         for(auto curr = begin; curr != end; ++curr)
00803 //         {
00804 //             v.visit(F, *curr);
00805 //         }
00806 //     }
00807 // };
00808 // }
00809
00810
00811 // template <std::size_t rings, typename Visitor, typename SimplexID>
00812 // void visit_neighbors_up(Visitor&& v, typename SimplexID::complex& F,
00813 // SimplexID s)
00814 // {
00815 //     NodeSet<SimplexID> nodes{s};
00816 //     namespace cvd = visitor_detail;
00817 //     cvd::Neighbors_Up_Node<Visitor,typename
00818 // SimplexID::complex,SimplexID::level,rings>::apply(
00819 //         std::forward<Visitor>(v),F,nodes,&s,&s+1);
00820 // }
00821
00822 // template <std::size_t rings, typename Visitor, typename SimplexID>
00823 // void visit_neighbors_down(Visitor&& v, typename SimplexID::complex& F,
00824 // SimplexID s)
00825 // {
00826 //     NodeSet<SimplexID> nodes{s};
00827 //     namespace cvd = visitor_detail;
00828 //     cvd::Neighbors_Down_Node<Visitor,typename
00829 // SimplexID::complex,SimplexID::level,rings>::apply(
00830 //         std::forward<Visitor>(v),F,nodes,&s,&s+1);
00831 // }

```

## 10.5 include/casc/decimate.h File Reference

Meta-data aware decimation functions.

```

#include <typeinfo>
#include "SimplexSet.h"

```

```
#include "SimplexMap.h"
#include "CASCTraversals.h"
#include "CASCFunctions.h"
```

## Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

## Functions

- template<typename Complex>  
void `casc::perform_removal` (Complex &F, `casc::SimplexSet`< Complex > &S)  
*Remove simplex in `SimplexSet` S from complex F.*
- template<typename Complex>  
void `casc::perform_insertion` (Complex &F, typename decimation\_detail::SimplexDataSet< Complex >::type &S)  
*Insert all simplices in `SimplexSet` S into complex F*
- template<typename Complex, template< typename > class Callback>  
void `casc::run_user_callback` (Complex &F, `casc::SimplexMap`< Complex > &S, Callback< Complex > &&clbk, typename decimation\_detail::SimplexDataSet< Complex >::type &rv)  
*Run the user specified callback function.*
- template<typename Complex, typename Simplex, template< typename > class Callback>  
void `casc::decimate` (Complex &F, Simplex s, Callback< Complex > &&clbk)  
*Decimate a simplex of any dimension while considering any meta-data stores on decimated simplices.*
- template<typename Complex, typename Simplex>  
Complex::KeyType `casc::decimateFirstHalf` (Complex &F, Simplex s, `SimplexMap`< Complex > &simplexMap)  
*Given a simplex to decimate generate a pre-post mapping.*
- template<typename Complex>  
void `casc::decimateBackHalf` (Complex &F, `SimplexMap`< Complex > &simplexMap, typename decimation\_detail::SimplexDataSet< Complex >::type &rv)  
*Given a simplexMap and mapped resulting data execute the decimation.*

## 10.6 decimate.h

[Go to the documentation of this file.](#)

```
00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
00009  * modify it under the terms of the GNU Lesser General Public
00010  * License as published by the Free Software Foundation; either
00011  * version 2.1 of the License, or (at your option) any later version.
00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
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00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
```

```

00021  *
00022  * *****
00023  */
00024
00029
00030 #pragma once
00031
00032 #include <typeinfo>
00033
00034 #include "SimplexSet.h"
00035 #include "SimplexMap.h"
00036 #include "CASCTraversals.h"
00037 #include "CASCFUNCTIONS.h"
00038
00039 #if __has_cpp_attribute(maybe_unused)
00040 #define MAYBE_UNUSED [[maybe_unused]]
00041 #else
00042 #define MAYBE_UNUSED
00043 #endif
00044
00045 namespace casc
00046 {
00049 namespace decimation_detail
00050 {
00056 template <typename Complex>
00057 struct SimplexDataSet
00058 {
00060     using KeyType = typename Complex::KeyType;
00061
00068     template <std::size_t k, typename T>
00069     struct DataType
00070     {
00072         using type = std::pair<std::array<KeyType, k>, T>;
00073     };
00074
00080     template <std::size_t k>
00081     struct DataType<k, void>
00082     {
00084         using type = std::array<KeyType, k>;
00085     };
00086
00088     template <std::size_t j>
00089     using DataSet = typename DataType<j, typename Complex::template NodeData<j> >::type;
00091     using LevelIndex = typename std::make_index_sequence<Complex::numLevels>;
00093     using SimplexIDLevel = typename util::int_type_map<std::size_t,
00094                                     std::tuple, LevelIndex, DataSet>::type;
00096     template <class T> using vector = std::vector<T>;
00098     using type = typename util::type_map<SimplexIDLevel, vector>::type;
00099 };
00100
00107 template <typename Complex>
00108 struct GetCompleteNeighborhood
00109 {
00111     using SimplexSet = typename casc::SimplexSet<Complex>;
00112
00118     GetCompleteNeighborhood(SimplexSet* p) : pLevels(p) {}
00119
00125     template <std::size_t level>
00126     bool visit(Complex &, typename Complex::template SimplexID<level>)
00127     {
00128         return true;
00129     }
00130
00139     bool visit(Complex &F, typename Complex::template SimplexID<1> s)
00140     {
00141         visit_BFS_up(
00142             func_detail::SimplexAggregator<Complex>(pLevels), F, s);
00143         return false;
00144     }
00145
00146     private:
00148         SimplexSet* pLevels;
00149 };
00150
00156 template <typename Complex>
00157 struct GrabVisitor
00158 {
00160     using SimplexSet = typename casc::SimplexSet<Complex>;
00161
00168     GrabVisitor(SimplexSet* p, SimplexSet* grab) : pLevels(p), pGrab(grab) {}
00169
00170     template <std::size_t level>
00171     bool visit(Complex &, typename Complex::template SimplexID<level> s)
00172     {
00173         if (pLevels->find(s) != pLevels->template end<level>())
00174         {
00175             //std::cout << "GrabVisitor (found): " << s << std::endl;

```

```

00176         pLevels->erase(s);
00177         pGrab->insert(s);
00178         return true;
00179     }
00180     else
00181     {
00182         return false;
00183     }
00184 }
00185
00186 private:
00187     SimplexSet* pLevels;
00188     SimplexSet* pGrab;
00191 };
00192
00193 template <typename Complex, std::size_t BaseLevel>
00194 struct InnerVisitor
00195 {
00196     using SimplexSet = typename casc::SimplexSet<Complex>;
00197     using SimplexMap = typename casc::SimplexMap<Complex>;
00198     using Simplex = typename Complex::template SimplexID<BaseLevel>;
00199     using KeyType = typename Complex::KeyType;
00200
00201     InnerVisitor(SimplexSet* p, Simplex s, KeyType np, SimplexMap* rv)
00202         : pLevels(p), simplex(s), new_point(np), data(rv) {}
00203
00214     template <std::size_t OldLevel>
00215     bool visit(Complex &F, typename Complex::template SimplexID<OldLevel> s)
00216     {
00217         constexpr std::size_t NewLevel = OldLevel - BaseLevel + 1;
00218
00219         if (pLevels->find(s) != pLevels->template end<OldLevel>())
00220         {
00221             //std::cout << "InnerVisitor (found): " << s << std::endl;
00222             std::array<KeyType, OldLevel> old_name = F.get_name(s);
00223             std::array<KeyType, BaseLevel> base_name = F.get_name(simplex);
00224             using NewArrayType = std::array<KeyType, NewLevel>;
00225             NewArrayType new_name;
00226
00227             std::size_t i = 0;    // new_name
00228             std::size_t j = 0;    // old_name
00229             std::size_t k = 0;    // base_name
00230
00231             new_name[i++] = new_point;
00232
00233             // Remove base_name from old_name and append to new_name
00234             while (i < NewLevel)
00235             {
00236                 if (k >= BaseLevel) {
00237                     // append to new_name and increment
00238                     new_name[i++] = old_name[j++];
00239                     continue;
00240                 }
00241                 if (base_name[k] == old_name[j])
00242                 {
00243                     // if equivalent than skip the value
00244                     ++j; ++k;
00245                 }
00246                 else
00247                 {
00248                     // append to new_name and increment
00249                     new_name[i++] = old_name[j++];
00250                 }
00251             }
00252
00253             SimplexSet grab;
00254             visit_BFS_down(GrabVisitor<Complex>(pLevels, &grab), F, s);
00255
00256             auto &levelMap = casc::get<NewLevel>(*data);
00257             auto it = levelMap.find(new_name);
00258             if (it != levelMap.end())
00259             {
00260                 it->second.insert(grab);
00261             }
00262             else
00263             {
00264                 MAYBE_UNUSED auto ret = levelMap.insert(
00265                     std::pair<NewArrayType, SimplexSet>(new_name, grab));
00266                 assert(ret.second);
00267             }
00268         }
00269         return true;
00270     }
00271
00272 private:
00273     SimplexSet* pLevels;
00274     Simplex      simplex;

```

```

00275         KeyType      new_point;
00276         SimplexMap* data;
00277     };
00278
00279
00280     template <typename Complex>
00281     struct MainVisitor
00282     {
00283         using SimplexSet = typename casc::SimplexSet<Complex>;
00284         using SimplexMap = typename casc::SimplexMap<Complex>;
00285         using KeyType = typename Complex::KeyType;
00286
00287         MainVisitor(SimplexSet* p, KeyType np, SimplexMap* rv)
00288             : pLevels(p), new_point(np), data(rv) {}
00289
00290         template <std::size_t level>
00291         bool visit(Complex &F, typename Complex::template SimplexID<level> s)
00292         {
00293             //std::cout << "MainVisitor: " << s << std::endl;
00294             visit_BFS_up(
00295                 InnerVisitor<Complex, level>(
00296                     pLevels, s, new_point, data),
00297                 F, s);
00298             return true;
00299         }
00300
00301     private:
00302         SimplexSet* pLevels;
00303         KeyType      new_point;
00304         SimplexMap* data;
00305     };
00306
00307     template <typename Complex, template<typename> class Callback>
00308     struct RunCallback
00309     {
00310         using SimplexMap = typename casc::SimplexMap<Complex>;
00311         using SimplexSet = typename casc::SimplexSet<Complex>;
00312         using SimplexDataSet = typename SimplexDataSet<Complex>::type;
00313         using KeyType = typename Complex::KeyType;
00314         template <std::size_t level>
00315         using DataType = typename Complex::template NodeData<level>;
00316
00317
00318         template <std::size_t k, typename ReturnType>
00319         struct PerformCallback
00320         {
00321             static void apply(Complex &F, Callback<Complex> &&clbk,
00322                             SimplexDataSet &rv,
00323                             const std::array<KeyType, k> &new_name,
00324                             const SimplexSet &merged)
00325             {
00326                 ReturnType rval = clbk(F, new_name, merged);
00327                 std::get<k>(rv).push_back(std::make_pair(new_name, rval));
00328             }
00329         };
00330
00331         template <std::size_t k>
00332         struct PerformCallback<k, void>
00333         {
00334             static void apply(Complex &F, Callback<Complex> &&clbk,
00335                             SimplexDataSet &rv,
00336                             const std::array<KeyType, k> &new_name,
00337                             const SimplexSet &merged)
00338             {
00339                 clbk(F, new_name, merged);
00340                 std::get<k>(rv).push_back(new_name);
00341             }
00342         };
00343
00344
00345         template <std::size_t k>
00346         static void apply(Complex &F, SimplexMap &S,
00347                         Callback<Complex> &&clbk, SimplexDataSet &rv)
00348         {
00349             auto &levelMap = casc::get<k>(S);
00350             for (auto s : levelMap)
00351             {
00352                 PerformCallback<k, DataType<k>>::apply(F, std::forward<Callback<Complex>>(clbk),
00353                                                         rv, s.first, s.second);
00354             }
00355         }
00356     };
00357
00358     template <typename Complex>
00359     struct PerformRemoval
00360     {
00361         template <std::size_t k>

```

```

00362     static void apply(Complex &F, casc::SimplexSet<Complex> &S)
00363     {
00364         for (auto curr : casc::get<k>(S))
00365             F.remove(curr);
00366     }
00367 };
00368
00369 template <typename Complex>
00370 struct PerformInsertion {
00371     using KeyType = typename Complex::KeyType;
00372
00373     template <std::size_t k, class T>
00374     static void insert(Complex &F, std::pair<std::array<KeyType, k>, T> P)
00375     {
00376         F.insert(P.first, P.second);
00377     }
00378
00379     template <std::size_t k>
00380     static void insert(Complex &F, std::array<KeyType, k> A)
00381     {
00382         F.insert(A);
00383     }
00384
00385     template <std::size_t k>
00386     static void apply(Complex &F,
00387                       typename SimplexDataSet<Complex>::type &data)
00388     {
00389         for (auto curr : std::get<k>(data))
00390         {
00391             insert(F, curr);
00392         }
00393     }
00394 };
00395 };
00396
00397 template <typename Complex>
00398 struct DoomedHelper
00399 {
00400     template <std::size_t k>
00401     static void apply(SimplexSet<Complex> &doomed, SimplexMap<Complex> &simplexMap){
00402         auto s = casc::get<k>(simplexMap);
00403         for (auto map : s){
00404             doomed.insert(map.second);
00405         }
00406     }
00407 };
00408 } // end namespace decimation_detail
00409
00410
00411 template <typename Complex>
00412 void perform_removal(Complex &F, casc::SimplexSet<Complex> &S)
00413 {
00414     using SimplexSet = typename casc::SimplexSet<Complex>;
00415     using LevelIndex = typename SimplexSet::cRevIndex;
00416     util::int_for_each<std::size_t, LevelIndex>(
00417         decimation_detail::PerformRemoval<Complex>(), F, S);
00418 }
00419
00420 template <typename Complex>
00421 void perform_insertion(Complex &F,
00422                       typename decimation_detail::SimplexDataSet<Complex>::type &S)
00423 {
00424     using SimplexSet = typename casc::SimplexSet<Complex>;
00425     using LevelIndex = typename SimplexSet::cLevelIndex;
00426     util::int_for_each<std::size_t, LevelIndex>(
00427         decimation_detail::PerformInsertion<Complex>(), F, S);
00428 }
00429
00430 template <typename Complex, template<typename> class Callback>
00431 void run_user_callback(Complex &F,
00432                       casc::SimplexMap<Complex> &S,
00433                       Callback<Complex> &&clbk,
00434                       typename decimation_detail::SimplexDataSet<Complex>::type &rv)
00435 {
00436     using SimplexMap = typename casc::SimplexMap<Complex>;
00437     using LevelIndex = typename SimplexMap::cLevelIndex;
00438     util::int_for_each<std::size_t, LevelIndex>(
00439         decimation_detail::RunCallback<Complex, Callback>(),
00440         F, S, std::forward<Callback<Complex>>(clbk), rv);
00441 }
00442
00443 template <typename Complex, typename Simplex, template<typename> class Callback>
00444 void decimate(Complex &F, Simplex s, Callback<Complex> &&clbk)
00445 {
00446     using SimplexSet = typename casc::SimplexSet<Complex>;

```

```

00491     using SimplexMap = typename casc::SimplexMap<Complex>;
00492
00493     // Create the vertex to replace `s`
00494     typename Complex::KeyType np = F.add_vertex();
00495     SimplexSet nbhd;
00496     SimplexMap simplexMap;
00497
00498     // Get the complete neighborhood
00499     visit_BFS_down(
00500         decimation_detail::GetCompleteNeighborhood<Complex>(&nbhd),
00501         F, s);
00502
00503     SimplexSet doomed = nbhd; // Backup the neighborhood
00504     // Call MainVisitor -> InnerVisitor -> GrabVisitor sequence
00505     visit_BFS_down(
00506         decimation_detail::MainVisitor<Complex>(
00507             &nbhd, np, &simplexMap),
00508         F, s);
00509     // Run the user specified callback
00510     typename decimation_detail::SimplexDataSet<Complex>::type rv;
00511     run_user_callback(F, simplexMap, std::forward<Callback<Complex>> >(clbk), rv);
00512     perform_removal(F, doomed); // Remove simplices in the neighborhood
00513     perform_insertion(F, rv); // Insert new simplices
00514 }
00515
00526 template <typename Complex, typename Simplex>
00527 typename Complex::KeyType decimateFirstHalf(Complex &F, Simplex s, SimplexMap<Complex> &simplexMap)
00528 {
00530     using SimplexSet = typename casc::SimplexSet<Complex>;
00531
00532     // Create the vertex to replace `s`
00533     typename Complex::KeyType np = F.add_vertex();
00534     SimplexSet nbhd;
00535
00536     // Get the complete neighborhood
00537     visit_BFS_down(
00538         decimation_detail::GetCompleteNeighborhood<Complex>(&nbhd),
00539         F, s);
00540
00541     // Call MainVisitor -> InnerVisitor -> GrabVisitor sequence
00542     visit_BFS_down(
00543         decimation_detail::MainVisitor<Complex>(
00544             &nbhd, np, &simplexMap),
00545         F, s);
00546     return np;
00547 }
00548
00559 template <typename Complex>
00560 void decimateBackHalf(Complex &F, SimplexMap<Complex> &simplexMap, typename
    decimation_detail::SimplexDataSet<Complex>::type &rv){
00561
00562     SimplexSet<Complex> doomed;
00563
00564     util::int_for_each<std::size_t, typename SimplexMap<Complex>::cLevelIndex>(decimation_detail::DoomedHelper<Complex>(),
    doomed, simplexMap);
00565
00566     perform_removal(F, doomed); // Remove simplices in the neighborhood
00567     perform_insertion(F, rv); // Insert new simplices
00568 }
00569 } // end namespace casc

```

## 10.7 include/casc/index\_tracker.h File Reference

B-tree based interval tracker.

```

#include <iostream>
#include <assert.h>
#include <array>
#include <vector>
#include <cstdlib>
#include <limits>

```



## Data Structures

- struct `index_tracker::index_tracker_detail::Interval< T >`  
*Interval object represents a range.*
- struct `index_tracker::index_tracker_detail::BTreeNode< _T, _d >`  
*An array based BTree.*
- class `index_tracker::index_tracker< _T, _d >`  
*Tracker of available indices implemented as a B-tree of intervals.*

## Namespaces

- namespace `index_tracker`  
*Index tracker namespace.*
- namespace `index_tracker::index_tracker_detail`  
*B-tree internal data structures.*

## Typedefs

- template<typename Node>  
using `index_tracker::index_tracker_detail::Pointer` = typename Node::Pointer
- template<typename Node>  
using `index_tracker::index_tracker_detail::Data` = typename Node::Data
- template<typename Node>  
using `index_tracker::index_tracker_detail::Scalar` = typename Node::Scalar

## Functions

- template<typename T>  
bool `index_tracker::index_tracker_detail::operator<` (const `Interval< T >` &x, const `Interval< T >` &y)
- template<typename T>  
bool `index_tracker::index_tracker_detail::operator>` (const `Interval< T >` &x, const `Interval< T >` &y)
- template<typename T>  
bool `index_tracker::index_tracker_detail::operator<` (T x, const `Interval< T >` &y)
- template<typename T>  
bool `index_tracker::index_tracker_detail::operator>` (const `Interval< T >` &x, T y)
- template<typename T>  
bool `index_tracker::index_tracker_detail::operator<` (const `Interval< T >` &x, T y)
- template<typename T>  
bool `index_tracker::index_tracker_detail::operator>` (T x, const `Interval< T >` &y)
- template<typename T>  
bool `index_tracker::index_tracker_detail::operator==` (const `Interval< T >` &x, const `Interval< T >` &y)
- template<typename T>  
std::ostream & `index_tracker::index_tracker_detail::operator<<` (std::ostream &out, const `Interval< T >` &x)
- template<typename T>  
int `index_tracker::index_tracker_detail::merge` (`Interval< T >` &A, T x)
- template<typename Node>  
void `index_tracker::index_tracker_detail::rebalance` (Pointer< Node > head, std::size\_t i)
- template<typename Node>  
void `index_tracker::index_tracker_detail::insert_H` (Pointer< Node > head, const Data< Node > &data)
- template<typename Node>  
Pointer< Node > `index_tracker::index_tracker_detail::insert` (Pointer< Node > head, Data< Node > data)

- `template<typename Node>`  
`bool index_tracker::index_tracker_detail::get (Pointer< Node > head, Data< Node > data)`
- `template<typename Node>`  
`void index_tracker::index_tracker_detail::get_replacement (Pointer< Node > head, Data< Node > &key)`
- `template<typename Node>`  
`void index_tracker::index_tracker_detail::remove_H (Pointer< Node > head, Data< Node > data)`
- `template<typename Node>`  
`Pointer< Node > index_tracker::index_tracker_detail::remove (Pointer< Node > head, Data< Node > data)`
- `template<typename Node>`  
`void index_tracker::index_tracker_detail::fill_left (Pointer< Node > head, Data< Node > &x)`
- `template<typename Node>`  
`void index_tracker::index_tracker_detail::fill_right (Pointer< Node > head, Data< Node > &x)`
- `template<typename Node>`  
`void index_tracker::index_tracker_detail::insert_scalar_H (Pointer< Node > head, Scalar< Node > data)`
- `template<typename Node>`  
`Pointer< Node > index_tracker::index_tracker_detail::insert_scalar (Pointer< Node > head, Scalar< Node > data)`
- `template<typename Node>`  
`void index_tracker::index_tracker_detail::insert_left (Pointer< Node > head, const Data< Node > &x)`
- `template<typename Node>`  
`bool index_tracker::index_tracker_detail::remove_scalar_H (Pointer< Node > head, Scalar< Node > x)`
- `template<typename Node>`  
`bool index_tracker::index_tracker_detail::remove_scalar (Pointer< Node > &head, Scalar< Node > data)`
- `template<typename Node>`  
`Scalar< Node > index_tracker::index_tracker_detail::pop_scalar (Pointer< Node > &head)`
- `template<typename Node>`  
`void index_tracker::index_tracker_detail::destruct (Pointer< Node > head)`
- `template<typename Node>`  
`Data< Node > index_tracker::index_tracker_detail::check_order (Pointer< Node > head, Data< Node > curr)`
- `template<typename T, std::size_t d>`  
`std::ostream & index_tracker::operator<< (std::ostream &out, const index_tracker_detail::BTreeNode< T, d > *head)`

## 10.8 index\_tracker.h

[Go to the documentation of this file.](#)

```

00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
00009  * modify it under the terms of the GNU Lesser General Public
00010  * License as published by the Free Software Foundation; either
00011  * version 2.1 of the License, or (at your option) any later version.
00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA

```

```

00021  *
00022  * *****
00023  */
00024
00029
00030 #pragma once
00031
00032 #include <iostream>
00033 #include <assert.h>
00034 #include <array>
00035 #include <vector>
00036 #include <cstdlib>
00037 #include <limits>
00038
00039
00041 namespace index_tracker
00042 {
00044     namespace index_tracker_detail {
00045
00046         template <typename T>
00052         struct Interval
00053         {
00054             {
00056                 Interval() : _a(0), _b(0) {}
00058                 Interval(T a) : _a(a), _b(a+1) {}
00060                 Interval(T a, T b) : _a(a), _b(b) { assert(a <= b); }
00062                 Interval(const Interval<T>& rhs) : _a(rhs._a), _b(rhs._b) {}
00063
00071                 Interval& operator=(const Interval& rhs)
00072                 {
00073                     _a = rhs._a;
00074                     _b = rhs._b;
00075                     return *this;
00076                 }
00077
00079                 bool has(T x) { return _a <= x && x < _b; }
00080
00082                 T lower() const { return _a; }
00084                 T upper() const { return _b; }
00085
00087                 T& lower() { return _a; }
00089                 T& upper() { return _b; }
00090
00092                 std::size_t size() { return _b - _a; }
00093
00094             private:
00095                 T _a;
00096                 T _b;
00097             };
00098
00099             template <typename T>
00100             bool operator<(const Interval<T>& x, const Interval<T>& y)
00101             {
00102                 return x.upper() <= y.lower();
00103             }
00104
00105             template <typename T>
00106             bool operator>(const Interval<T>& x, const Interval<T>& y)
00107             {
00108                 return x.lower() >= y.upper();
00109             }
00110
00111             template <typename T>
00112             bool operator<(T x, const Interval<T>& y)
00113             {
00114                 return x < y.lower();
00115             }
00116
00117             template <typename T>
00118             bool operator>(const Interval<T>& x, T y)
00119             {
00120                 return x.lower() > y;
00121             }
00122
00123             template <typename T>
00124             bool operator<(const Interval<T>& x, T y)
00125             {
00126                 return x.upper() <= y;
00127             }
00128
00129             template <typename T>
00130             bool operator>(T x, const Interval<T>& y)
00131             {
00132                 return x >= y.upper();
00133             }
00134
00135             template <typename T>

```

```

00136     bool operator==(const Interval<T>& x, const Interval<T>& y)
00137     {
00138         return (x.lower() == y.lower()) && (x.upper() == y.upper());
00139     }
00140
00141     template <typename T>
00142     std::ostream& operator<<(std::ostream& out, const Interval<T>& x)
00143     {
00144         out << "[" << x.lower() << "~" << x.upper() << "]";
00145         return out;
00146     }
00147
00148     template <typename T>
00149     int merge(Interval<T>& A, T x)
00150     {
00151         // If x isn't the next lower value return 0
00152         if(x + 1 < A.lower())
00153             return 0;
00154         else if(x + 1 == A.lower())
00155         {
00156             // if x is the next lowest value assign to lower
00157             A.lower() = x;
00158             return 1;
00159         }
00160         else if(A.lower() <= x && x < A.upper()) // x is in range already
00161             return 2;
00162         else if(A.upper() == x)
00163         {
00164             // x is the next higher assign upper
00165             A.upper() = x + 1;
00166             return 3;
00167         }
00168         else if(A.upper() < x)
00169             // x isn't next after this range return 4
00170             return 4;
00171         else
00172             return 5; // Something undefined happened.
00173     }
00174
00175     template <typename _T, std::size_t _d>
00176     struct BTreeNode
00177     {
00178         static constexpr std::size_t d = _d;
00179         static constexpr std::size_t N = 2*d+1;
00180         using Scalar = _T;
00181         using Data = Interval<Scalar>;
00182         using Pointer = BTreeNode*;
00183
00184         BTreeNode() {}
00185         BTreeNode(const Data& t)
00186             : k(1), next{nullptr, nullptr}
00187         {
00188             data[0] = t;
00189         }
00190
00191         template <typename Iter>
00192         BTreeNode(Iter begin, Iter end)
00193         {
00194             k = 0;
00195             while(begin != end)
00196             {
00197                 next[k] = nullptr;
00198                 data[k++] = *begin++;
00199             }
00200             next[k] = nullptr;
00201         }
00202
00203         std::size_t k;
00204         std::array<Data, N> data;
00205         std::array<Pointer, N+1> next;
00206     };
00207
00208     template <typename Node> using Pointer = typename Node::Pointer;
00209     template <typename Node> using Data = typename Node::Data;
00210     template <typename Node> using Scalar = typename Node::Scalar;
00211
00212     template <typename Node>
00213     void rebalance(Pointer<Node> head, std::size_t i)
00214     {
00215         Pointer<Node> curr = head->next[i];
00216
00217         if(curr->k == Node::N)
00218         {
00219             // Pointer<Node> left = curr; // UNUSED

```

```

00229     Pointer<Node> right = new Node(curr->data.begin() + Node::d + 1, curr->data.end());
00230     curr->k = Node::d;
00231
00232     if(curr->next[0] == nullptr)
00233     {
00234         right->next[0] = nullptr;
00235     }
00236     else
00237     {
00238         for(std::size_t i = 0; i <= Node::d; ++i)
00239         {
00240             right->next[i] = curr->next[Node::d + i + 1];
00241         }
00242     }
00243
00244     Data<Node> up = curr->data[Node::d];
00245
00246     for(std::size_t j = head->k; j > i; --j)
00247     {
00248         head->data[j] = head->data[j-1];
00249         head->next[j+1] = head->next[j];
00250     }
00251     head->data[i] = up;
00252     head->next[i+1] = right;
00253     ++(head->k);
00254 }
00255 else if(curr->k < Node::d)
00256 {
00257     if(i > 0 && head->next[i-1]->k > Node::d)
00258     {
00259         Pointer<Node> left = head->next[i-1];
00260         Pointer<Node> right = head->next[i];
00261
00262         if(right->next[0] != nullptr)
00263             right->next[right->k + 1] = right->next[right->k];
00264         for(std::size_t j = right->k; j > 0; --j)
00265         {
00266             right->data[j] = right->data[j-1];
00267             if(left->next[0] != nullptr)
00268                 right->next[j] = right->next[j-1];
00269         }
00270         right->data[0] = head->data[i-1];
00271         if(left->next[0] != nullptr)
00272             right->next[0] = left->next[left->k];
00273         ++(right->k);
00274
00275         head->data[i-1] = left->data[left->k-1];
00276
00277         --(left->k);
00278
00279         //      std::cout << "Rotate Right" << std::endl;
00280     }
00281     else if(i < head->k && head->next[i+1]->k > Node::d)
00282     {
00283         Pointer<Node> left = head->next[i];
00284         Pointer<Node> right = head->next[i+1];
00285
00286         left->data[left->k] = head->data[i];
00287         ++(left->k);
00288         if(left->next[0] != nullptr)
00289             left->next[left->k] = right->next[0];
00290
00291         head->data[i] = right->data[0];
00292         for(std::size_t j = 0; j < right->k - 1; ++j)
00293         {
00294             right->data[j] = right->data[j+1];
00295             if(right->next[0] != nullptr)
00296                 right->next[j] = right->next[j+1];
00297         }
00298         --(right->k);
00299         if(right->next[0] != nullptr)
00300             right->next[right->k] = right->next[right->k + 1];
00301
00302         //      std::cout << "Rotate Left" << std::endl;
00303     }
00304     else
00305     {
00306         if(i < head->k)
00307         {
00308             Pointer<Node> left = head->next[i];
00309             Pointer<Node> right = head->next[i+1];
00310
00311             left->data[(left->k)++] = head->data[i];
00312             for(std::size_t j = 0; j < right->k; ++j)
00313             {
00314                 left->data[left->k] = right->data[j];
00315                 if(left->next[0] != nullptr)

```

```

00316         left->next[left->k] = right->next[j];
00317         ++(left->k);
00318     }
00319     if(left->next[0] != nullptr)
00320         left->next[left->k] = right->next[right->k];
00321
00322     delete right;
00323
00324     --(head->k);
00325     for(std::size_t j = i; j < head->k; ++j)
00326     {
00327         head->data[j] = head->data[j+1];
00328         head->next[j+1] = head->next[j+2];
00329     }
00330
00331     else
00332     {
00333         Pointer<Node> left = head->next[i-1];
00334         Pointer<Node> right = head->next[i];
00335
00336         left->data[left->k] = head->data[i-1];
00337         ++(left->k);
00338         for(std::size_t j = 0; j < right->k; ++j)
00339         {
00340             left->data[left->k] = right->data[j];
00341             if(left->next[0] != nullptr)
00342                 left->next[left->k] = right->next[j];
00343             ++(left->k);
00344         }
00345         if(left->next[0] != nullptr)
00346             left->next[left->k] = right->next[right->k];
00347
00348         delete right;
00349         --(head->k);
00350     }
00351 }
00352
00353 }
00354
00355 template <typename Node>
00356 void insert_H(Pointer<Node> head, const Data<Node>& data)
00357 {
00358     if(head->next[0] == nullptr)
00359     {
00360         const auto k = head->k;
00361
00362         std::size_t i = 0;
00363         while(i < k && head->data[i] < data)
00364         {
00365             ++i;
00366         }
00367         for(std::size_t j = k; j > i; --j)
00368         {
00369             head->data[j] = head->data[j-1];
00370         }
00371         head->data[i] = data;
00372         head->k = k+1;
00373     }
00374     else
00375     {
00376         const auto k = head->k;
00377
00378         std::size_t i = 0;
00379         while(i < k && head->data[i] < data)
00380             ++i;
00381
00382         insert_H<Node>(head->next[i], data);
00383         rebalance<Node>(head, i);
00384     }
00385 }
00386
00387 template <typename Node>
00388 Pointer<Node> insert(Pointer<Node> head, Data<Node> data)
00389 {
00390     if(head == nullptr)
00391     {
00392         return new Node(data);
00393     }
00394     else
00395     {
00396         insert_H<Node>(head, data);
00397         if(head->k == Node::N)
00398         {
00399             Pointer<Node> nn = new Node();
00400             nn->k = 0;
00401             nn->next[0] = head;
00402             rebalance<Node>(nn, 0);

```

```

00403         return nn;
00404     }
00405     else
00406     {
00407         return head;
00408     }
00409 }
00410 }
00411
00412 template <typename Node>
00413 bool get(Pointer<Node> head, Data<Node> data)
00414 {
00415     if(head->next[0] == nullptr)
00416     {
00417         for(std::size_t i = 0; i < head->k; ++i)
00418         {
00419             if(data == head->data[i])
00420             {
00421                 return true;
00422             }
00423         }
00424         return false;
00425     }
00426     else
00427     {
00428         for(std::size_t i = 0; i < head->k; ++i)
00429         {
00430             if(data < head->data[i])
00431             {
00432                 return get<Node>(head->next[i], data);
00433             }
00434             else if(data == head->data[i])
00435             {
00436                 return true;
00437             }
00438         }
00439         return get<Node>(head->next[head->k], data);
00440     }
00441 }
00442
00443
00444
00445 template <typename Node>
00446 void get_replacement(Pointer<Node> head, Data<Node>& key)
00447 {
00448     if(head->next[0] == nullptr)
00449     {
00450         key = head->data[head->k-1];
00451         --(head->k);
00452     }
00453     else
00454     {
00455         get_replacement<Node>(head->next[head->k], key);
00456         rebalance<Node>(head, head->k);
00457     }
00458 }
00459
00460 template <typename Node>
00461 void remove_H(Pointer<Node> head, Data<Node> data)
00462 {
00463     if(head->next[0] == nullptr)
00464     {
00465         for(std::size_t i = 0; i < head->k; ++i)
00466         {
00467             if(data == head->data[i])
00468             {
00469                 for(std::size_t j = i+1; j < head->k; ++j)
00470                 {
00471                     head->data[j-1] = head->data[j];
00472                 }
00473                 --(head->k);
00474                 break;
00475             }
00476         }
00477     }
00478     else
00479     {
00480         for(std::size_t i = 0; i < head->k; ++i)
00481         {
00482             if(data < head->data[i])
00483             {
00484                 remove_H<Node>(head->next[i], data);
00485                 rebalance<Node>(head, i);
00486                 return;
00487             }
00488             else if(data == head->data[i])
00489             {

```

```

00490         get_replacement<Node>(head->next[i], head->data[i]);
00491         rebalance<Node>(head, i);
00492         return;
00493     }
00494 }
00495 remove_H<Node>(head->next[head->k], data);
00496 rebalance<Node>(head, head->k);
00497 }
00498 }
00499
00500 template <typename Node>
00501 Pointer<Node> remove(Pointer<Node> head, Data<Node> data)
00502 {
00503     remove_H<Node>(head, data);
00504
00505     if(head->k == 0)
00506     {
00507         Pointer<Node> rval = head->next[0];
00508         delete head;
00509         return rval;
00510     }
00511     else
00512     {
00513         return head;
00514     }
00515 }
00516
00517
00518 template <typename Node>
00519 void fill_left(Pointer<Node> head, Data<Node>& x)
00520 {
00521     if(head->next[0] == nullptr)
00522     {
00523         Data<Node>& left = head->data[head->k-1];
00524         if(left.upper() == x.lower())
00525         {
00526             x.lower() = left.lower();
00527             --(head->k);
00528         }
00529     }
00530     else
00531     {
00532         fill_left<Node>(head->next[head->k], x);
00533         rebalance<Node>(head, head->k);
00534     }
00535 }
00536
00537
00538 template <typename Node>
00539 void fill_right(Pointer<Node> head, Data<Node>& x)
00540 {
00541     if(head->next[0] == nullptr)
00542     {
00543         Data<Node>& right = head->data[0];
00544         if(right.lower() == x.upper())
00545         {
00546             x.upper() = right.upper();
00547             --(head->k);
00548             for(std::size_t i = 0; i < head->k; ++i)
00549             {
00550                 head->data[i] = head->data[i+1];
00551             }
00552         }
00553     }
00554     else
00555     {
00556         fill_right<Node>(head->next[0], x);
00557         rebalance<Node>(head, 0);
00558     }
00559 }
00560
00561
00562 template <typename Node>
00563 void insert_scalar_H(Pointer<Node> head, Scalar<Node> data)
00564 {
00565     // If the
00566     if(head->next[0] == nullptr)
00567     {
00568         const auto k = head->k;
00569
00570         std::size_t i;
00571         for(i = 0; i < k; ++i)
00572         {
00573             Data<Node>& A = head->data[i];
00574             Scalar<Node> x = data;
00575
00576             if(x + 1 < A.lower())

```



```

00577         {
00578             for(std::size_t j = k; j > i; --j)
00579             {
00580                 head->data[j] = head->data[j-1];
00581             }
00582             head->data[i] = data;
00583             ++(head->k);
00584             return;
00585         }
00586         else if(x + 1 == A.lower())
00587         {
00588             A.lower() = x;
00589             return;
00590         }
00591         else if(A.lower() <= x && x < A.upper())
00592         {
00593             return;
00594         }
00595         else if(A.upper() == x)
00596         {
00597             if(i + 1 < k)
00598             {
00599                 Data<Node>& B = head->data[i+1];
00600                 if(x + 1 == B.lower())
00601                 {
00602                     A.upper() = B.upper();
00603                     for(std::size_t j = i+1; j < k-1; ++j)
00604                     {
00605                         head->data[j] = head->data[j+1];
00606                     }
00607                     --(head->k);
00608                 }
00609                 else
00610                 {
00611                     A.upper() = x + 1;
00612                 }
00613             }
00614             else
00615             {
00616                 A.upper() = x + 1;
00617             }
00618             return;
00619         }
00620     }
00621     head->data[i] = data;
00622     ++(head->k);
00623 }
00624 else
00625 {
00626     const auto k = head->k;
00627
00628     std::size_t i;
00629     for(i = 0; i < k; ++i)
00630     {
00631         Data<Node>& A = head->data[i];
00632         Scalar<Node> x = data;
00633
00634         if(x + 1 < A.lower())
00635         {
00636             insert_scalar_H<Node>(head->next[i], data);
00637             rebalance<Node>(head, i);
00638             return;
00639         }
00640         else if(x + 1 == A.lower())
00641         {
00642             A.lower() = x;
00643             fill_left<Node>(head->next[i], A);
00644             rebalance<Node>(head, i);
00645             return;
00646         }
00647         else if(A.lower() <= x && x < A.upper())
00648         {
00649             return;
00650         }
00651         else if(A.upper() == x)
00652         {
00653             A.upper() = x + 1;
00654             fill_right<Node>(head->next[i+1], A);
00655             rebalance<Node>(head, i+1);
00656             return;
00657         }
00658     }
00659     insert_scalar_H<Node>(head->next[i], data);
00660     rebalance<Node>(head, i);
00661 }
00662 }
00663

```

```

00664     template <typename Node>
00665     Pointer<Node> insert_scalar(Pointer<Node> head, Scalar<Node> data)
00666     {
00667         if(head == nullptr)
00668         {
00669             return new Node(data);
00670         }
00671         else
00672         {
00673             insert_scalar_H<Node>(head, data);
00674             if(head->k == Node::N)
00675             {
00676                 Pointer<Node> nn = new Node();
00677                 nn->k = 0;
00678                 nn->next[0] = head;
00679                 rebalance<Node>(nn, 0);
00680                 return nn;
00681             }
00682             else if(head->k == 0)
00683             {
00684                 Pointer<Node> rval = head->next[0];
00685                 delete head;
00686                 return rval;
00687             }
00688             else
00689             {
00690                 return head;
00691             }
00692         }
00693     }
00694
00695     template <typename Node>
00696     void insert_left(Pointer<Node> head, const Data<Node>& x)
00697     {
00698         if(head->next[0] == nullptr)
00699         {
00700             head->data[head->k] = x;
00701             ++(head->k);
00702         }
00703         else
00704         {
00705             insert_left<Node>(head->next[head->k], x);
00706             rebalance<Node>(head, head->k);
00707         }
00708     }
00709
00710
00711     template <typename Node>
00712     bool remove_scalar_H(Pointer<Node> head, Scalar<Node> x)
00713     {
00714         if(head->next[0] == nullptr)
00715         {
00716             const auto k = head->k;
00717
00718             std::size_t i;
00719             for(i = 0; i < k; ++i)
00720             {
00721                 Data<Node>& A = head->data[i];
00722
00723                 if(x < A.lower())
00724                 {
00725                     // std::cout << "if(x < A.lower())" << std::endl;
00726                     return false;
00727                 }
00728                 else if(x == A.lower())
00729                 {
00730                     // std::cout << "if(x == A.lower())" << std::endl;
00731                     if(x + 1 == A.upper())
00732                     {
00733                         // std::cout << "if(x + 1 == A.upper())" << std::endl;
00734                         --(head->k);
00735                         for(std::size_t j = i; j < head->k; ++j)
00736                         {
00737                             head->data[j] = head->data[j+1];
00738                         }
00739                         return true;
00740                     }
00741                     A.lower() = x + 1;
00742                     return true;
00743                 }
00744                 else if(*A.lower() < x &&* / x + 1 < A.upper())
00745                 {
00746                     // std::cout << "x + 1 < A.upper()" << std::endl;
00747                     for(std::size_t j = head->k; j > i; --j)
00748                     {
00749                         head->data[j] = head->data[j-1];
00750                     }

```

```

00751         ++(head->k);
00752         A.upper() = x;
00753         head->data[i+1].lower() = x + 1;
00754         return true;
00755     }
00756     else if(x + 1 == A.upper())
00757     {
00758         //         std::cout << "x + 1 < A.upper()" << std::endl;
00759         A.upper() = x;
00760         return true;
00761     }
00762 }
00763 return false;
00764 }
00765 else
00766 {
00767     const auto k = head->k;
00768
00769     std::size_t i;
00770     for(i = 0; i < k; ++i)
00771     {
00772         Data<Node>& A = head->data[i];
00773
00774         if(x < A.lower())
00775         {
00776             bool rval = remove_scalar_H<Node>(head->next[i], x);
00777             rebalance<Node>(head, i);
00778             return rval;
00779         }
00780         else if(x == A.lower())
00781         {
00782             if(x + 1 == A.upper())
00783             {
00784                 get_replacement<Node>(head->next[i], A);
00785                 rebalance<Node>(head, i);
00786                 return true;
00787             }
00788             A.lower() = x + 1;
00789             return true;
00790         }
00791         else if(/*A.lower() < x &&*/ x + 1 < A.upper())
00792         {
00793             Data<Node> B(A.lower(), x);
00794             A.lower() = x + 1;
00795             insert_left<Node>(head->next[i], B);
00796             rebalance<Node>(head, i);
00797             return true;
00798         }
00799         else if(x + 1 == A.upper())
00800         {
00801             A.upper() = x;
00802             return true;
00803         }
00804     }
00805     bool rval = remove_scalar_H<Node>(head->next[i], x);
00806     rebalance<Node>(head, i);
00807     return rval;
00808 }
00809 }
00810
00811 template <typename Node>
00812 bool remove_scalar(Pointer<Node>& head, Scalar<Node> data)
00813 {
00814     if(head == nullptr)
00815     {
00816         return false;
00817     }
00818
00819     bool rval = remove_scalar_H<Node>(head, data);
00820
00821     if(head->k == Node::N)
00822     {
00823         Pointer<Node> nn = new Node();
00824         nn->k = 0;
00825         nn->next[0] = head;
00826         rebalance<Node>(nn, 0);
00827         head = nn;
00828     }
00829     else if(head->k == 0)
00830     {
00831         Pointer<Node> tmp = head;
00832         head = head->next[0];
00833         delete tmp;
00834     }
00835
00836     return rval;
00837 }

```

```

00838
00839     template <typename Node>
00840     Scalar<Node> pop_scalar(Pointer<Node>& head)
00841     {
00842         if(head)
00843         {
00844             Scalar<Node> x = head->data[0].lower();
00845             remove_scalar<Node>(head, x);
00846             return x;
00847         }
00848         exit(-1);
00849     }
00850
00851     template <typename Node>
00852     void destruct(Pointer<Node> head)
00853     {
00854         if(head == nullptr)
00855         {
00856             return;
00857         }
00858         else
00859         {
00860             if(head->next[0] != nullptr)
00861             {
00862                 for(std::size_t i = 0; i < head->k; ++i)
00863                 {
00864                     destruct<Node>(head->next[i]);
00865                 }
00866                 delete head;
00867             }
00868         }
00869     }
00870
00871
00872     template <typename Node>
00873     Data<Node> check_order(Pointer<Node> head, Data<Node> curr)
00874     {
00875         if(head != nullptr)
00876         {
00877             if(head->next[0] == nullptr)
00878             {
00879                 for(std::size_t i = 0; i < head->k; ++i)
00880                 {
00881                     if(curr > head->data[i])
00882                     {
00883                         std::cout << "ORDER WRONG!!!  --  " << curr << " > " << head->data[i] <<
std::endl;
00884                         exit(1);
00885                     }
00886                     curr = head->data[i];
00887                 }
00888             }
00889             else
00890             {
00891                 for(std::size_t i = 0; i < head->k; ++i)
00892                 {
00893                     curr = check_order<Node>(head->next[i], curr);
00894                     if(curr > head->data[i])
00895                     {
00896                         std::cout << "ORDER WRONG!!!  --  " << curr << " > " << head->data[i] <<
std::endl;
00897                         exit(1);
00898                     }
00899                     curr = head->data[i];
00900                 }
00901                 curr = check_order<Node>(head->next[head->k], curr);
00902             }
00903         }
00904         return curr;
00905     }
00906 } // End namespace index_tracker_detail
00907
00908 template <typename T, std::size_t d>
00909 std::ostream& operator<<(std::ostream& out, const index_tracker_detail::BTreeNode<T,d>* head)
00910 {
00911     if(head == nullptr)
00912     {
00913         out << "[nil]";
00914     }
00915     else
00916     {
00917         out << "[";
00918         for(std::size_t i = 0; i < head->k; ++i)
00919         {
00920             if(head->next[0] != nullptr)
00921                 out << head->next[i] << " ";
00922             out << head->data[i] << " ";

```

```

00923     }
00924     if(head->next[0] != nullptr)
00925         out << head->next[head->k];
00926     out << "J";
00927 }
00928 return out;
00929 }
00930
00937 template <typename _T, std::size_t _d = 16>
00938 class index_tracker
00939 {
00940 public:
00942     using Node = index_tracker_detail::BTreeNode<_T, _d>;
00943     using T = _T;
00944     constexpr static std::size_t d = _d;
00945
00946     index_tracker()
00947         : head(new Node(index_tracker_detail::Interval<T>(0, std::numeric_limits<T>::max()))
00948     {
00949     ~index_tracker()
00950     {
00951         index_tracker_detail::destruct<Node>(head);
00952     }
00953
00954     void insert(T x)
00955     {
00956         head = index_tracker_detail::insert_scalar<Node>(head, x);
00957     }
00958
00959     index_tracker_detail::Scalar<Node> pop()
00960     {
00961         auto x = index_tracker_detail::pop_scalar<Node>(head);
00962         return x;
00963     }
00964
00965     void remove(index_tracker_detail::Scalar<Node> x)
00966     {
00967         index_tracker_detail::remove_scalar<Node>(head, x);
00968     }
00969
00970     bool empty() const
00971     {
00972         return head == nullptr;
00973     }
00974
00975     friend std::ostream& operator<<(std::ostream& out, const index_tracker& x)
00976     {
00977         out << x.head;
00978         return out;
00979     }
00980
00981 private:
00982     index_tracker_detail::Pointer<Node> head;
00983 };
00984 // end namespace index_tracker

```

## 10.9 include/casc/Orientable.h File Reference

Data type for orientability.

```

#include <iostream>
#include <queue>
#include <set>

```

### Data Structures

- struct [casc::Orientable](#)  
Class representing the orientation.

## Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

## Functions

- `template<typename Complex>`  
`void casc::init_orientation (Complex &F)`  
*Initialize the partial ordering of the simplex edges.*
- `template<typename Complex>`  
`void casc::clear_orientation (Complex &F)`  
*Clear the orientation of the facets.*
- `template<typename Complex>`  
`std::tuple< int, bool, bool > casc::compute_orientation (Complex &F)`  
*Initializes and calculates the orientation of a *simplicial\_complex*.*
- `template<typename Complex>`  
`std::tuple< int, bool, bool > casc::check_orientation (Complex &F)`  
*Checks for self consistent orientation and fill in missing orientations.*

## 10.10 Orientable.h

[Go to the documentation of this file.](#)

```

00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
00009  * modify it under the terms of the GNU Lesser General Public
00010  * License as published by the Free Software Foundation; either
00011  * version 2.1 of the License, or (at your option) any later version.
00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00029
00030
00031 #pragma once
00032
00033 #include <iostream>
00034 #include <queue>
00035 #include <set>
00036
00037
00038 namespace casc{
00042 struct Orientable {
00044     int orientation;
00045 };
00046
00049 namespace orientation_detail{
00050
00051 template <class Complex, class SizeT >
00052 struct init_orientation_helper {};
00053
00054 template <class Complex, std::size_t k >
00055 struct init_orientation_helper<Complex, std::integral_constant<std::size_t, k>

```

```

00056 {
00057     static void f(Complex& F)
00058     {
00059         for(auto curr : F.template get_level_id<k>())
00060         {
00061             for(auto a : F.get_cover(curr))
00062             {
00063                 int orient = 1;
00064                 for(auto b : F.get_name(curr))
00065                 {
00066                     // Count the number of indices > name
00067                     if(a > b)
00068                     {
00069                         orient *= -1;
00070                     }
00071                     else
00072                     {
00073                         break;
00074                     }
00075                 }
00076                 (*F.get_edge_up(curr,a)).orientation = orient;
00077             }
00078         }
00079         init_orientation_helper<Complex, std::integral_constant<std::size_t, k+1>::f(F);
00080     }
00081 };
00082 };
00083
00084 template <typename Complex>
00085 struct init_orientation_helper<Complex, std::integral_constant<std::size_t, Complex::topLevel>
00086 {
00087     static void f(Complex&) {}
00088 };
00089 // end namespace orientation_detail
00090
00091 template <typename Complex>
00092 void init_orientation(Complex& F)
00093 {
00094     orientation_detail::init_orientation_helper<Complex, std::integral_constant<std::size_t, 0>::f(F);
00095 }
00096
00097 template <typename Complex>
00098 void clear_orientation(Complex& F)
00099 {
00100     // clear orientation
00101     for(auto& curr : F.template get_level<Complex::topLevel>())
00102     {
00103         curr.orientation = 0;
00104     }
00105 }
00106
00107 // TODO: Implement this as a disjoint set operation during insertion (2)
00108 template <typename Complex>
00109 std::tuple<int, bool, bool> compute_orientation(Complex& F)
00110 {
00111     init_orientation(F);
00112     clear_orientation(F);
00113     return check_orientation(F);
00114 }
00115
00116 template <typename Complex>
00117 std::tuple<int, bool, bool> check_orientation(Complex& F)
00118 {
00119     // compute orientation
00120     constexpr std::size_t k = Complex::topLevel - 1;
00121
00122     std::deque<typename Complex::template SimplexID<k>> frontier;
00123     std::set<typename Complex::template SimplexID<k>> visited;
00124     int connected_components = 0;
00125     bool orientable = true;
00126     bool psuedo_manifold = true;
00127     for(auto outer : F.template get_level_id<k>())
00128     {
00129         if(visited.find(outer) == visited.end())
00130         {
00131             ++connected_components;
00132             frontier.push_back(outer);
00133             while(!frontier.empty())
00134             {
00135                 typename Complex::template SimplexID<k> curr = frontier.front();
00136                 if(visited.find(curr) == visited.end())
00137                 {
00138                     visited.insert(curr);
00139                     auto w = F.get_cover(curr);

```

```

00185
00186         if(w.size() == 1)
00187         {
00188             // w is a boundary
00189             //std::cout << curr << ":" << w[0] << " ~ Boundary" << std::endl;
00190         }
00191         else if(w.size() == 2)
00192         {
00193             auto& edge0 = *F.get_edge_up(curr, w[0]);
00194             auto& edge1 = *F.get_edge_up(curr, w[1]);
00195
00196             auto& node0 = *F.get_simplex_up(curr, w[0]);
00197             auto& node1 = *F.get_simplex_up(curr, w[1]);
00198
00199             // If node0 doesn't have an orientation yet... Assign one
00200             if(node0.orientation == 0)
00201             {
00202                 if(node1.orientation == 0)
00203                 {
00204                     node0.orientation = -1;
00205                     node1.orientation = -edge1.orientation * edge0.orientation *
node0.orientation;
00206                 }
00207                 else
00208                 {
00209                     node0.orientation = -edge0.orientation * edge1.orientation *
node1.orientation;
00210                 }
00211             }
00212             else
00213             {
00214                 // if node1 doesn't have an orientation...
00215                 if(node1.orientation == 0)
00216                 {
00217                     node1.orientation = -edge1.orientation * edge0.orientation *
node0.orientation;
00218                 }
00219                 else
00220                 {
00221                     // Check if the orientations are consistent
00222                     if(edge0.orientation*node0.orientation +
edge1.orientation*node1.orientation != 0)
00223                     {
00224                         orientable = false;
00225                         // std::cout << "++++" << std::endl;
00226                         // std::cout << edge0.orientation << " : " << node0.orientation <<
std::endl;
00227                         // std::cout << edge1.orientation << " : " << node1.orientation <<
std::endl;
00228
00229                         // std::cout << " : "
00230                         // << edge0.orientation*node0.orientation +
edge1.orientation*node1.orientation
00231                         // << std::endl;
00232                         // std::cout << "-----"
00233                         // << std::endl;
00234                         // std::cout << "Non-Orientable: "
00235                         // << edge0.orientation*node0.orientation +
edge1.orientation*node1.orientation
00236                         // << std::endl;
00237                     }
00238                 }
00239             }
00240             neighbors_up(F, curr, std::back_inserter(frontier));
00241         }
00242         else
00243         {
00244             // W.size() != 1 or 2
00245             psuedo_manifold = false;
00246         }
00247     }
00248     frontier.pop_front();
00249 }
00250 }
00251 }
00252 return std::make_tuple(connected_components, orientable, psuedo_manifold);
00253 }
00254 } // end namespace casc

```

## 10.11 include/casc/SimplexMap.h File Reference

SimplexMap data structure and associated convenience functions.



```
#include <array>
#include <map>
#include "util.h"
#include "stringutil.h"
```

## Data Structures

- struct `casc::SimplexMap< Complex >`  
*A multimap to represent a map of simplex indices to a set of simplices.*

## Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

## Functions

- template<std::size\_t k, typename Complex>  
static auto & `casc::get (SimplexMap< Complex > &S)`  
*Get the map for a simplex dimension.*
- template<std::size\_t k, typename Complex>  
static auto & `casc::get (const SimplexMap< Complex > &S)`  
*This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.*

# 10.12 SimplexMap.h

[Go to the documentation of this file.](#)

```
00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
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00011  * version 2.1 of the License, or (at your option) any later version.
00012  *
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00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00029
00030 #pragma once
00031
00032 #include <array>
00033 #include <map>
00034 #include "util.h"
00035 #include "stringutil.h"
00036
00037 namespace casc
```

```

00038 {
00039
00046 template <typename Complex>
00047 struct SimplexMap
00048 {
00050     template <std::size_t j>
00051     using SimplexID = typename Complex::template SimplexID<j>;
00053     using LevelIndex = typename Complex::LevelIndex;
00055     using cLevelIndex = typename util::remove_first_val<std::size_t,
00056                                                         LevelIndex>::type;
00058     using RevIndex = typename util::reverse_sequence<std::size_t,
00059                                                         LevelIndex>::type;
00061     using cRevIndex = typename util::reverse_sequence<std::size_t,
00062                                                         cLevelIndex>::type;
00064     using type_this = SimplexMap<Complex>;
00065
00069     SimplexMap() {};
00070
00071     // TODO: Put in convenience functions for easy accession etc... (0)
00079     template <std::size_t k>
00080     inline auto &get()
00081     {
00082         return std::get<k>(tupleMap);
00083     }
00084
00088     template <std::size_t k>
00089     inline auto &get() const
00090     {
00091         return std::get<k>(tupleMap);
00092     }
00093
00102     friend std::ostream &operator<<(std::ostream &output, const SimplexMap<Complex> &S)
00103     {
00104         output << "SimplexMap(";
00105         util::int_for_each<std::size_t, LevelIndex>(PrintHelper(),
00106                                                         output, S);
00107         output << ")";
00108         return output;
00109     }
00110
00111     private:
00115         struct PrintHelper
00116         {
00125             template <std::size_t k>
00126             static void apply(std::ostream &output, const SimplexMap<Complex> &S)
00127             {
00128                 output << "[l=" << k;
00129                 auto s = std::get<k>(S.tupleMap);
00130                 for (auto simplex : s)
00131                 {
00132                     output << ", " << to_string(simplex.first) << ":" << simplex.second;
00133                 }
00134                 output << "]";
00135             }
00136         };
00137
00139         template <std::size_t k> using array = std::array<typename Complex::KeyType, k>;
00141         using ArrayLevel = typename
00143         util::int_type_map<std::size_t, std::tuple, LevelIndex, array>::type;
00144         template <class T> using map = std::map<T, SimplexSet<Complex> >;
00145         typename util::type_map<ArrayLevel, map>::type tupleMap;
00146     };
00147
00158 template <std::size_t k, typename Complex>
00159 static inline auto &get(SimplexMap<Complex> &S)
00160 {
00161     return S.template get<k>();
00162 }
00163
00165 template <std::size_t k, typename Complex>
00166 static inline auto &get(const SimplexMap<Complex> &S)
00167 {
00168     return S.template get<k>();
00169 }
00170 } // end namespace casc

```

## 10.13 include/casc/SimplexSet.h File Reference

SimplexSet data structure and associated convenience functions.

```

#include <algorithm>
#include <unordered_set>

```

```
#include "util.h"
```

## Data Structures

- struct `casc::SimplexSet< Complex >`  
*A multiset to store simplices in a [simplicial\\_complex](#).*

## Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

## Functions

- template<std::size\_t k, typename Complex>  
static auto & `casc::get` (`SimplexSet< Complex >` &S)  
*Get the [NodeSet](#) for a simplex dimension from a [SimplexSet](#).*
- template<std::size\_t k, typename Complex>  
static auto & `casc::get` (const `SimplexSet< Complex >` &S)
- template<typename Complex>  
bool `casc::operator==` (const `SimplexSet< Complex >` &lhs, const `SimplexSet< Complex >` &rhs)  
*Compare if the sets are equivalent.*
- template<typename Complex>  
bool `casc::operator!=` (const `SimplexSet< Complex >` &lhs, const `SimplexSet< Complex >` &rhs)  
*Compare if the sets are not equivalent.*
- template<typename Complex>  
static void `casc::set_union` (const `SimplexSet< Complex >` &A, const `SimplexSet< Complex >` &B, `SimplexSet< Complex >` &dest)  
*Compute the set union.*
- template<typename Complex>  
static void `casc::set_intersection` (const `SimplexSet< Complex >` &A, const `SimplexSet< Complex >` &B, `SimplexSet< Complex >` &dest)  
*Compute the set intersection.*
- template<typename Complex>  
static void `casc::set_difference` (const `SimplexSet< Complex >` &A, const `SimplexSet< Complex >` &B, `SimplexSet< Complex >` &dest)  
*Compute the set difference.*

## 10.14 SimplexSet.h

[Go to the documentation of this file.](#)

```
00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
00009  * modify it under the terms of the GNU Lesser General Public
00010  * License as published by the Free Software Foundation; either
00011  * version 2.1 of the License, or (at your option) any later version.
```

```

00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00029
00030 #pragma once
00031
00032 #include <algorithm>
00033 #include <unordered_set>
00034 #include "util.h"
00035
00036 namespace casc
00037 {
00038
00048 template <typename Complex>
00049 struct SimplexSet
00050 {
00052     template <std::size_t j>
00053     using SimplexID = typename Complex::template SimplexID<j>;
00055     using LevelIndex = typename Complex::LevelIndex;
00057     using cLevelIndex = typename util::remove_first_val<std::size_t,
00058                                     LevelIndex>::type;
00060     using RevIndex = typename util::reverse_sequence<std::size_t,
00061                                     LevelIndex>::type;
00063     using cRevIndex = typename util::reverse_sequence<std::size_t,
00064                                     cLevelIndex>::type;
00066     using type_this = SimplexSet<Complex>;
00067
00069     using SimplexIDLevel = typename util::int_type_map<std::size_t,
00070                                     std::tuple, LevelIndex, SimplexID>::type;
00071     // No real sense to hide this tuple of sets from the end users.
00072     // Making it private, we'd have to introduce lots of friend structs.
00074     typename util::type_map<SimplexIDLevel, NodeSet>::type tupleSet;
00075
00077     SimplexSet() {};
00079     ~SimplexSet() {};
00080
00081     // type_this& operator=(const type_this& other){
00082     //     util::int_for_each<std::size_t, LevelIndex>(CopyHelper(), this, other);
00083     // }
00084
00085     // type_this& operator=(type_this&& other){
00086     //     util::int_for_each<std::size_t, LevelIndex>(CopyHelper(), this, other);
00087     // }
00088
00096     template <std::size_t k>
00097     inline auto empty() const noexcept{
00098         return std::get<k>(tupleSet).empty();
00099     }
00100
00109     template <std::size_t k>
00110     inline auto size() const noexcept{
00111         return std::get<k>(tupleSet).size();
00112     }
00113
00117     void clear()
00118     {
00119         util::int_for_each<std::size_t, LevelIndex>(ClearHelper(), this);
00120     }
00121
00129     template <std::size_t k>
00130     inline void insert(SimplexID<k> s)
00131     {
00132         std::get<k>(tupleSet).insert(s);
00133     }
00134
00140     void insert(const SimplexSet<Complex> &s)
00141     {
00142         util::int_for_each<std::size_t, LevelIndex>(
00143             InsertHelper(), this, s);
00144     }
00145
00153     template <std::size_t k>
00154     inline void erase(SimplexID<k> s)
00155     {
00156         std::get<k>(tupleSet).erase(s);
00157     }
00158

```

```

00164     void erase(const SimplexSet<Complex> &s)
00165     {
00166         util::int_for_each<std::size_t, LevelIndex>(
00167             EraseHelper(), this, s);
00168     }
00169
00181     template <std::size_t k>
00182     inline auto find(const SimplexID<k> s)
00183     {
00184         return std::get<k>(tupleSet).find(s);
00185     }
00186
00198     template <std::size_t k>
00199     inline auto find(const SimplexID<k> s) const
00200     {
00201         return std::get<k>(tupleSet).find(s);
00202     }
00203
00212     template <std::size_t k>
00213     inline auto end()
00214     {
00215         return std::get<k>(tupleSet).end();
00216     }
00217
00226     template <std::size_t k>
00227     inline auto cend() const
00228     {
00229         return std::get<k>(tupleSet).cend();
00230     }
00231
00239     template <std::size_t k>
00240     inline auto begin()
00241     {
00242         return std::get<k>(tupleSet).begin();
00243     }
00244
00252     template <std::size_t k>
00253     inline auto cbegin() const
00254     {
00255         return std::get<k>(tupleSet).cbegin();
00256     }
00257
00258     /**
00259     // * @brief      Get the NodeSet for a particular simplex dimension.
00260     // *
00261     // * @tparam      k      Simplex dimension to get.
00262     // *
00263     // * @return      Returns the NodeSet corresponding to the requested dimension.
00264     // */
00265     template <std::size_t k>
00266     inline auto &get()
00267     {
00268         return std::get<k>(tupleSet);
00269     }
00270
00271     /**
00272     // * @brief      Get the NodeSet for a particular simplex dimension.
00273     // *
00274     // * @tparam      k      Simplex dimension to get.
00275     // *
00276     // * @return      Returns the NodeSet corresponding to the requested dimension.
00277     // */
00278     template <std::size_t k>
00279     inline auto &get() const
00280     {
00281         return std::get<k>(tupleSet);
00282     }
00283
00294     friend std::ostream &operator<<(std::ostream &output, const SimplexSet<Complex> &S)
00295     {
00296         output << "SimplexSet(";
00297         util::int_for_each<std::size_t, LevelIndex>(PrintHelper(),
00298             output, S);
00299         output << ")";
00300         return output;
00301     }
00302
00303     private:
00304     struct InsertHelper
00305     {
00306     {
00318         template <std::size_t k>
00319         static void apply(type_this* that, const SimplexSet<Complex> &S)
00320         {
00321             auto s = std::get<k>(S.tupleSet);
00322             for (auto simplex : s)
00323             {

```

```

00324         that->insert(simplex);
00325     }
00326 }
00327 };
00328
00332 struct EraseHelper
00333 {
00342     template <std::size_t k>
00343     static void apply(type_this* that, const SimplexSet<Complex> &S)
00344     {
00345         auto s = std::get<k>(S.tupleSet);
00346         for (auto simplex : s)
00347         {
00348             that->erase(simplex);
00349         }
00350     }
00351 };
00352
00356 struct PrintHelper
00357 {
00366     template <std::size_t k>
00367     static void apply(std::ostream &output, const SimplexSet<Complex> &S)
00368     {
00369         output << "[l=" << k;
00370         auto s = std::get<k>(S.tupleSet);
00371         for (auto simplex : s)
00372         {
00373             output << ", " << simplex;
00374         }
00375         output << "];";
00376     }
00377 };
00378
00382 struct ClearHelper
00383 {
00391     template <std::size_t k>
00392     void apply(type_this* that)
00393     {
00394         auto &s = std::get<k>(that->tupleSet);
00395         s.clear();
00396     }
00397 };
00398
00399 // struct CopyHelper
00400 // {
00401 //     template <std::size_t k>
00402 //     void apply(type_this& that, type_this& other){
00403 //         auto &s = that.get<k>();
00404 //         s = other.get<k>();
00405 //     }
00406 //
00407 //     template <std::size_t k>
00408 //     void apply(type_this& that, type_this&& other){
00409 //         auto &s = that.get<k>();
00410 //         s = other.get<k>();
00411 //     }
00412 // };
00413 };
00414
00426 template <std::size_t k, typename Complex>
00427 static inline auto &get(SimplexSet<Complex> &S)
00428 {
00429     return S.template get<k>();
00430 }
00431
00435 template <std::size_t k, typename Complex>
00436 static inline auto &get(const SimplexSet<Complex> &S)
00437 {
00438     return S.template get<k>();
00439 }
00440
00443 namespace simplex_set_detail
00444 {
00445
00451 template <typename Complex>
00452 struct UnionH
00453 {
00465     template <std::size_t k>
00466     static void apply(const SimplexSet<Complex> &A,
00467                     const SimplexSet<Complex> &B,
00468                     SimplexSet<Complex> &dest)
00469     {
00470         auto a = std::get<k>(A.tupleSet);
00471         auto b = std::get<k>(B.tupleSet);
00472         auto &d = std::get<k>(dest.tupleSet);
00473         d.insert(a.begin(), a.end());
00474         d.insert(b.begin(), b.end());

```

```

00475     }
00476 };
00477
00483 template <typename Complex>
00484 struct IntersectH
00485 {
00497     template <std::size_t k>
00498     static void apply(const SimplexSet<Complex> &A,
00499                     const SimplexSet<Complex> &B,
00500                     SimplexSet<Complex> &dest)
00501     {
00502         auto a = casc::get<k>(A);
00503         auto b = casc::get<k>(B);
00504         auto &d = casc::get<k>(dest);
00505
00506         if (a.size() < b.size())
00507         {
00508             for (auto item : a)
00509             {
00510                 if (b.find(item) != b.end())
00511                     d.insert(item);
00512             }
00513         }
00514         else
00515         {
00516             for (auto item : b)
00517             {
00518                 if (a.find(item) != a.end())
00519                     d.insert(item);
00520             }
00521         }
00522     }
00523 };
00524
00530 template <typename Complex>
00531 struct DifferenceH
00532 {
00544     template<std::size_t k>
00545     static void apply(const SimplexSet<Complex> &A,
00546                     const SimplexSet<Complex> &B,
00547                     SimplexSet<Complex> &dest)
00548     {
00549         auto a = casc::get<k>(A);
00550         auto b = casc::get<k>(B);
00551         auto &d = casc::get<k>(dest);
00552
00553         for (auto item : a)
00554         {
00555             if (b.find(item) == b.end())
00556                 d.insert(item);
00557         }
00558     }
00559 };
00560
00566 template <typename Complex>
00567 struct OperatorEQH
00568 {
00570     bool result;
00571
00573     OperatorEQH(): result(true) {}
00574
00583     template <std::size_t k>
00584     void apply(const SimplexSet<Complex> &lhs,
00585              const SimplexSet<Complex> &rhs){
00586         auto a = casc::get<k>(lhs);
00587         auto b = casc::get<k>(rhs);
00588         result &= a==b;
00589     }
00590 };
00591 } // end namespace simplex_set_detail
00592
00604 template <typename Complex>
00605 bool operator==(const SimplexSet<Complex> &lhs, const SimplexSet<Complex> &rhs){
00606     auto func = simplex_set_detail::OperatorEQH<Complex>();
00607     util::int_for_each<std::size_t, typename Complex::LevelIndex>(
00608         func, lhs, rhs);
00609     return func.result;
00610 }
00611
00622 template <typename Complex>
00623 bool operator!=(const SimplexSet<Complex> &lhs, const SimplexSet<Complex> &rhs){
00624     return !(lhs == rhs);
00625 }
00626
00636 template <typename Complex>
00637 static void set_union(const SimplexSet<Complex> &A,
00638                     const SimplexSet<Complex> &B,

```

```

00639             SimplexSet<Complex>          &dest)
00640 {
00641     util::int_for_each<std::size_t,
00642         typename Complex::LevelIndex>(
00643         simplex_set_detail::UnionH<Complex>(), A, B, dest);
00644 }
00645
00655 template <typename Complex>
00656 static void set_intersection(const SimplexSet<Complex> &A,
00657                             const SimplexSet<Complex> &B,
00658                             SimplexSet<Complex>          &dest)
00659 {
00660     util::int_for_each<std::size_t,
00661         typename Complex::LevelIndex>(
00662         simplex_set_detail::IntersectH<Complex>(), A, B, dest);
00663 }
00664
00674 template <typename Complex>
00675 static void set_difference(const SimplexSet<Complex> &A,
00676                           const SimplexSet<Complex> &B,
00677                           SimplexSet<Complex>          &dest)
00678 {
00679     util::int_for_each<std::size_t,
00680         typename Complex::LevelIndex>(
00681         simplex_set_detail::DifferenceH<Complex>(), A, B, dest);
00682 }
00683 } // end namespace casc

```

## 10.15 include/casc/SimplicialComplex.h File Reference

This header contains the main CASC data structure and associated components.

```

#include <algorithm>
#include <assert.h>
#include <cstdint>
#include <map>
#include <set>
#include <iterator>
#include <array>
#include <vector>
#include <iostream>
#include <fstream>
#include <functional>
#include <type_traits>
#include <ostream>
#include <unordered_set>
#include <unordered_map>
#include <utility>
#include <stdexcept>
#include "index_tracker.h"
#include "util.h"

```

### Data Structures

- class [casc::simplicial\\_complex< traits >](#)  
*The CASC data structure for representing simplicial complexes of arbitrary dimensionality with coloring.*
- struct [casc::simplicial\\_complex< traits >::SimplexID< k >](#)  
*A handle for a simplex object in the complex.*
- struct [casc::simplicial\\_complex< traits >::EdgeID< k >](#)  
*External reference to an edge or a connection within the complex.*



## Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

## Typedefs

- `template<typename KeyType, typename ... Ts>`  
using `casc::AbstractSimplicialComplex`
- `template<typename T>`  
using `casc::NodeSet`  
*Helpful alias defining a `unordered_set` of simplices. See also `hashSimplexID`.*

## 10.16 SimplicialComplex.h

[Go to the documentation of this file.](#)

```

00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
00009  * modify it under the terms of the GNU Lesser General Public
00010  * License as published by the Free Software Foundation; either
00011  * version 2.1 of the License, or (at your option) any later version.
00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00030
00031 #pragma once
00032
00033 #include <algorithm>
00034 #include <assert.h>
00035 #include <cstdlib>
00036 #include <map>
00037 #include <set>
00038 #include <iterator>
00039 #include <array>
00040 #include <vector>
00041 #include <iostream>
00042 #include <fstream>
00043 #include <functional>
00044 #include <type_traits>
00045 #include <ostream>
00046 #include <unordered_set>
00047 #include <unordered_map>
00048 #include <utility>
00049 #include <stdexcept>
00050
00051 #include "index_tracker.h"
00052 #include "util.h"
00053
00054 #if __has_cpp_attribute(maybe_unused)
00055 #define MAYBE_UNUSED [[maybe_unused]]
00056 #else
00057 #define MAYBE_UNUSED
00058 #endif
00059
00061 namespace casc
00062 {
00065     namespace detail

```

```

00066 {
00067 template <class T> using map = std::map<std::size_t, T>;
00068
00069 template <typename T1, typename T2>
00070 struct asc_pair {
00071     using this_t = asc_pair<T1, T2>;
00072     asc_pair() {}
00073     asc_pair(const T1& first, const T2& second) : _pair(first, second) {}
00074     asc_pair(T1&& first, T2&& second) : _pair(std::forward<T1>(first), std::forward<T2>(second)) {}
00075     asc_pair(const this_t& other) : _pair(other._pair) {}
00076     asc_pair(this_t&& other) : _pair(std::forward<std::pair<T1,T2>>(other._pair)) {}
00077
00078     operator T1() const {
00079         return _pair.first;
00080     }
00081
00082     this_t& operator=(const this_t& other){
00083         _pair = other._pair;
00084         return *this;
00085     }
00086
00087     this_t& operator=(this_t&& other){
00088         _pair = std::move(other._pair);
00089         return *this;
00090     }
00091
00092     friend bool operator==(const this_t& lhs, const this_t& rhs) {return lhs.first == rhs.first;}
00093     friend bool operator!=(const this_t& lhs, const this_t& rhs) {return lhs.first != rhs.first;}
00094     friend bool operator<=(const this_t& lhs, const this_t& rhs) {return lhs.first <= rhs.first;}
00095     friend bool operator>=(const this_t& lhs, const this_t& rhs) {return lhs.first >= rhs.first;}
00096     friend bool operator<(const this_t& lhs, const this_t& rhs) {return lhs.first < rhs.first;}
00097     friend bool operator>(const this_t& lhs, const this_t& rhs) {return lhs.first > rhs.first;}
00098
00099     T1& first = _pair.first;
00100     T2& second = _pair.second;
00101 private:
00102     std::pair<T1,T2> _pair;
00103 };
00104
00105 template <typename KEY_T, typename VAL_T, std::size_t k>
00106 struct asc_arraymap {
00107     using pair_t = asc_pair<KEY_T, VAL_T>;
00108     using array_t = std::array<pair_t, k>;
00109     using iterator = typename array_t::iterator;
00110     using const_iterator = typename array_t::const_iterator;
00111
00112     asc_arraymap(){
00113         _begin = _array.begin();
00114         _end = _array.begin();
00115     }
00116
00117     void insert(pair_t& p){
00118         if (_end == _array.end())
00119             throw std::out_of_range("insert&: Adding element beyond the end of array.");
00120         *_end = p;
00121         ++_end;
00122         std::sort(_begin, _end);
00123     }
00124
00125     void insert(pair_t&& p){
00126         if (_end == _array.end())
00127             throw std::out_of_range("insert&&: Adding element beyond the end of array.");
00128         *_end = std::forward<pair_t>(p);
00129         ++_end;
00130         std::sort(_begin, _end);
00131     }
00132
00133     iterator find(const KEY_T& key){
00134         return std::find(_begin, _end, key);
00135     }
00136
00137     void erase(const KEY_T& key){
00138         auto it = std::find(_begin, _end, key);
00139         if(it != _end){
00140             std::copy(it+1, _end, it);
00141             --_end;
00142         }
00143     }
00144
00145     std::size_t size() const{
00146         return std::distance(_end, _begin);
00147     }
00148
00149     VAL_T& operator[](const KEY_T& key){
00150         auto it = std::find(_begin, _end, key);
00151         if(it != _end){
00152             return it->second;
00153         }
00154     }
00155
00156     }
00157
00158     }
00159
00160     }
00161
00162     }
00163
00164     }
00165
00166     }

```

```

00167     }
00168     else{
00169         if (_end == _array.end())
00170             throw std::out_of_range("operator[]: Adding element beyond the end of array.");
00171         _end->first = key;
00172         ++_end;
00173         std::sort(_begin, _end);
00174         return std::find(_begin, _end, key)->second;
00175     }
00176 }
00177
00178 iterator begin(){ return _begin; }
00179 iterator end(){ return _end; }
00180 const_iterator cbegin() const {return _begin;}
00181 const_iterator cend() const {return _end;}
00182
00183 private:
00184     array_t _array;
00185     iterator _begin;
00186     iterator _end;
00187 };
00188
00189
00190 template <typename KEY_T, typename VAL_T>
00191 struct asc_vectormap {
00192     using pair_t = asc_pair<KEY_T, VAL_T>;
00193     using vector_t = std::vector<pair_t>;
00194     using iterator = typename vector_t::iterator;
00195     using const_iterator = typename vector_t::const_iterator;
00196
00197     asc_vectormap() {}
00198
00199     void insert(pair_t& p){
00200         iterator first = std::lower_bound(_vector.begin(), _vector.end(), p);
00201         if ((first == _vector.end()) || (*first != p)){
00202             _vector.insert(first, p);
00203         }
00204         else{
00205             std::cout << "Item already exists...";
00206         }
00207     }
00208
00209     void insert(pair_t&& p){
00210         iterator first = std::lower_bound(_vector.begin(), _vector.end(), p);
00211         if ((first == _vector.end()) || (*first != p)){
00212             _vector.insert(first, std::forward<pair_t>(p));
00213         }
00214         else{
00215             std::cout << "Item already exists...";
00216         }
00217     }
00218
00219     iterator find(const KEY_T& key){
00220         iterator first = std::lower_bound(_vector.begin(), _vector.end(), key);
00221         if (first != _vector.end()){
00222             if (*first != key){
00223                 return _vector.end();
00224             }
00225             else{
00226                 return first;
00227             }
00228         }
00229         else{
00230             return first;
00231         }
00232     }
00233
00234     void erase(const KEY_T& key){
00235         iterator it = this->find(key);
00236         if (it != _vector.end()){
00237             _vector.erase(it);
00238         }
00239     }
00240
00241     std::size_t size() const{
00242         return _vector.size();
00243     }
00244
00245     VAL_T& at(const KEY_T& key){
00246         iterator first = std::lower_bound(_vector.begin(), _vector.end(), key);
00247         if ((first == _vector.end()) || (first->first != key)){
00248             throw std::out_of_range("Could not find element in asc_vectormap.");
00249         }
00250         else {
00251             return first->second;
00252         }
00253     }
00254 }

```

```

00260
00261     VAL_T& operator[](const KEY_T& key){
00262         iterator first = std::lower_bound(_vector.begin(), _vector.end(), key);
00263         if ((first == _vector.end()) || (first->first != key)){
00264             first = _vector.emplace(first, pair_t());
00265             first->first = key;
00266             return first->second;
00267         }
00268         else {
00269             return first->second;
00270         }
00271     }
00272
00273     iterator begin(){ return _vector.begin(); }
00274     iterator end(){ return _vector.end(); }
00275     const_iterator cbegin() const {return _vector.cbegin();}
00276     const_iterator cend() const {return _vector.cend();}
00277 private:
00278     vector_t _vector;
00279 };
00280
00281
00282 template <class KeyType, std::size_t k, std::size_t N, typename DataTypes, class> struct asc_Node;
00290
00292 struct asc_NodeBase {
00293     asc_NodeBase(std::size_t id) : _node(id) {}
00294     virtual ~asc_NodeBase() {};
00295     std::size_t _node;
00301 };
00302
00308 template <class DataType>
00309 struct asc_NodeData {
00310     DataType _data;
00311 };
00312
00319 template <>
00320 struct asc_NodeData<void> {};
00321
00328 template <class KeyType, class DataType>
00329 struct asc_EdgeData {
00330     std::unordered_map<KeyType, DataType> _edge_data;
00332 };
00333
00339 template <class KeyType>
00340 struct asc_EdgeData<KeyType, void> {};
00341
00351 template < class KeyType,
00352             std::size_t k,
00353             std::size_t N,
00354             class NodeDataTypes,
00355             class EdgeDataTypes>
00356 struct asc_NodeDown :
00357     public asc_EdgeData<KeyType,
00358         typename util::type_get<k-1, EdgeDataTypes>::type> {
00359     using DownNodeT = asc_Node<KeyType, k-1, N, NodeDataTypes, EdgeDataTypes>;
00361
00363     asc_arraymap<KeyType, DownNodeT*, k> _down;
00364     // std::map<KeyType, DownNodeT*> _down;
00365 };
00366
00376 template < class KeyType,
00377             std::size_t k,
00378             std::size_t N,
00379             class NodeDataTypes,
00380             class EdgeDataTypes>
00381 struct asc_NodeUp {
00382     using UpNodeT = asc_Node<KeyType, k+1, N, NodeDataTypes, EdgeDataTypes>;
00384     asc_vectormap<KeyType, UpNodeT*> _up;
00385     // std::unordered_map<KeyType, UpNodeT*> _up;    /**< @brief Map of pointers to children */
00386 };
00387
00397 template <class KeyType, std::size_t k, std::size_t N, class NodeDataTypes, class EdgeDataTypes>
00398 struct asc_Node : public asc_NodeBase,
00399     public asc_NodeData<typename util::type_get<k, NodeDataTypes>::type>,
00400     public asc_NodeDown<KeyType, k, N, NodeDataTypes, EdgeDataTypes>,
00401     public asc_NodeUp<KeyType, k, N, NodeDataTypes, EdgeDataTypes>
00402 {
00404     static constexpr std::size_t level = k;
00405
00411     asc_Node(std::size_t id) : asc_NodeBase(id) {}
00412
00421     friend std::ostream &operator<<(std::ostream &output, const asc_Node &node)
00422     {
00423         output << "Node(level=" << k << ", " << "id=" << node._node;
00424         if (node._down.size() > 0)
00425         {
00426             for (auto it = node._down.cbegin(); it != node._down.cend(); ++it)

```

```

00427         {
00428             output << " , NodeDownID={' "
00429                 << it->first << " , "
00430                 << it->second->_node << " }";
00431         }
00432     }
00433     if (node._up.size() > 0)
00434     {
00435         for (auto it = node._up.cbegin(); it != node._up.cend(); ++it)
00436         {
00437             output << " , NodeUpID={' "
00438                 << it->first << " , "
00439                 << it->second->_node << " }";
00440         }
00441     }
00442     output << " )";
00443     return output;
00444 }
00445 };
00446
00455 template <class KeyType, std::size_t N, class NodeDataTypes, class EdgeDataTypes>
00456 struct asc_Node<KeyType, 0, N, NodeDataTypes, EdgeDataTypes> :
00457     public asc_NodeBase,
00458     public asc_NodeData<typename util::type_get<0, NodeDataTypes>::type>,
00459     public asc_NodeUp<KeyType, 0, N, NodeDataTypes, EdgeDataTypes>
00460 {
00461     static constexpr std::size_t level = 0;
00462
00463     asc_Node(std::size_t id) : asc_NodeBase(id) {}
00464
00465     friend std::ostream &operator<<(std::ostream &output, const asc_Node &node)
00466     {
00467         output << "Node(level=" << 0
00468             << " , id=" << node._node;
00469         if (node._up.size() > 0)
00470         {
00471             for (auto it = node._up.cbegin(); it != node._up.cend(); ++it)
00472             {
00473                 output << " , NodeUpID={' "
00474                     << it->first << " , "
00475                     << it->second->_node << " }";
00476             }
00477         }
00478         output << " )";
00479         return output;
00480     }
00481 };
00482
00495 template <class KeyType, std::size_t N, class NodeDataTypes, class EdgeDataTypes>
00496 struct asc_Node<KeyType, N, N, NodeDataTypes, EdgeDataTypes> :
00497     public asc_NodeBase,
00498     public asc_NodeData<typename util::type_get<N, NodeDataTypes>::type>,
00499     public asc_NodeDown<KeyType, N, N, NodeDataTypes, EdgeDataTypes>
00500 {
00501     static constexpr std::size_t level = N;
00502
00503     asc_Node(std::size_t id) : asc_NodeBase(id) {}
00504
00505     friend std::ostream &operator<<(std::ostream &output, const asc_Node &node)
00506     {
00507         output << "Node(level=" << N
00508             << " , id=" << node._node;
00509         if (node._down.size() > 0)
00510         {
00511             for (auto it = node._down.cbegin(); it != node._down.cend(); ++it)
00512             {
00513                 output << " , NodeDownID={' "
00514                     << it->first << " , "
00515                     << it->second->_node << " }";
00516             }
00517         }
00518         output << " )";
00519         return output;
00520     }
00521 };
00522
00533 template <typename Iter, typename Data>
00534 struct node_id_iterator : public std::iterator<std::bidirectional_iterator_tag, Data> {
00535     public:
00536         using super = std::iterator<std::bidirectional_iterator_tag, Data>;
00537         node_id_iterator() {}
00538         node_id_iterator(Iter j) : i(j) {}
00539         node_id_iterator &operator++() { ++i; return *this; }
00540         node_id_iterator operator++(int) { auto tmp = *this; ++(*this); return tmp; }
00541         node_id_iterator &operator--() { --i; return *this; }
00542         node_id_iterator operator--(int) { auto tmp = *this; --(*this); return tmp; }
00543         bool operator==(node_id_iterator j) const { return i == j.i; }
00544 }

```

```

00573         bool operator!=(node_id_iterator j) const { return !(*this == j); }
00575         Data operator*() { return Data(i->second); }
00577         const Data operator*() const {return Data(i->second); }
00579         typename super::pointer operator->() { return Data(i->second); }
00580     protected:
00582         Iter i;
00583 };
00584
00595 template <typename Iter, typename Data>
00596 inline node_id_iterator<Iter, Data> make_node_id_iterator(Iter j)
00597 {
00598     return node_id_iterator<Iter, Data>(j);
00599 }
00600
00607 template <typename Iter, typename Data>
00608 struct node_data_iterator : public std::iterator<std::bidirectional_iterator_tag, Data> {
00609     public:
00611         using super = std::iterator<std::bidirectional_iterator_tag, Data>;
00613         node_data_iterator() {}
00615         node_data_iterator(Iter j) : i(j) {}
00617         node_data_iterator &operator++() { ++i; return *this; }
00619         node_data_iterator operator++(int) { auto tmp = *this; ++(*this); return tmp; }
00621         node_data_iterator &operator--() { --i; return *this; }
00623         node_data_iterator operator--(int) { auto tmp = *this; --(*this); return tmp; }
00625         bool operator==(node_data_iterator j) const { return i == j.i; }
00627         bool operator!=(node_data_iterator j) const { return !(*this == j); }
00629         typename super::reference operator*() { return i->second->_data; }
00631         typename super::pointer operator->() { return i->second->_data; }
00632     protected:
00634         Iter i;
00635 };
00636
00647 template <typename Iter, typename Data>
00648 inline node_data_iterator<Iter, Data> make_node_data_iterator(Iter j)
00649 {
00650     return node_data_iterator<Iter, Data>(j);
00651 }
00652
00661 template <typename K, typename ... Ts>
00662 struct simplicial_complex_traits_default
00663 {
00665     template <std::size_t k> using all_int = int;
00667     using KeyType = K;
00669     using NodeTypes = util::type_holder<Ts...>;
00671     using EdgeTypes = typename util::int_type_map<std::size_t,
00672                                                 util::type_holder,
00673                                                 typename std::make_index_sequence<sizeof ...
00674                                                 (Ts)-1>,
00675                                                 all_int>::type;
00676 };
00677 // end namespace detail
00678
00702 template <typename traits>
00703 class simplicial_complex
00704 {
00705     public:
00707         using KeyType = typename traits::KeyType;
00709         using NodeDataTypes = typename traits::NodeTypes;
00711         using EdgeDataTypes = typename traits::EdgeTypes;
00713         using type_this = simplicial_complex<traits>;
00715         static constexpr std::size_t numLevels = NodeDataTypes::size;
00717         static constexpr std::size_t topLevel = numLevels-1;
00719         static constexpr std::size_t bdryLevel = numLevels-2;
00721         using LevelIndex = typename std::make_index_sequence<numLevels>;
00722     private:
00724         template <std::size_t k> using Node = detail::asc_Node<KeyType, k, topLevel, NodeDataTypes,
EdgeDataTypes>;
00726         template <std::size_t k> using NodePtr = Node<k>*;
00727
00728     public:
00730         template <std::size_t k> using NodeData = typename util::type_get<k, NodeDataTypes>::type;
00732         template <std::size_t k> using EdgeData = typename util::type_get<k, EdgeDataTypes>::type;
00733
00734         friend struct SimplexID;
00736
00746         template <std::size_t k>
00747         struct SimplexID {
00749             using complex = simplicial_complex<traits>;
00751             friend simplicial_complex<traits>;
00753             static constexpr std::size_t level = k;
00754
00755             SimplexID() : ptr(nullptr) {}
00759
00765             SimplexID(NodePtr<k> p) : ptr(p) {}
00766
00772             SimplexID(const SimplexID &rhs) : ptr(rhs.ptr) {}
00773

```

```

00775         SimplexID &operator=(const SimplexID &rhs) { ptr = rhs.ptr; return *this; }
00776
00778     friend bool operator==(SimplexID lhs, SimplexID rhs) { return lhs.ptr == rhs.ptr; }
00780     friend bool operator!=(SimplexID lhs, SimplexID rhs) { return lhs.ptr != rhs.ptr; }
00782     friend bool operator<=(SimplexID lhs, SimplexID rhs) { return lhs.ptr <= rhs.ptr; }
00784     friend bool operator>=(SimplexID lhs, SimplexID rhs) { return lhs.ptr >= rhs.ptr; }
00786     friend bool operator<(SimplexID lhs, SimplexID rhs) { return lhs.ptr < rhs.ptr; }
00788     friend bool operator>(SimplexID lhs, SimplexID rhs) { return lhs.ptr > rhs.ptr; }
00789
00791     explicit operator std::uintptr_t () const { return reinterpret_cast<std::uintptr_t>(ptr); }
00792 }
00793
00794     complex::NodeData<k> const &operator*() const { return ptr->_data; }
00796     complex::NodeData<k> &operator*() { return ptr->_data; }
00797
00799     complex::NodeData<k> const &data() const { return ptr->_data; }
00801     complex::NodeData<k> &data() { return ptr->_data; }
00802
00810     std::array<KeyType, k> indices() const
00811     {
00812         std::array<KeyType, k> s;
00813         std::size_t i = 0;
00814         for (auto curr : ptr->_down)
00815         {
00816             s[i++] = curr.first;
00817         }
00818
00819         return std::move(s);
00820     }
00821
00822     // Valid in C++17
00823     // TODO: (0) expose this to modern compilers
00824     // if constexpr (k < complex::topLevel){
00832     template <class Inserter>
00833     void cover_insert(Inserter pos) const
00834     {
00835         for (auto curr : ptr->_up)
00836         {
00837             *pos++ = curr.first;
00838         }
00839     }
00840
00846     std::vector<KeyType> cover() const
00847     {
00848         std::vector<KeyType> rval;
00849         cover_insert(std::back_inserter(rval));
00850         return rval;
00851     }
00852     // }
00853
00863     template <std::size_t j>
00864     SimplexID<k+j> get_simplex_up(const KeyType (&s)[j]) const
00865     {
00866         static_assert(k+j <= complex::topLevel, "Cannot get simplex greater than the facets");
00867         return complex::get_recurse<k, j>::apply(s, this->ptr);
00868     }
00869
00879     template <std::size_t j>
00880     SimplexID<k+j> get_simplex_up(const std::array<KeyType, j> &arr) const
00881     {
00882         static_assert(k+j <= complex::topLevel, "Cannot get simplex greater than the facets");
00883         return get_recurse<k, j>::apply(arr.data(), this->ptr);
00884     }
00885
00898     SimplexID<k+1> get_simplex_up(const KeyType s) const
00899     {
00900         return get_recurse<k, 1>::apply(&s, this->ptr);
00901     }
00902
00906     template <std::size_t j>
00907     SimplexID<k-j> get_simplex_down(const KeyType (&s)[j]) const
00908     {
00909         return get_down_recurse<k, j>::apply(s, this->ptr);
00910     }
00911
00915     template <std::size_t j>
00916     SimplexID<k-j> get_simplex_down(const std::array<KeyType, j> &arr) const
00917     {
00918         return get_down_recurse<k, j>::apply(arr.data(), this->ptr);
00919     }
00920
00924     SimplexID<k-1> get_simplex_down(const KeyType s) const
00925     {
00926         return get_down_recurse<k, 1>::apply(&s, this->ptr);
00927     }
00928
00944     friend std::ostream &operator<<(std::ostream &out,

```

```

00945                                     const SimplexID &nid)
00946     {
00947         // currently no such thing as static_if in c++ so we use a
00948         // template
00949         // helper
00950         out << "s{";
00951         print_helper<k, 0>::apply(out, nid);
00952         out << "}";
00953         return out;
00954     }
00955
00956
00957     // NOTE: Manually swap out these print functions for debugging if
00958     // desired.
00959     // /**
00960     //  * @brief      A full debug printout of of the node itself
00961     //  *
00962     //  * @param      out      Handle to the stream
00963     //  * @param[in]   nid      SimplexID of interest
00964     //  *
00965     //  * @return      Handle to the stream
00966     //  */
00967     // friend std::ostream& operator<<(std::ostream& out, const
00968     // SimplexID& nid){ out << *nid.ptr; return out; }
00969
00970     // /**
00971     //  * @brief      Print the SimplexID as an ID.
00972     //  *
00973     //  * Example "0x7fd502402f10"
00974     //  *
00975     //  * @param      out      Handle to the stream
00976     //  * @param[in]   nid      Node of interest
00977     //  *
00978     //  * @return      Handle to the stream
00979     //  */
00980     // friend std::ostream &operator<<(std::ostream &out, const
00981     // SimplexID &nid) { out << nid.ptr; return out; }
00982
00983 private:
00992     template <std::size_t l, std::size_t foo>
00993     struct print_helper
00994     {
01003         static std::ostream &apply(std::ostream &out,
01004                                     const SimplexID<l> &nid)
01005         {
01006             auto down = (*nid.ptr)._down;
01007             for (auto it = down.cbegin(); it != down.cend()-1; ++it)
01008             {
01009                 out << it->first << ",";
01010             }
01011             out << (down.cend()-1)->first;
01012             return out;
01013         }
01014     };
01015
01023     template <std::size_t foo>
01024     struct print_helper<0, foo>
01025     {
01034         static std::ostream &apply(std::ostream &out,
01035                                     const SimplexID &nid)
01036         {
01037             out << "root " << nid;
01038             return out;
01039         }
01040     };
01042     NodePtr<k> ptr;
01043 };
01044
01045 friend struct EdgeID;
01046
01054 template <std::size_t k>
01055 struct EdgeID {
01057     using complex = simplicial_complex<traits>;
01059     friend simplicial_complex<traits>;
01061     static constexpr std::size_t level = k;
01062
01066     EdgeID() : ptr(nullptr), edge(0) {}
01067
01074     EdgeID(NodePtr<k> p, KeyType e) : ptr(p), edge(e) {}
01075
01081     EdgeID(const EdgeID &rhs) : ptr(rhs.ptr), edge(rhs.edge) {}
01082
01084     EdgeID &operator=(const EdgeID &rhs) { ptr = rhs.ptr; edge = rhs.edge; return *this;}
01085
01087     friend bool operator==(EdgeID lhs, EdgeID rhs) { return lhs.ptr == rhs.ptr && lhs.edge ==
rhs.edge; }
01089     friend bool operator!=(EdgeID lhs, EdgeID rhs) { return !(lhs == rhs); }

```



```

01091     friend bool operator<=(EdgeID lhs, EdgeID rhs) { return lhs < rhs || lhs == rhs; }
01093     friend bool operator>=(EdgeID lhs, EdgeID rhs) { return lhs > rhs || lhs == rhs; }
01095     friend bool operator<(EdgeID lhs, EdgeID rhs)
01096     {
01097         return (lhs.ptr < rhs.ptr) || (lhs.ptr == rhs.ptr && lhs.edge < rhs.edge);
01098     }
01100     friend bool operator>(EdgeID lhs, EdgeID rhs) { return rhs < lhs; }
01101
01102     // explicit operator std::size_t () const { return
01103     // static_cast<std::size_t>(ptr);
01104
01106     auto const &operator*() const { return data(); }
01108     auto &operator*() { return data(); }
01109
01111     KeyType      key() const { return edge; }
01112
01114     auto const &data() const { return ptr->_edge_data[edge]; }
01116     auto      &data() { return ptr->_edge_data[edge]; }
01117
01123     SimplexID<k> up() const { return ptr; }
01124
01130     SimplexID<k-1> down() const { return SimplexID<k-1>(ptr->_down[edge]); }
01131
01132     private:
01134         NodePtr<k> ptr;
01136         KeyType      edge;
01137 };
01138
01142     simplicial_complex()
01143     : node_count(0)
01144     {
01145         for (auto &x : level_count) // Initialize level_count to 0 for all
01146                                     // levels
01147         {
01148             x = 0;
01149         }
01150         // Create a root node
01151         _root = create_node<0>();
01152     }
01153
01161     ~simplicial_complex()
01162     {
01163         std::size_t count;
01164         remove_recurse<0, 0>::apply(this, &_root, &_root + 1, count);
01165     }
01166
01179     template <std::size_t n>
01180     SimplexID<n> insert(const KeyType (&s)[n])
01181     {
01182         for (const KeyType* p = s; p < s + n; ++p)
01183         {
01184             unused_vertices.remove(*p);
01185         }
01186         return insert_full<0, n>::apply(this, _root, s);
01187     }
01188
01203     template <std::size_t n>
01204     SimplexID<n> insert(const KeyType (&s)[n], const NodeData<n> &data)
01205     {
01206         for (const KeyType* p = s; p < s + n; ++p)
01207         {
01208             unused_vertices.remove(*p);
01209         }
01210         Node<n>* rval = insert_full<0, n>::apply(this, _root, s);
01211         rval->_data = data;
01212         return rval;
01213     }
01214
01223     template <std::size_t n>
01224     SimplexID<n> insert(const std::array<KeyType, n> &s)
01225     {
01226         for (KeyType x : s)
01227         {
01228             unused_vertices.remove(x);
01229         }
01230         return insert_full<0, n>::apply(this, _root, s.data());
01231     }
01232
01242     template <std::size_t n>
01243     SimplexID<n> insert(const std::array<KeyType, n> &s, const NodeData<n> &data)
01244     {
01245         for (KeyType x : s)
01246         {
01247             unused_vertices.remove(x);
01248         }
01249         Node<n>* rval = insert_full<0, n>::apply(this, _root, s.data());
01250         rval->_data = data;

```

```

01251         return rval;
01252     }
01253
01263     KeyType add_vertex()
01264     {
01265         KeyType v[1] = {unused_vertices.pop()};
01266         insert<1>(v);
01267         return v[0];
01268     }
01269
01275     KeyType add_vertex(const NodeData<1> &data)
01276     {
01277         KeyType v[1] = {unused_vertices.pop()};
01278         insert<1>(v, data);
01279         return v[0];
01280     }
01281
01282
01292     template <std::size_t n, typename Lambda>
01293     void get_name(SimplexID<n> id, Lambda fn) const
01294     {
01295         for (auto curr : id.ptr->_down)
01296         {
01297             fn(curr.first);
01298         }
01299     }
01300
01310     template <std::size_t n>
01311     std::array<KeyType, n> get_name(SimplexID<n> id) const
01312     {
01313         std::array<KeyType, n> s;
01314         std::size_t i = 0;
01315         for (auto curr : id.ptr->_down)
01316         {
01317             s[i++] = curr.first;
01318         }
01319         assert(i == n);
01320         return s;
01321     }
01322
01333     std::array<KeyType, 0> get_name(SimplexID<0>) const
01334     {
01335         std::array<KeyType, 0> name{};
01336         return name;
01337     }
01338
01339
01349     template <std::size_t n>
01350     SimplexID<n> get_simplex_up(const KeyType (&s)[n]) const
01351     {
01352         return get_recurse<0, n>::apply(s, _root);
01353     }
01354
01355     template <std::size_t n>
01356     SimplexID<n> get_simplex_up(const std::array<KeyType, n> &arr) const
01357     {
01358         return get_recurse<0, n>::apply(arr.data(), _root);
01359     }
01360
01373     template <std::size_t i, std::size_t j>
01374     SimplexID<i+j> get_simplex_up(const SimplexID<i> id, const KeyType (&s)[j]) const
01375     {
01376         return get_recurse<i, j>::apply(s, id);
01377     }
01378
01379     template <std::size_t i, std::size_t j>
01380     SimplexID<i+j> get_simplex_up(const SimplexID<i> id, const std::array<KeyType, j> &arr) const
01381     {
01382         return get_recurse<i, j>::apply(arr.data(), id);
01383     }
01384
01385
01398     template <std::size_t i>
01399     SimplexID<i+1> get_simplex_up(const SimplexID<i> id, const KeyType s) const
01400     {
01401         return get_recurse<i, 1>::apply(&s, id.ptr);
01402     }
01403
01409     SimplexID<0> get_simplex_up() const
01410     {
01411         return _root;
01412     }
01413
01414
01427     template <std::size_t i, std::size_t j>
01428     SimplexID<i-j> get_simplex_down(const SimplexID<i> id, const KeyType (&s)[j]) const
01429     {

```

```

01430         return get_down_recurse<i, j>::apply(s, id.ptr);
01431     }
01432
01433     template <std::size_t i, std::size_t j>
01434     SimplexID<i-j> get_simplex_down(const SimplexID<i> id, const std::array<KeyType, j> &arr)
01435     const
01436     {
01437         return get_down_recurse<i, j>::apply(arr.data(), id.ptr);
01438     }
01439
01440     template <std::size_t i>
01441     SimplexID<i-1> get_simplex_down(const SimplexID<i> id, const KeyType s) const
01442     {
01443         return get_down_recurse<i, 1>::apply(&s, id.ptr);
01444     }
01445
01446     SimplexID<0> get_simplex_down() const
01447     {
01448         return _root;
01449     }
01450
01451     template <std::size_t k, class Inserter>
01452     void get_cover_insert(const SimplexID<k> id, Inserter pos) const
01453     {
01454         for (auto curr : id.ptr->_up)
01455         {
01456             *pos++ = curr.first;
01457         }
01458     }
01459
01460     template <std::size_t k, class Lambda>
01461     void get_cover(const SimplexID<k> id, Lambda fn) const
01462     {
01463         for (auto curr : id.ptr->_up)
01464         {
01465             fn(curr.first);
01466         }
01467     }
01468
01469     template <std::size_t k>
01470     std::vector<KeyType> get_cover(const SimplexID<k> id) const
01471     {
01472         std::vector<KeyType> rval;
01473         get_cover_insert(id, std::back_inserter(rval));
01474         return rval;
01475     }
01476
01477     template <std::size_t k>
01478     std::set<SimplexID<k+1> > up(const std::set<SimplexID<k> > &&simplices) const
01479     {
01480         std::set<SimplexID<k+1> > rval;
01481         for (auto simplex : simplices)
01482         {
01483             for (auto p : simplex.ptr->_up)
01484             {
01485                 rval.insert(SimplexID<k+1>(p.second));
01486             }
01487         }
01488         return rval;
01489     }
01490
01491     template <std::size_t k>
01492     std::set<SimplexID<k+1> > up(const std::set<SimplexID<k> > &&simplices) const
01493     {
01494         std::set<SimplexID<k+1> > rval;
01495         for (auto simplex : simplices)
01496         {
01497             for (auto p : simplex.ptr->_up)
01498             {
01499                 rval.insert(SimplexID<k+1>(p.second));
01500             }
01501         }
01502         return rval;
01503     }
01504
01505     template <std::size_t k>
01506     std::set<SimplexID<k+1> > up(const SimplexID<k> nid) const
01507     {
01508         std::set<SimplexID<k+1> > rval;
01509         for (auto p : nid.ptr->_up)
01510         {
01511             rval.insert(SimplexID<k+1>(p.second));
01512         }
01513         return rval;
01514     }
01515
01516     template <std::size_t k, class InsertIter>

```

```

01588 void up(const std::set<SimplexID<k>>&& simplices, InsertIter iter) const
01589 {
01590     for (auto simplex : simplices)
01591     {
01592         for (auto p : simplex.ptr->_up)
01593         {
01594             *iter++ = SimplexID<k+1>(p.second);
01595         }
01596     }
01597 }
01598
01599 template <std::size_t k, class InsertIter>
01600 void up(const std::set<SimplexID<k>>&& simplices, InsertIter iter) const
01601 {
01602     for (auto simplex : simplices)
01603     {
01604         for (auto p : simplex.ptr->_up)
01605         {
01606             *iter++ = SimplexID<k+1>(p.second);
01607         }
01608     }
01609 }
01610
01611 template <std::size_t k, class InsertIter>
01612 void up(const SimplexID<k> simplex, InsertIter iter) const
01613 {
01614     for (auto p : simplex.ptr->_up)
01615     {
01616         *iter++ = SimplexID<k+1>(p.second);
01617     }
01618 }
01619
01620 template <std::size_t k>
01621 std::set<SimplexID<k-1> > down(const std::set<SimplexID<k> > &&simplices) const
01622 {
01623     std::set<SimplexID<k-1> > rval;
01624     for (auto nid : simplices)
01625     {
01626         for (auto p : nid.ptr->_down)
01627         {
01628             rval.insert(SimplexID<k-1>(p.second));
01629         }
01630     }
01631     return rval;
01632 }
01633
01634 template <std::size_t k>
01635 std::set<SimplexID<k-1> > down(const std::set<SimplexID<k> > &simplices) const
01636 {
01637     std::set<SimplexID<k-1> > rval;
01638     for (auto simplex : simplices)
01639     {
01640         for (auto p : simplex.ptr->_down)
01641         {
01642             rval.insert(SimplexID<k-1>(p.second));
01643         }
01644     }
01645     return rval;
01646 }
01647
01648 template <std::size_t k>
01649 std::set<SimplexID<k-1> > down(const SimplexID<k> simplex) const
01650 {
01651     std::set<SimplexID<k-1> > rval;
01652     for (auto p : simplex.ptr->_down)
01653     {
01654         rval.insert(SimplexID<k-1>(p.second));
01655     }
01656     return rval;
01657 }
01658
01659 template <std::size_t k, class InsertIter>
01660 void down(const std::set<SimplexID<k>>&& simplices, InsertIter iter) const{
01661     for (auto simplex : simplices)
01662     {
01663         for (auto p : simplex.ptr->_down)
01664         {
01665             *iter++ = SimplexID<k-1>(p.second);
01666         }
01667     }
01668 }
01669
01670 template <std::size_t k, class InsertIter>
01671 void down(const std::set<SimplexID<k>>&& simplices, InsertIter iter) const{
01672     for (auto simplex : simplices)
01673     {
01674         for (auto p : simplex.ptr->_down)

```

```

01702         {
01703             *iter++ = SimplexID<k-1>(p.second);
01704         }
01705     }
01706 }
01707
01708 template <std::size_t k, class InsertIter>
01709 void down(const SimplexID<k> simplex, InsertIter iter) const{
01710     for (auto p : simplex.ptr->_down)
01711     {
01712         *iter++ = SimplexID<k-1>(p.second);
01713     }
01714 }
01715
01726 template <std::size_t k>
01727 EdgeID<k+1> get_edge_up(SimplexID<k> simplex, KeyType a)
01728 {
01729     return EdgeID<k+1>(simplex.ptr->_up.at(a), a);
01730 }
01731
01742 template <std::size_t k>
01743 EdgeID<k> get_edge_down(SimplexID<k> simplex, KeyType a)
01744 {
01745     return EdgeID<k>(simplex.ptr, a);
01746 }
01747
01758 template <std::size_t k>
01759 EdgeID<k+1> get_edge_up(SimplexID<k> simplex, KeyType a) const
01760 {
01761     return EdgeID<k+1>(simplex.ptr->_up.at(a), a);
01762 }
01763
01774 template <std::size_t k>
01775 EdgeID<k> get_edge_down(SimplexID<k> simplex, KeyType a) const
01776 {
01777     return EdgeID<k>(simplex.ptr, a);
01778 }
01779
01789 template <std::size_t k>
01790 bool exists(const KeyType (&s)[k]) const
01791 {
01792
01793     return get_recurse<0, k>::apply(s, _root) != nullptr;
01794 }
01795
01803 template <std::size_t k>
01804 std::size_t size() const
01805 {
01806     return std::get<k>(levels).size();
01807 }
01808
01809
01810 // template <std::size_t k> using SimplexIDIterator = detail::node_id_iterator<typename
detail::map<NodePtr<k>>::iterator, SimplexID<k>;
01819 template <std::size_t k>
01820 auto get_level_id()
01821 {
01822     auto begin = std::get<k>(levels).begin();
01823     auto end = std::get<k>(levels).end();
01824     auto data_begin = detail::make_node_id_iterator<decltype(begin), SimplexID<k> >(begin);
01825     auto data_end = detail::make_node_id_iterator<decltype(end), SimplexID<k> >(end);
01826     return util::make_range(data_begin, data_end);
01827 }
01828
01837 template <std::size_t k>
01838 auto get_level_id() const
01839 {
01840     auto begin = std::get<k>(levels).cbegin();
01841     auto end = std::get<k>(levels).cend();
01842     auto data_begin = detail::make_node_id_iterator<decltype(begin), const SimplexID<k>
>(begin);
01843     auto data_end = detail::make_node_id_iterator<decltype(end), const SimplexID<k> >(end);
01844     return util::make_range(data_begin, data_end);
01845 }
01846
01847
01848 // template <std::size_t k> using DataIterator = detail::node_data_iterator<typename
std::map<std::size_t, NodePtr<k>>::iterator, NodeData<k>;
01858 template <std::size_t k>
01859 auto get_level()
01860 {
01861     auto begin = std::get<k>(levels).begin();
01862     auto end = std::get<k>(levels).end();
01863     auto data_begin = detail::make_node_data_iterator<decltype(begin), NodeData<k> >(begin);
01864     auto data_end = detail::make_node_data_iterator<decltype(end), NodeData<k> >(end);
01865     return util::make_range(data_begin, data_end);
01866 }

```

```

01867
01877     template <std::size_t k>
01878     auto get_level() const
01879     {
01880         auto begin = std::get<k>(levels).cbegin();
01881         auto end = std::get<k>(levels).cend();
01882         auto data_begin = detail::make_node_data_iterator<decltype(begin), const NodeData<k>
>(begin);
01883         auto data_end = detail::make_node_data_iterator<decltype(end), const NodeData<k> >(end);
01884         return util::make_range(data_begin, data_end);
01885     }
01886
01897     template <std::size_t k>
01898     std::size_t remove(const KeyType (&s)[k])
01899     {
01900         Node<k>* root = get_recurse<0, k>::apply(s, _root);
01901         std::size_t count = 0;
01902         return remove_recurse<k, 0>::apply(this, &root, &root + 1, count);
01903     }
01904
01914     template <std::size_t k>
01915     std::size_t remove(const std::array<KeyType, k> &s)
01916     {
01917         Node<k>* root = get_recurse<0, k>::apply(s.data(), _root);
01918         std::size_t count = 0;
01919         return remove_recurse<k, 0>::apply(this, &root, &root + 1, count);
01920     }
01921
01932     template <std::size_t k>
01933     std::size_t remove(SimplexID<k> s)
01934     {
01935         std::size_t count = 0;
01936         return remove_recurse<k, 0>::apply(this, &s.ptr, &s.ptr + 1, count);
01937     }
01938
01951     template <std::size_t k>
01952     bool onBoundary(const SimplexID<k> s) const
01953     {
01954         return onBoundaryH<k, 0>::apply(s);
01955     }
01956
01957
01967     template <std::size_t level>
01968     bool nearBoundary(const SimplexID<level> s) const
01969     {
01970         return nearBoundaryH<level, 0>::apply(s);
01971     }
01972
01973     /** Reintroduce this code block when this is resolved
01974     // http://www.open-std.org/jtc1/sc22/wg21/docs/cwg\_defects.html#727
01975
01976     // /**
01977     //  * @brief Checks whether a simplex is on a boundary.
01978     //  *
01979     //  * @param[in] s SimplexID of interest
01980     //  *
01981     //  * @tparam k Dimension of the simplex
01982     //  *
01983     //  * @return True if the simplex interacts with a
01984     //  *         topLevel-1 simplex which is on a boundary.
01985     //  */
01986     // template <std::size_t k>
01987     // bool onBoundary(const SimplexID<k> s) const
01988     // {
01989     //     for(auto p : s.ptr->_up)
01990     //     {
01991     //         if(onBoundary(SimplexID<k+1>(p.second)))
01992     //             return true;
01993     //     }
01994     //     return false;
01995     // }
01996
01997     // /**
01998     //  * @brief Specialization of the facets
01999     //  *
02000     //  * @param[in] s SimplexID of interest
02001     //  *
02002     //  * @tparam k Dimension of the simplex
02003     //  *
02004     //  * @return True if s is on a boundary
02005     //  */
02006     // template<>
02007     // bool onBoundary(const SimplexID<topLevel> s) const
02008     // {
02009     //     for(auto p : s.ptr->_down){
02010     //         if(onBoundary(SimplexID<topLevel-1>(p.second)))
02011     //             return true;

```

```

02012         //      }
02013         //      return false;
02014     // }
02015
02016     // /**
02017     // * @brief      Specialization of the topLevel-1 simplices
02018     // *
02019     // * @param[in]   s      SimplexID of interest
02020     // *
02021     // * @tparam      k      Dimension of the simplex
02022     // *
02023     // * @return      True if s is on a boundary
02024     // */
02025     // template<>
02026     // bool onBoundary(const SimplexID<topLevel-1> s) const
02027     // {
02028     //     return s.ptr->_up.size() != 2;
02029     // }
02030
02031
02032
02033
02034
02044     template <std::size_t L, std::size_t R>
02045     bool leq(SimplexID<L> lhs, SimplexID<R> rhs) const
02046     {
02047         auto name_lhs = get_name(lhs);
02048         auto name_rhs = get_name(rhs);
02049
02050         std::size_t i = 0;
02051         for (std::size_t j = 0; i < L && j < R; ++j)
02052         {
02053             if (name_lhs[i] == name_rhs[j])
02054             {
02055                 ++i;
02056             }
02057         }
02058         return (i == L);
02059     }
02060
02073     template <std::size_t L, std::size_t R>
02074     bool eq(SimplexID<L>, SimplexID<R>) const
02075     {
02076         return false;
02077     }
02078
02089     template <std::size_t k>
02090     bool eq(SimplexID<k> lhs, SimplexID<k> rhs) const
02091     {
02092         auto name_lhs = get_name(lhs);
02093         auto name_rhs = get_name(rhs);
02094
02095         for (std::size_t i = 0; i < k; ++i)
02096         {
02097             if (name_lhs[i] != name_rhs[i])
02098             {
02099                 return false;
02100             }
02101         }
02102         return true;
02103     }
02104
02116     template <std::size_t L, std::size_t R>
02117     bool lt(SimplexID<L> lhs, SimplexID<R> rhs) const
02118     {
02119         return L < R && leq(lhs, rhs);
02120     }
02121
02122 private:
02130     template <std::size_t level, std::size_t foo>
02131     struct nearBoundaryH
02132     {
02133         static bool apply(const SimplexID<level> s){
02134             auto name = s.indices();
02135             KeyType down[level-1];
02136
02137             for(std::size_t i = 0; i < level; ++i){
02138                 std::size_t k = 0;
02139                 for(std::size_t j = 0; j < level; ++j){
02140                     if (i != j){
02141                         down[k++] = name[j];
02142                     }
02143                 }
02144                 if(onBoundaryH<l, 0>::apply(
02145                     get_down_recurse<level, level-1>::apply(down, s.ptr)
02146                 ))
02147                     return true;
02148             }
02149             return false;
02150         }
02151     }

```

```

02151     };
02152
02159     template <std::size_t foo>
02160     struct nearBoundaryH<1, foo>
02161     {
02162         static bool apply(const SimplexID<1> s){
02163             if(onBoundaryH<1, 0>::apply(s))
02164                 return true;
02165             return false;
02166         }
02167     };
02168
02176     template <std::size_t level, std::size_t foo>
02177     struct onBoundaryH
02178     {
02186         static bool apply(const SimplexID<level> s)
02187         {
02188             for(auto p : s.ptr->_up)
02189             {
02190                 if(onBoundaryH<level+1, foo>::apply(SimplexID<level+1>(p.second)))
02191                     return true;
02192             }
02193             return false;
02194         }
02195     };
02196
02203     template <std::size_t foo>
02204     struct onBoundaryH<topLevel, foo>
02205     {
02213         static bool apply(const SimplexID<topLevel> s)
02214         {
02215             for(auto p : s.ptr->_down){
02216                 if(onBoundaryH<topLevel-1, foo>::apply(SimplexID<topLevel-1>(p.second)))
02217                     return true;
02218             }
02219             return false;
02220         }
02221     };
02222
02229     template <std::size_t foo>
02230     struct onBoundaryH<bdryLevel, foo>
02231     {
02239         static bool apply(const SimplexID<bdryLevel> s)
02240         {
02241             return s.ptr->_up.size() < 2;
02242         }
02243     };
02244
02252     template <std::size_t level, std::size_t foo>
02253     struct remove_recurse
02254     {
02269         template <typename T>
02270         static std::size_t apply(type_this* that, T begin, T end, std::size_t &count)
02271         {
02272             std::set<Node<level+1>*> next;
02273             // for each node of interest...
02274             for (auto i = begin; i != end; ++i)
02275             {
02276                 auto up = (*i)->_up;
02277                 for (auto j = up.begin(); j != up.end(); ++j)
02278                 {
02279                     next.insert(j->second);
02280                 }
02281                 that->remove_node(*i);
02282                 ++count;
02283             }
02284             return remove_recurse<level+1, foo>::apply(that, next.begin(), next.end(), count);
02285         }
02286     };
02287
02294     template <std::size_t foo>
02295     struct remove_recurse<topLevel, foo>
02296     {
02310         template <typename T>
02311         static std::size_t apply(type_this* that, T begin, T end, std::size_t &count)
02312         {
02313             for (auto i = begin; i != end; ++i)
02314             {
02315                 that->remove_node(*i);
02316                 ++count;
02317             }
02318             return count;
02319         }
02320     };
02321
02328     template <std::size_t level, std::size_t n>
02329     struct get_recurse

```



```

02330     {
02340         static Node<level+n>* apply(const KeyType* s, Node<level>* root)
02341         {
02342             // TODO: We probably don't need to check if root is a valid
02343             // simplex (10)
02344             if (root)
02345             {
02346                 auto p = root->_up.find(*s);
02347                 if (p != root->_up.end())
02348                 {
02349                     return get_recurse<level+1, n-1>::apply(s+1, root->_up.at(*s));
02350                 }
02351                 else
02352                 {
02353                     return nullptr;
02354                 }
02355             }
02356             else
02357             {
02358                 return nullptr;
02359             }
02360         }
02361     };
02362     template <std::size_t level>
02363     struct get_recurse<level, 0>
02364     {
02365         static Node<level>* apply(const KeyType*, Node<level>* root)
02366         {
02367             return root;
02368         }
02369     };
02370     template <std::size_t level, std::size_t n>
02371     struct get_down_recurse
02372     {
02373         static Node<level-n>* apply(const KeyType* s, Node<level>* root)
02374         {
02375             if (root)
02376             {
02377                 auto p = root->_down.find(*s);
02378                 if (p != root->_down.end())
02379                 {
02380                     return get_down_recurse<level-1, n-1>::apply(s+1, root->_down[*s]);
02381                 }
02382                 else
02383                 {
02384                     return nullptr;
02385                 }
02386             }
02387             else
02388             {
02389                 return nullptr;
02390             }
02391         }
02392     };
02393     template <std::size_t level>
02394     struct get_down_recurse<level, 0>
02395     {
02396         static Node<level>* apply(const KeyType*, Node<level>* root)
02397         {
02398             return root;
02399         }
02400     };
02401     template <std::size_t level, std::size_t n>
02402     struct insert_full
02403     {
02404         static Node<level+n>* apply(type_this* that, Node<level>* root, const KeyType* begin)
02405         {
02406             return insert_for<level, n, n>::apply(that, root, begin);
02407         }
02408     };
02409     template <std::size_t level>
02410     struct insert_full<level, 0>
02411     {
02412         static Node<level>* apply(type_this*, Node<level>* root, const KeyType*)
02413         {
02414             return root;
02415         }
02416     };
02417     template <std::size_t level, std::size_t antistep, std::size_t n>
02418     struct insert_for
02419     {

```

```

02516         static Node<level+n>* apply(type_this* that, Node<level>* root, const KeyType* begin)
02517     {
02518         insert_raw<level, n-antistep>::apply(that, root, begin);
02519         return insert_for<level, antistep-1, n>::apply(that, root, begin);
02520     }
02521 };
02522
02523 template <std::size_t level, std::size_t n>
02524 struct insert_for<level, 1, n>
02525 {
02526     static Node<level+n>* apply(type_this* that, Node<level>* root, const KeyType* begin)
02527     {
02528         return insert_raw<level, n-1>::apply(that, root, begin);
02529     }
02530 };
02531
02532 template <std::size_t level, std::size_t n>
02533 struct insert_raw
02534 {
02535     static Node<level+n+1>* apply(type_this* that, Node<level>* root, const KeyType* begin)
02536     {
02537         KeyType v = *(begin+n);
02538         Node<level+1>* nn;
02539         // if root->v doesn't exist then create it
02540         auto iter = root->_up.find(v);
02541         if (iter == root->_up.end())
02542         {
02543             nn = that->create_node<level+1>();
02544
02545             nn->_down[v] = root;
02546             root->_up[v] = nn;
02547             that->backfill(root, nn, v);
02548         }
02549         else
02550         {
02551             nn = iter->second; // otherwise get it
02552         }
02553         return insert_full<level+1, n>::apply(that, nn, begin);
02554     }
02555 };
02556
02557 template <std::size_t level>
02558 void backfill(Node<level>* root, Node<level+1>* nn, KeyType value)
02559 {
02560     for (auto curr = root->_down.begin(); curr != root->_down.end(); ++curr)
02561     {
02562         int v = curr->first;
02563
02564         Node<level-1>* parent = curr->second;
02565         Node<level>* child = parent->_up[value];
02566
02567         nn->_down[v] = child;
02568         child->_up[v] = nn;
02569     }
02570 }
02571
02572 void backfill(Node<0>*, Node<1>*, int)
02573 {
02574     return;
02575 }
02576
02577 template <std::size_t level>
02578 Node<level>* create_node()
02579 {
02580     // Create the new node
02581     auto p = new Node<level>(node_count++);
02582     ++(level_count[level]); // Increment the count in the level
02583
02584     // node_count-1 to match the internal IDs correctly.
02585     MAYBE_UNUSED bool ret = std::get<level>(levels).insert(
02586         std::pair<std::size_t, NodePtr<level>>(node_count-1, p)).second;
02587     assert(ret);
02588     /*
02589     // sanity check to make sure there aren't duplicate keys...
02590     if (ret==false) {
02591         std::cout << "Error: Node '" << node_count << "' already existed
02592             with value " << *p << std::endl;
02593     }
02594     */
02595     return p;
02596 }
02597
02598 template <std::size_t level>
02599 void remove_node(Node<level>* p)
02600 {
02601     for (auto curr = p->_down.begin(); curr != p->_down.end(); ++curr)

```

```

02667         {
02668             curr->second->_up.erase(curr->first);
02669         }
02670         for (auto curr = p->_up.begin(); curr != p->_up.end(); ++curr)
02671         {
02672             curr->second->_down.erase(curr->first);
02673         }
02674         --(level_count[level]);
02675         std::get<level>(levels).erase(p->_node);
02676         delete p;
02677     }
02678
02684     void remove_node(Node<1>* p)
02685     {
02686         // This for loop should only have a single iteration.
02687         for (auto curr = p->_down.begin(); curr != p->_down.end(); ++curr)
02688         {
02689             unused_vertices.insert(curr->first);
02690             curr->second->_up.erase(curr->first);
02691         }
02692         for (auto curr = p->_up.begin(); curr != p->_up.end(); ++curr)
02693         {
02694             curr->second->_down.erase(curr->first);
02695         }
02696         --(level_count[1]);
02697         std::get<1>(levels).erase(p->_node);
02698         delete p;
02699     }
02700
02706     void remove_node(Node<0>* p)
02707     {
02708         for (auto curr = p->_up.begin(); curr != p->_up.end(); ++curr)
02709         {
02710
02711             curr->second->_down.erase(curr->first);
02712         }
02713         --(level_count[0]);
02714         std::get<0>(levels).erase(p->_node);
02715         delete p;
02716     }
02717
02723     void remove_node(Node<topLevel>* p)
02724     {
02725         for (auto curr = p->_down.begin(); curr != p->_down.end(); ++curr)
02726         {
02727             curr->second->_up.erase(curr->first);
02728         }
02729         --(level_count[topLevel]);
02730         std::get<topLevel>(levels).erase(p->_node);
02731         delete p;
02732     }
02733
02735     NodePtr<0> _root;
02737     std::size_t node_count;
02739     std::array<std::size_t, numLevels> level_count;
02741     using NodePtrLevel = typename
02743     util::int_type_map<std::size_t, std::tuple, LevelIndex, NodePtr>::type;
02745     typename util::type_map<NodePtrLevel, detail::map::type> levels;
02746     index_tracker::index_tracker<KeyType> unused_vertices;
02747 };
02748
02764 template <typename KeyType, typename ... Ts>
02765 using AbstractSimplicialComplex = simplicial_complex<
02766     detail::simplicial_complex_traits_default<KeyType, Ts...> >;
02767
02769 namespace simplex_set_detail{
02780 template <typename SimplexID>
02781 struct hashSimplexID{
02792     std::size_t operator()(const SimplexID nid) const
02793     {
02794         return std::hash<std::uintptr_t>()(static_cast<uintptr_t>(nid));
02795     }
02796 };
02797 } // end namespace simplex_set_detail
02799
02801 template <typename T> using NodeSet =
02802     std::unordered_set<T, simplex_set_detail::hashSimplexID<T> >;
02803 } // end namespace casc

```

## 10.17 include/casc/stringutil.h File Reference

String utilities for CASC.

```
#include <string>
```

## Namespaces

- namespace `casc`  
*Namespace for everything CASC.*

## Functions

- `template<typename T, std::size_t k>`  
`std::string casc::to\_string (const std::array< T, k > &A)`  
*Returns a string representation of the vertex subsimplicies of a given simplex.*

## 10.18 stringutil.h

[Go to the documentation of this file.](#)

```
00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
00009  * modify it under the terms of the GNU Lesser General Public
00010  * License as published by the Free Software Foundation; either
00011  * version 2.1 of the License, or (at your option) any later version.
00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00029
00030 #pragma once
00031
00032 #include <string>
00033
00034 namespace casc
00035 {
00047 template <typename T, std::size_t k>
00048 std::string to_string(const std::array<T,k>& A)
00049 {
00050     if (k==0) {
00051         return "{root}";
00052     }
00053     std::string out;
00054     out += "{";
00055     for(int i = 0; i + 1 < k; ++i)
00056     {
00057         out += std::to_string(A[i]) + ",";
00058     }
00059     if(k > 0)
00060     {
00061         out += std::to_string(A[k-1]);
00062     }
00063     out += "}";
00064     return out;
00065 }
00066 } // end namespace casc
```

## 10.19 include/casc/typetraits.h File Reference

Helper functions for debugging template types.

### Functions

- `template<class T>`  
`CONSTEXPR14_TN static_string type_name ()`  
*Print the typename of an object at compile time.*

### 10.19.1 Detailed Description

This is copied directly from this very helpful post from [Stackoverflow](#).

### 10.19.2 Function Documentation

#### 10.19.2.1 type\_name()

```
template<class T>
CONSTEXPR14_TN static_string type_name ()
```

Example usage:

```
std::cout << "decltype(i) is " << type_name<decltype(i)>() << '\n';
```

## 10.20 typetraits.h

[Go to the documentation of this file.](#)

```
00001
00008
00010 #pragma once
00011
00012 #include <cstddef>
00013 #include <stdexcept>
00014 #include <cstring>
00015 #include <ostream>
00016
00017 #ifndef _MSC_VER
00018 #   if __cplusplus < 201103
00019 #       define CONSTEXPR11_TN
00020 #       define CONSTEXPR14_TN
00021 #       define NOEXCEPT_TN
00022 #   elif __cplusplus < 201402
00023 #       define CONSTEXPR11_TN constexpr
00024 #       define CONSTEXPR14_TN
00025 #       define NOEXCEPT_TN noexcept
00026 #   else
00027 #       define CONSTEXPR11_TN constexpr
00028 #       define CONSTEXPR14_TN constexpr
00029 #       define NOEXCEPT_TN noexcept
00030 #   endif
00031 #else // _MSC_VER
00032 #   if _MSC_VER < 1900
00033 #       define CONSTEXPR11_TN
00034 #       define CONSTEXPR14_TN
00035 #       define NOEXCEPT_TN
00036 #   elif _MSC_VER < 2000
00037 #       define CONSTEXPR11_TN constexpr
00038 #       define CONSTEXPR14_TN
```

```

00039 #   define NOEXCEPT_TN noexcept
00040 #   else
00041 #   define CONSTEXPR11_TN constexpr
00042 #   define CONSTEXPR14_TN constexpr
00043 #   define NOEXCEPT_TN noexcept
00044 #   endif
00045 #endif // _MSC_VER
00046
00047 class static_string
00048 {
00049     const char* const p_;
00050     const std::size_t sz_;
00051
00052 public:
00053     typedef const char* const_iterator;
00054
00055     template <std::size_t N>
00056     CONSTEXPR11_TN static_string(const char(&a)[N]) NOEXCEPT_TN
00057         : p_(a)
00058         , sz_(N-1)
00059         {}
00060
00061     CONSTEXPR11_TN static_string(const char* p, std::size_t N) NOEXCEPT_TN
00062         : p_(p)
00063         , sz_(N)
00064         {}
00065
00066     CONSTEXPR11_TN const char* data() const NOEXCEPT_TN {return p_;}
00067     CONSTEXPR11_TN std::size_t size() const NOEXCEPT_TN {return sz_;}
00068
00069     CONSTEXPR11_TN const_iterator begin() const NOEXCEPT_TN {return p_;}
00070     CONSTEXPR11_TN const_iterator end() const NOEXCEPT_TN {return p_ + sz_;}
00071
00072     CONSTEXPR11_TN char operator[](std::size_t n) const
00073     {
00074         return n < sz_ ? p_[n] : throw std::out_of_range("static_string");
00075     }
00076 };
00077
00078 inline
00079 std::ostream&
00080 operator<<(std::ostream& os, static_string const& s)
00081 {
00082     return os.write(s.data(), s.size());
00083 }
00084
00085
00094 template <class T>
00095 CONSTEXPR14_TN
00096 static_string
00097 type_name()
00098 {
00099 #ifdef __clang__
00100     static_string p = __PRETTY_FUNCTION__;
00101     return static_string(p.data() + 31, p.size() - 31 - 1);
00102 #elif defined(__GNUC__)
00103     static_string p = __PRETTY_FUNCTION__;
00104 #   if __cplusplus < 201402
00105     return static_string(p.data() + 36, p.size() - 36 - 1);
00106 #   else
00107     return static_string(p.data() + 46, p.size() - 46 - 1);
00108 #   endif
00109 #elif defined(_MSC_VER)
00110     static_string p = __FUNCSIG__;
00111     return static_string(p.data() + 38, p.size() - 38 - 7);
00112 #endif
00113 }

```

## 10.21 include/casc/util.h File Reference

Metatemplate pack expansion helpers.

```

#include <utility>
#include <array>

```

## Data Structures

- struct [util::range< T >](#)  
*A range object to support range based for loops.*
- struct [util::type\\_holder< Ts >](#)  
*Queue based data structure to hold list of types.*
- struct [util::type\\_holder< T, Ts... >](#)  
*Partial specialization to allow FIFO access of typenames.*
- struct [util::type\\_get< k, T >](#)  
*Helper to get the kth element from a [type\\_holder](#).*
- struct [util::type\\_get< 0, type\\_holder< Ts... > >](#)  
*Specialization for terminal case.*
- struct [util::type\\_get< k, type\\_holder< Ts... > >](#)  
*Specialization to recursively pop types to get the kth type.*
- struct [util::type\\_map< C, V >](#)  
*Map the types in C into  $V<T>$ .*
- struct [util::int\\_type\\_map< IntegerType, OutHolder, IntegerSequence, F >](#)  
*Maps an integer sequence and typename, F, into outholder.*
- struct [util::type\\_swap< TUPLE, HOLDER\\_FULL >](#)  
*Move a list of types from one container to another.*
- struct [util::type\\_swap< TUPLE, HOLDER< Ts... > >](#)  
*Move a list of types from one container to another.*
- struct [util::reverse\\_sequence< Integer, IntegerSequence >](#)  
*Reverse an Integer Sequence.*
- struct [util::remove\\_first\\_val< Integer, IntegerSequence >](#)  
*General template for removing the first value from a type holder.*
- struct [util::remove\\_first\\_val< Integer, InHolder< Integer, I, Is... > >](#)  
*Specialization for removing first integer from a sequence of compile time integers.*

## Namespaces

- namespace [util](#)  
*Metatemplate programming utilities namespace.*

## Functions

- template<typename T>  
[range< T > util::make\\_range](#) (T b, T e)  
*Make a range object.*
- template<typename T>  
[range< T > util::make\\_range](#) (std::pair< T, T > p)  
*Makes a range object.*
- template<class Integer, typename IntegerSequence, typename Fn, typename ... Args>  
[void util::int\\_for\\_each](#) (Fn &&f, Args &&... args)  
*Calls a function  $f.apply<k>()$  for a sequence of integer k's.*

## 10.22 util.h

[Go to the documentation of this file.](#)

```

00001 /*
00002  * *****
00003  * This file is part of the Colored Abstract Simplicial Complex library.
00004  * Copyright (C) 2016-2017
00005  * by Christopher Lee, John Moody, Rommie Amaro, J. Andrew McCammon,
00006  * and Michael Holst
00007  *
00008  * This library is free software; you can redistribute it and/or
00009  * modify it under the terms of the GNU Lesser General Public
00010  * License as published by the Free Software Foundation; either
00011  * version 2.1 of the License, or (at your option) any later version.
00012  *
00013  * This library is distributed in the hope that it will be useful,
00014  * but WITHOUT ANY WARRANTY; without even the implied warranty of
00015  * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
00016  * Lesser General Public License for more details.
00017  *
00018  * You should have received a copy of the GNU Lesser General Public
00019  * License along with this library; if not, write to the Free Software
00020  * Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA 02110-1301 USA
00021  *
00022  * *****
00023  */
00024
00029
00030 #pragma once
00031
00032 #include <utility>
00033 #include <array>
00034
00036 namespace util
00037 {
00048 template<typename T> struct range
00049 {
00050
00058     template <class C>
00059     range(C &&c) : _begin(c.begin()), _end(c.end()) {}
00060
00067     range(T b, T e) : _begin(b), _end(e) {}
00068
00074     T begin() { return _begin; }
00075
00081     T end() { return _end; }
00082
00083     private:
00085         T _begin;
00087         T _end;
00088 };
00089
00100 template<typename T> range<T> make_range(T b, T e)
00101 {
00102     return range<T>(std::move(b), std::move(e));
00103 }
00104
00114 template<typename T> range<T> make_range(std::pair<T, T> p)
00115 {
00116     return range<T>(std::move(p.first), std::move(p.second));
00117 }
00118
00127 template <typename ... Ts>
00128 struct type_holder
00129 {
00131     static const std::size_t size = sizeof ... (Ts);
00132 };
00133
00140 template <typename T, typename ... Ts>
00141 struct type_holder<T, Ts...>
00142 {
00144     using head = T;
00146     using tail = type_holder<Ts...>;
00148     static const std::size_t size = 1 + type_holder<Ts...>::size;
00149 };
00150
00159 template <std::size_t k, typename T>
00160 struct type_get {};
00161
00167 template <typename ... Ts>
00168 struct type_get<0, type_holder<Ts...> >
00169 {
00171     using type = typename type_holder<Ts...>::head;
00172 };
00173

```



```

00180 template <std::size_t k, typename ... Ts>
00181 struct type_get<k, type_holder<Ts...> >
00182 {
00183     using type = typename type_get<k-1, typename type_holder<Ts...>::tail::type;
00184 };
00185
00186
00187 namespace detail
00188 {
00189     template <class C, template <typename> class V, typename ... Rs>
00190     struct type_map_helper {};
00191
00192     template <template <class ...> class G, template <typename> class V, typename ... Rs>
00193     struct type_map_helper<G<>, V, Rs...>
00194     {
00195         using type = G<Rs...>;
00196     };
00197
00198     template <template < class ...> class G, typename T, typename ... Ts, template <typename> class V,
00199             typename ... Rs>
00200     struct type_map_helper<G<T, Ts...>, V, Rs...>
00201     {
00202         using type = typename type_map_helper<G<Ts...>, V, Rs..., V<T> >::type;
00203     };
00204 } // end of namespace detail
00205
00206 template <class C, template <typename> class V>
00207 struct type_map
00208 {
00209     using type = typename detail::type_map_helper<C, V>::type;
00210 };
00211
00212 namespace detail
00213 {
00214     template <class IntegerType, template <class ...> class OutHolder, class IntegerSequence, template
00215             <IntegerType> class F, typename ... Accumulators>
00216     struct int_type_map_helper {};
00217
00218     template <class Integer, template <class ...> class OutHolder, template <class, Integer...> class
00219             InHolder, template <Integer> class F, class ... Accumulator>
00220     struct int_type_map_helper<Integer, OutHolder, InHolder<Integer>, F, Accumulator...>
00221     {
00222         using type = OutHolder<Accumulator...>;
00223     };
00224
00225     template <class Integer, template <class ...> class OutHolder, template <class, Integer...> class
00226             InHolder, Integer I, Integer... Is, template <Integer> class F, class ... Accumulator>
00227     struct int_type_map_helper<Integer, OutHolder, InHolder<Integer, I, Is...>, F, Accumulator...>
00228     {
00229         using type = typename int_type_map_helper<Integer, OutHolder, InHolder<Integer, Is...>, F,
00230             Accumulator..., F<I> >::type;
00231     };
00232 } // end namespace detail
00233
00234 template <class IntegerType, template <class ...> class OutHolder, class IntegerSequence, template
00235             <IntegerType> class F>
00236     struct int_type_map
00237     {
00238         using type = typename detail::int_type_map_helper<IntegerType, OutHolder, IntegerSequence,
00239             F>::type;
00240     };
00241
00242     template <template <class ...> class TUPLE, typename HOLDER_FULL>
00243     struct type_swap
00244     {};
00245
00246     template <template <class ...> class TUPLE, template <class ...> class HOLDER, typename ... Ts>
00247     struct type_swap<TUPLE, HOLDER<Ts...> >
00248     {
00249         using type = TUPLE<Ts...>;
00250     };
00251
00252     namespace detail
00253     {
00254         template <class Integer, class IntegerSequence, Integer... Accumulator>
00255         struct reverse_sequence_helper {};
00256
00257         template <class Integer,
00258                 template<class, Integer...> class InHolder,
00259                 Integer... Accumulator>
00260         struct reverse_sequence_helper<Integer, InHolder<Integer>, Accumulator...>
00261         {
00262             using type = InHolder<Integer, Accumulator...>;
00263         };
00264
00265         template <class Integer,
00266                 template<class, Integer...> class InHolder,
00267                 Integer I, Integer... Is,

```

```

00374         Integer... Accumulator>
00375 struct reverse_sequence_helper<Integer, InHolder<Integer, I, Is...>, Accumulator...>
00376 {
00377     // Push the first type into the Accumulator and recurse.
00378     using type = typename reverse_sequence_helper<Integer,
00379                                         InHolder<Integer, Is...>, I, Accumulator...>::type;
00380 };
00381 } // end namespace detail
00382 } // end namespace detail
00383
00384
00391 template <class Integer, class IntegerSequence>
00392 struct reverse_sequence
00393 {
00394     using type = typename detail::reverse_sequence_helper<Integer, IntegerSequence>::type;
00395 };
00396
00397
00398
00405 template <class Integer, class IntegerSequence>
00406 struct remove_first_val {};
00407
00417 template <class Integer,
00418         template<class, Integer...> class InHolder,
00419         Integer I, Integer... Is>
00420 struct remove_first_val<Integer, InHolder<Integer, I, Is...> >
00421 {
00422     using type = InHolder<Integer, Is...>;
00423 };
00424
00425
00427 namespace detail
00428 {
00433 template <typename Integer, typename IntegerSequence, typename Fn, typename ... Args>
00434 struct int_for_each_helper {};
00435
00445 template <class Integer, template <class, Integer...> class InHolder,
00446         Integer I, typename Fn, typename ... Args>
00447 struct int_for_each_helper<Integer, InHolder<Integer, I>, Fn, Args...>
00448 {
00449     static void apply(Fn &&f, Args && ... args)
00450     {
00451         f.template apply<I>(std::forward<Args>(args) ...);
00452     }
00453 };
00454
00465 template <class Integer, template <class, Integer...> class InHolder,
00466         Integer I, Integer... Is, typename Fn, typename ... Args>
00467 struct int_for_each_helper<Integer, InHolder<Integer, I, Is...>, Fn, Args...>
00468 {
00469     static void apply(Fn &&f, Args && ... args)
00470     {
00471         f.template apply<I>(std::forward<Args>(args) ...);
00472         int_for_each_helper<Integer, InHolder<Integer, Is...>, Fn, Args...>::apply(
00473             std::forward<Fn>(f),
00474             std::forward<Args>(args) ...);
00475     }
00476 };
00477 } // end namespace detail
00478
00491 template <class Integer, typename IntegerSequence, typename Fn, typename ... Args>
00492 void int_for_each(Fn &&f, Args && ... args)
00493 {
00494     detail::int_for_each_helper<Integer, IntegerSequence, Fn, Args...>::apply(std::forward<Fn>(f),
00495                                     std::forward<Args>(args) ...);
00496 }
00497 } // End of namespace util

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